

## CSE 509 class note (4/19)

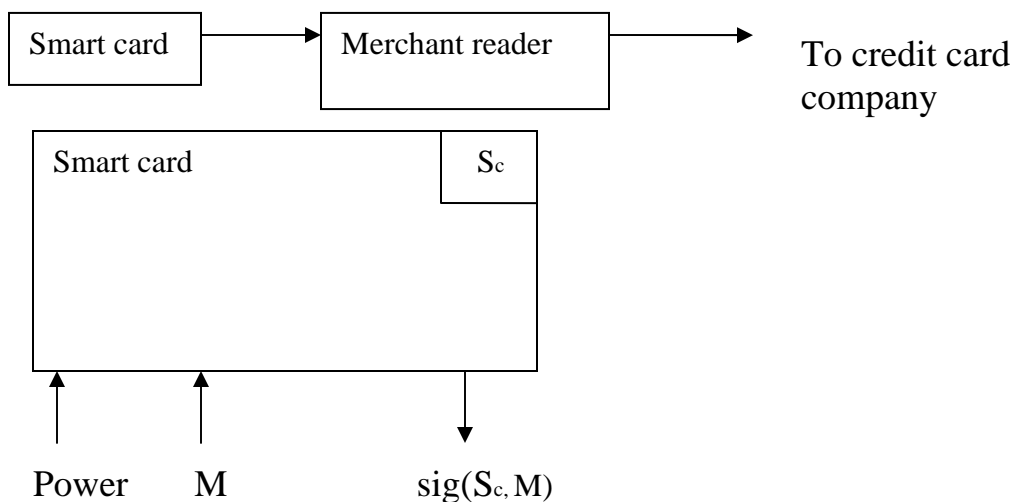
### Side Channel Attacks

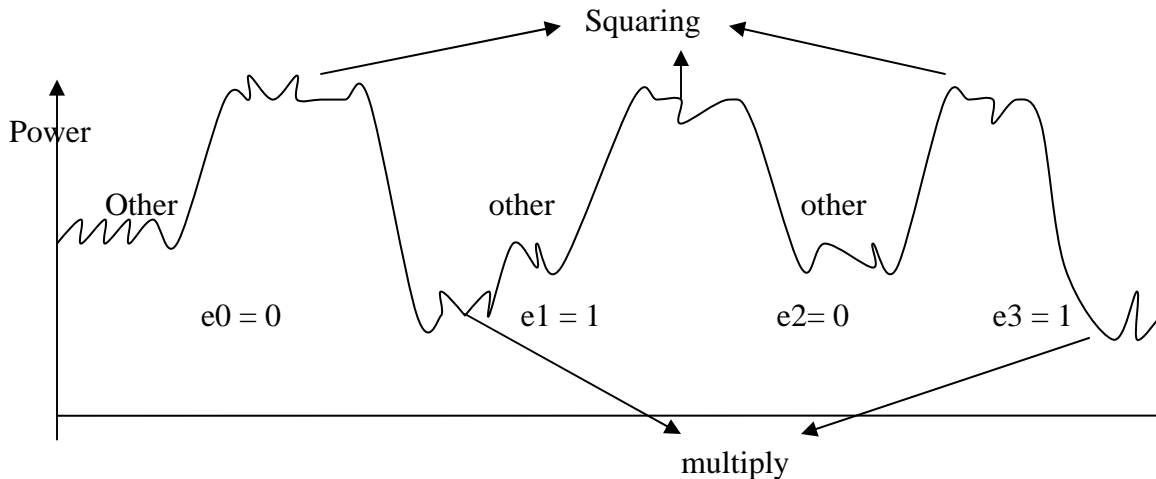
- Timing
- Power
- Sound
- Light
  
- Usability and Security
  - o Depending on Users
  - o Role playing
  
- Modular Exponentiation

```
ModExp(m,e,n)      // M^e mod n
  Let el ... e0=e  // the bits of e
  Let acc = 1
  For i=0 ... l
    if ei==1
      acc = acc*m mod n
      m = m^2 mod n
  return acc;
```

$$\begin{aligned} m^e \bmod n &= m^{(2^0 e_0 + 2^1 e_1 + 2^2 e_2 + \dots + 2^l e_l)} \bmod n \\ &= m^{e_0} * (m^2)^{e_1} * (m^4)^{e_2} * (m^{(2^l)})^{e_l} \bmod n \end{aligned}$$

- Power Analysis (smart cards)





- timing attack against square and multiply
  - some reductions take longer than others
    - o fast reductions
    - o slow reductions
    - o if attackers knows  $acc * m$ , he can predict whether reduction is fast or slow

attacker input	$m_0$	$m_1$	$m_2$	$m_3$	...	$m_k$
time	$t_0$	$t_1$	$t_2$	$t_3$	...	$t_k$

suppose  $e_0 = 1$

- can compute
  - o  $acc$  and  $m$  at end of round 0
- predict whether round 1 will be fast or slow for each message  $m_i$
- let
  - o  $f$  = average time of "fast" messages
  - o  $s$  = average time of "slow" messages
- two cases
  - o  $|s_1 - f_1|$  is small and  $|s_0 - f_0|$  is small  
 $\rightarrow e_1 = 0$
- suppose  $|s_b - f_b|$  is large and  $|s(\sim b) - f(\sim b)|$  is small  
 $\rightarrow e_1 = 1$  and  $e_0 = b$

repeat for round 2, ...,  $l$

- defense
  - o for  $i=0 \dots l$ 
    - if  $e_i == 1$ 
      - $acc = acc * m \bmod n$
    - else
      - $tmp = acc * m \bmod n$
      - $m = m^2 \bmod n$

- RSA binding

to compute  $m^e \bmod n$

- pick random  $r$
- compute  $x = (rm)^e \bmod n$
- compute  $y = r^e \bmod n$
- return  $x/y \bmod n$