

CSE 504 Compiler Design

Top-Down Parsing (Predictive Parsing)

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Parsing

- Parsing is the process of determining if a string of tokens can be generated by a grammar
- For any context-free grammar, there is a parser that can parse a string of n tokens in $O(n^3)$ times.
- For programming languages, we can generally construct a grammar that can be parsed quickly (in linear time).
- Top-Down parsing
 - Build parse trees from the root node to leaf nodes.
 - Simple (parsers can be made manually), but limited.
- Bottom-Up parsing
 - Build parse trees from leaves towards the root.
 - More complex (parsers are generated from software tools), but more generic.

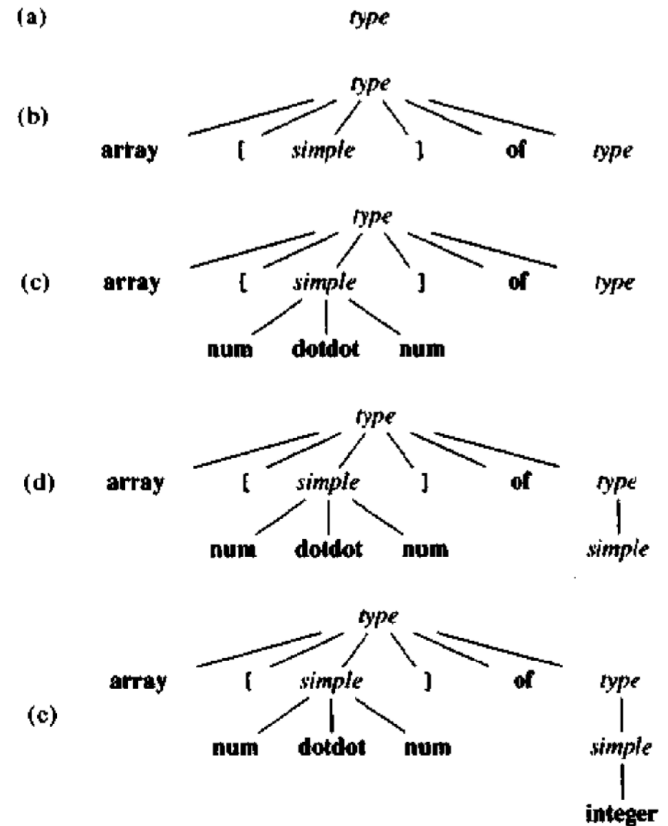
Top-Down Parsing

- Start from the **root**, labeled with the **starting nonterminal**, repeatedly perform the following two steps.
 - At node **n**, labeled with nonterminal **A**, select one of the **productions for A** and **construct children at n** for the symbols on the **RHS of the production**.
 - Find the next node at which a subtree is to be constructed.

```

type → simple
      | ↑ id
      | array [ simple ] of type
simple → integer
      | char
      | num dotdot num
    
```

array [num dotdot num] of integer



Predictive Parsing

- Recursive Decent Parsing
 - A top-down parsing method.
 - For each **nonterminal** of a grammar, **associate a procedure** and execute it to process the input.
- Predictive Parsing
 - A recursive decent parsing method.
 - The **lookahead** symbol unambiguously determines the procedure for each nonterminal.
 - In the next example, we use an additional procedure **match** to advance the next input token if the argument matches the lookahead symbol.

Pseudo-code for a predictive parser

```
procedure type ;  
begin  
  if lookahead is in { integer, char, num } then  
    simple  
  else if lookahead = '↑' then begin  
    match('↑'); match(id)  
  end  
  else if lookahead = array then begin  
    match(array); match('['); simple; match(']'); match(of); type  
  end  
  else error  
end;
```

```
procedure simple ;  
begin  
  if lookahead = integer then  
    match(integer)  
  else if lookahead = char then  
    match(char)  
  else if lookahead = num then begin  
    match(num); match(dotdot); match(num)  
  end  
  else error  
end;  
  
procedure match(t: token);  
begin  
  if lookahead = t then  
    lookahead := nexttoken  
  else error  
end;
```

Predictive Parsing: procedure FIRST

- Predictive parsing relies on what first symbols can be generated by the RHS of a production.
- **FIRST(α)**
 - Let α be the RHS of a production for nonterminal A
 - FIRST(α) returns the set of tokens that appear as the first symbol of the strings generated from α .
 - For recursive decent parsing without backtracking, if there are **more than one productions**, their FIRST sets must be **disjoint**.
 - E.g. for $A \rightarrow \alpha \mid \beta$, $\text{FIRST}(\alpha) \cap \text{FIRST}(\beta) = \emptyset$
 - Example:

□ $\text{FIRST}(\text{simple}) = \{ \text{integer, char, num} \}$
 $\text{FIRST}(\uparrow \text{id}) = \{ \uparrow \}$
 $\text{FIRST}(\text{array [simple] of type}) = \{ \text{array} \}$

Designing a Predictive Parser

- The procedures for **nonterminals** do two things
 1. Decide which production to use by looking at the lookahead and $FIRST(\alpha)$.
 - If there are conflicts, we **cannot parse** the grammar with this parsing method.
 - If lookahead doesn't appear in any of the FIRST sets, use the **ϵ -Production**.
 2. Procedures mimic the RHS of a production
 - Nonterminals result in **a call to the procedure** for the nonterminal.
 - Tokens matching the lookahead results in **reading the next input**.
 - If the token does not match the lookahead, **an error** is declared.

Designing a Predictive Parser: Extension to a **syntax directed translation**

1. Construct a predictive parser, ignoring the actions in productions
2. Copy the action from the translation scheme to the parser
 - If an action appears after a grammar symbol X , copy the action after implementing X .
 - If an action appears at the beginning of a production, copy it before implementing the production.

Left Recursion

- A problem with left-recursive grammars
 - Infinite recursion will occur in recursive decent parsers.
 - `expr -> expr + term`
 - The leftmost symbol on the RHS is the same as the LHS of the production
 - The parser may look like

```
procedure expr;  
begin  
    if lookahead is in FIRST('expr + term') then  
    begin  
        expr; match('+'); term;  
    end  
end
```

Fixing the Left Recursion Problem

- Change **Left Recursive** Grammar to **Right Recursive** one

- $A \rightarrow A \alpha \mid \beta$

- $A \rightarrow \beta R$

- $R \rightarrow \alpha R \mid \epsilon$

- **Example**

- $\text{expr} \rightarrow \text{expr} + \text{term} \mid \text{term}$

- $A = \text{expr}, \alpha = + \text{term}, \beta = \text{term}$

- $\text{expr} \rightarrow \text{term rest}$

- $\text{rest} \rightarrow + \text{term rest} \mid \epsilon$

Adapting the Translation Scheme

- If semantic actions are in left recursive productions, carry them along in the production
- Example

```
expr -> expr + term { print('+') }
expr -> expr - term { print('-') }
expr -> term
term -> 0 { print('0') }
...
term -> 9 { print('9') }
```

=>

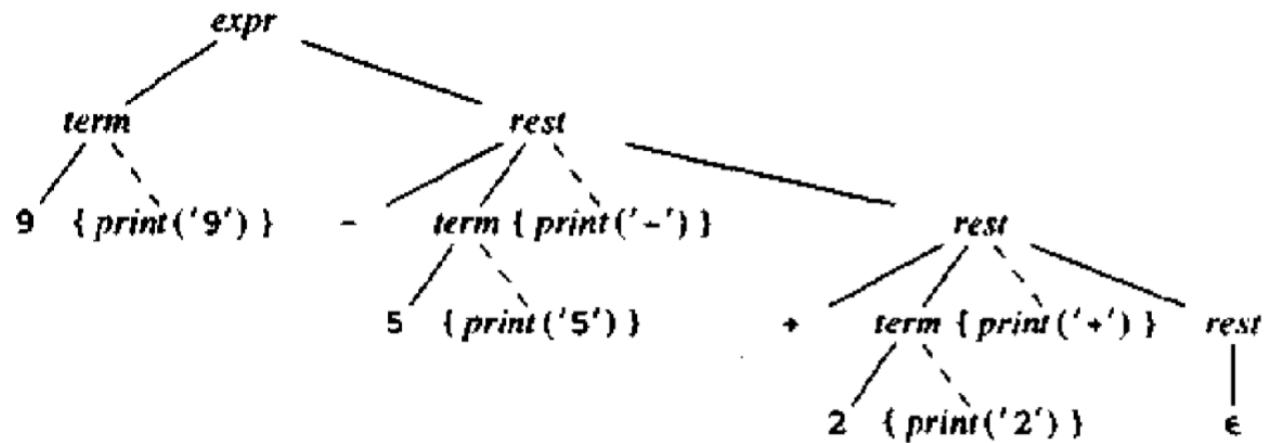
```
expr -> term rest
rest -> + term { print('+') } rest
rest -> - term { print('-') } rest
rest -> ε
term -> 0 { print('0') }
...
term -> 9 { print('9') }
```

- $A \rightarrow A \alpha \mid A \beta \mid \gamma$
- $A \rightarrow \gamma R$
- $R \rightarrow \alpha R \mid \beta R \mid \epsilon$

$A = \text{expr},$
 $\alpha = + \text{ term } \{ \text{print}(\text{'+'}) \},$
 $\beta = - \text{ term } \{ \text{print}(\text{'-'}) \},$
 $\gamma = \text{term}$

Adapting the Translation Scheme

- Example: Translation of 9-5+2 into 95-2+



Procedures for expr, term, and rest

```
expr()
{
    term(); rest();
}

rest()
{
    if (lookahead == '+') {
        match('+'); term(); putchar('+'); rest();
    }
    else if (lookahead == '-') {
        match('-'); term(); putchar('-'); rest();
    }
    else ;
}

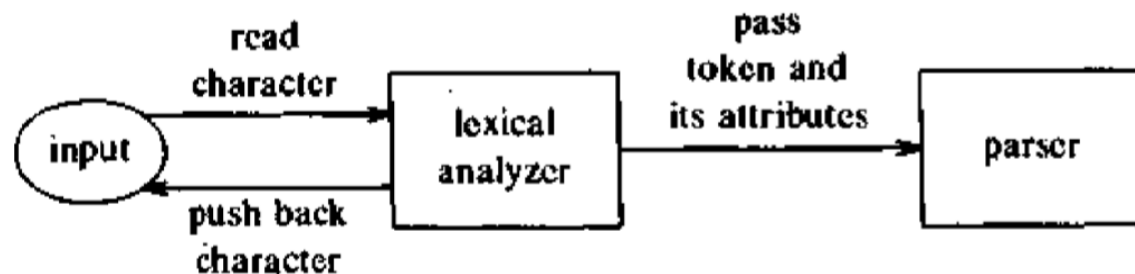
term()
{
    if (isdigit(lookahead)) {
        putchar(lookahead); match(lookahead);
    }
    else error();
}
```

Lexical Analyzer

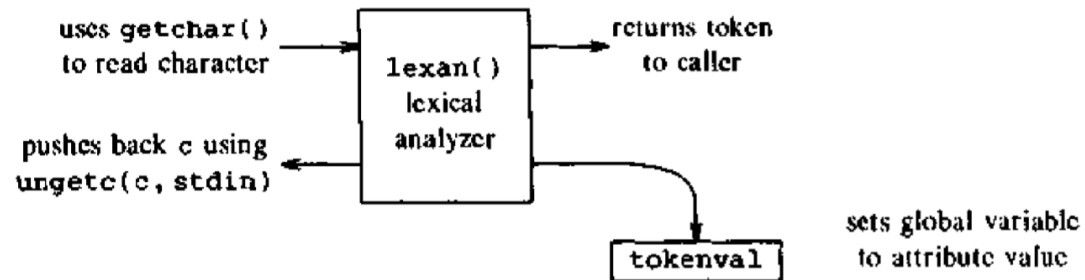
- It converts input to a stream of tokens.
- Lexeme: a sequence of input characters that comprise a single token.
- Insulates parser from the lexeme representation of tokens.
- Frees parsers from removing **white space** and **comments**.
 - Removing white spaces from the grammar can be unnecessarily complex.
- For **numbers**, return num and its value as an attribute.
- For **identifiers**, return id and its symboltable entry as an attribute.
- For **keywords**, need to check if a lexeme is a keyword or an identifier.
 - Easier if the keywords are reserved.

Interface to Lexical Analyzer

- In some situations, the lexical analyzer has to read some characters ahead before it can decide.
 - e.g. to distinguish \geq and $>$, after reading $>$ the lexical analyzer needs to read one more character.
 - The extra characters have to be **pushed back onto the input**.
- The parser hold the produced tokens and their attributes in **a token buffer**.
 - Commonly the buffer holds just one token and **a procedure call** from the parser to the lexical analyzer would work.



A Lexical Analyzer



- Updating the grammar and semantic actions for the factor

- `factor -> (expr)`
 | `NUM { print (NUM.value) }`

- Procedure for factor

```
factor()
{
    if (lookahead == '(') {
        match('('); expr(); match(')');
    }
    else if (lookahead == NUM) {
        printf(" %d ", tokenval); match(NUM);
    }
    else error();
}
```


Symbol Table

- Stores information about various source language constructs.
 - lexeme for the id,
 - type of the id (e.g. procedure, variable, label),
 - its position in storage, ...
- Interface
 - `insert(s, t)` : returns index of the new entry for string `s`, token `t`.
 - `lookup(s)` : returns index of the entry for string `s`, or an invalid index if `s` is not found.