

## Sample Questions

### 1. Predicate Logic

Translate the following statements in English into sentences in FOL (First Order Logic).

- Any course in Mathematics is harder than some courses in Computer Science.
- If a course is harder than all courses in Computer Science, it must be in Physics.

### 2. Predicate Logic

Formalize these statements into FOL sentences and put them into clause form.

*Some craftsmen are not artisans. Only artisans are highly paid.*

Use resolution to answer the question: Who is not highly paid?

You will need to use this information for answering the question: *The clause form for  $P(X)$  is  $P(c)$  where  $c$  is a constant.*

### 3. Unification

Assume  $a, b, c$  are constants;  $X, Y, Z, W, U$  are variables. For each pair of sentences, give the most general unifier if it exists:

- $P(a, b, c)$  and  $P(X, Y, Z)$
- $P(X, a, g(X))$  and  $P(f(Y), Y, Z)$
- $\text{Knows}(\text{Father}(Y), Y)$  and  $\text{Knows}(X, X)$
- $\text{Hits}(\text{amy}, \text{beth})$  and  $\text{Loves}(X, X)$
- $L(X, Y, g(a, Y), d)$ ,  $L(Z, c, g(W, U), V)$

### 4. Predicate Logic

Given the set of clauses  $S = \{ \neg C(X) \vee W(X), \neg C(X) \vee R(X), C(a), O(a) \}$  and the goal clause  $G = (O(X) \wedge R(X))$ , show using resolution that  $S \models G$ .

### 5. Concept Learning

Num	Restaurant	Meal	Day	Cost	Reaction
1	The Nines	bkfst	Fri	\$	sick (+)
2	Banfis	lunch	Fri	\$\$	ok (-)
3	The Nines	lunch	Sat	\$	sick (+)
4	Moosewood	bkfst	Sun	\$	ok (-)
5	The Nines	bkfst	Sun	\$\$	ok (-)

- [10 points] Apply the version space algorithm to the example above to learn the concept of *Reaction*. Show each step.
- [2 points] List two inadequacies of the algorithm

## 6. Decision Tree Learning

The following dataset will be used to learn a decision tree for predicting whether a mushroom is edible or not based on its shape, color and odor.

Shape	Color	Odor	Edible
C	B	1	Yes
D	B	1	Yes
D	W	1	Yes
D	W	2	Yes
C	B	2	Yes
D	B	2	No
D	G	2	No
C	U	2	No
C	B	3	No
C	W	3	No
D	W	3	No

- What is entropy  $H(\text{Edible} \mid \text{Order} = 1 \text{ or } \text{Odor} = 3)$ ?
- Which attribute would the decision tree algorithm (described in class) choose to use for root of the tree?
- Draw the full decision tree that will be learned from this training set.

## 7. Naive Bayes Learning

Suppose we are given the following dataset, where A,B,C are input binary random variables, and y is a binary output whose value we want to predict.

A	B	C	y
0	0	1	0
0	1	0	0
1	1	0	0
0	0	1	1
1	1	1	1
1	0	0	1
1	1	0	1

How would a naive Bayes classifier predict  $y$  given this input:  $A=0, B=0, C=1$ . Assume that in case of a tie the classifier always prefers to predict 0 for  $y$ .

**8.** For MLE, EM, Clustering – understand the examples in the lecture slides.