CSE528 Computer Graphics: Theory, Algorithms, and Applications

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Key Elements of Cameras and Geometric Coordinate Systems

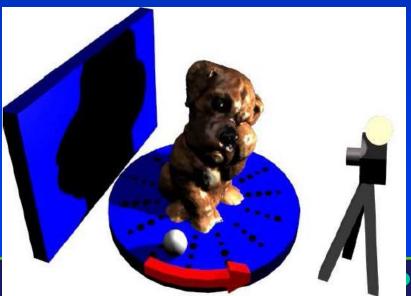
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Image Formation

- Camera
- Light, shape, reflectance, texture





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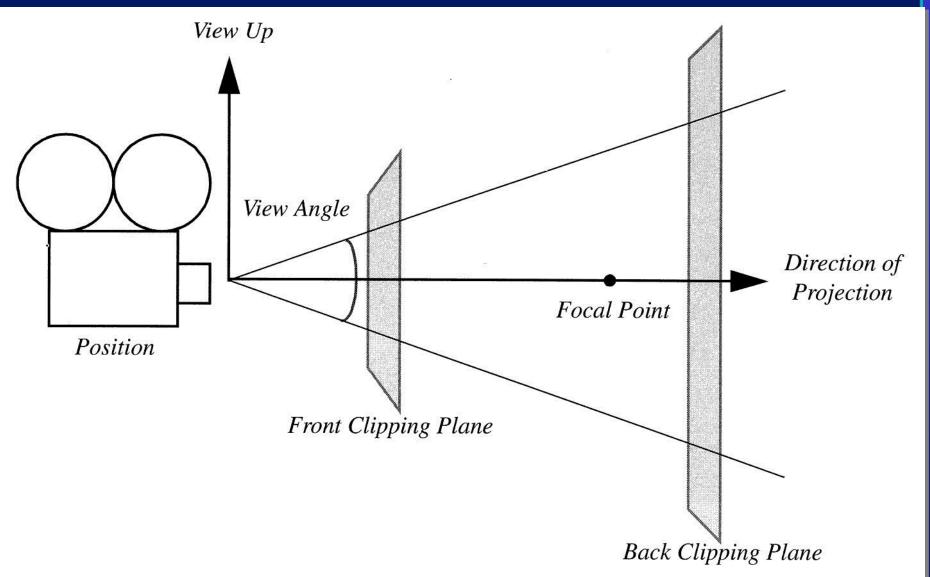
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Cameras

- We have light sources that illuminate 3D objects (or datasets) in our virtual scene within the graphics system
- Light rays interact with surface properties and generate colors according to the illumination model
- But how do we view the scene, select the position and orientation of the viewpoint?
- This is where the virtual camera comes in

Basic Camera Attributes



Basic Camera Attributes

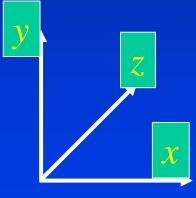
- *Position* given in (x,y,z) coordinates
- Up-vector orients the camera, given in (x,y,z)
- Direction of projection points the camera in some (x,y,z) direction; also called viewing direction
- Why is the up-vector needed if we have a direction of projection?
- Why is the direction of projection needed if we have an up-vector?



Coordinate Systems

- Two kinds of Cartesian coordinate systems: right-handed and left-handed
- Use whichever coordinate system seems most natural in the given context

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CSE528 Lectures



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right-handed system

Coordinate Systems

- You might be familiar with different types of coordinate systems:
 - Cartesian
 - Polar
 - Spherical
 - Cylindrical

 Computer graphics and visualization applications use several distinct coordinate systems: *model*, *world*, *view* and *display*

Usually they use Cartesian coordinates

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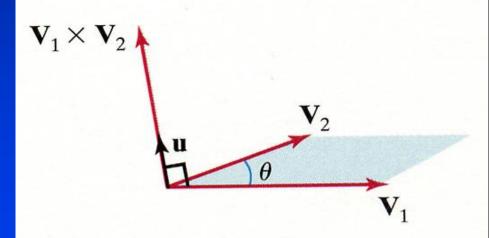
Basic Camera Attributes

- *Front and back clipping planes* determine which objects *might* be visible
- Planes perpendicular to viewing direction
- Specified as distances along viewing direction
- Also called near and far clipping planes
- Objects on near side of front clipping plane and on far side of back clipping plane are invisible
- Objects between the clipping planes may occlude each other and may be fully visible, partially visible, or invisible

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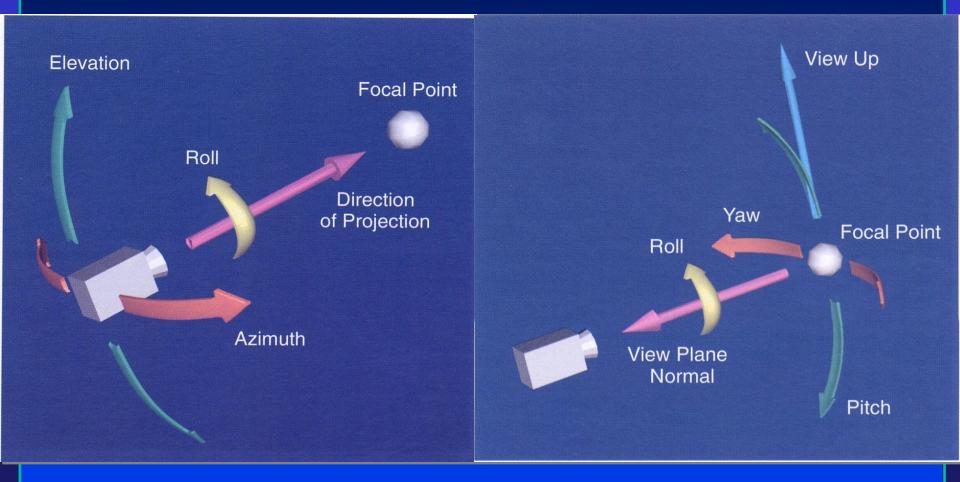


- Changing *azimuth* = rotating camera's position around its view vector w.r.t. focal point
- Changing *elevation* = rotating camera's position around cross-product of view direction and up-vector
- Cross-product of two vectors provides vector in dir. perpendicular to two original vectors



 Changing roll = rotate camera's up-vector about the <u>viewing direction (twisting the camera)</u> <u>Center for Visual Computing</u>

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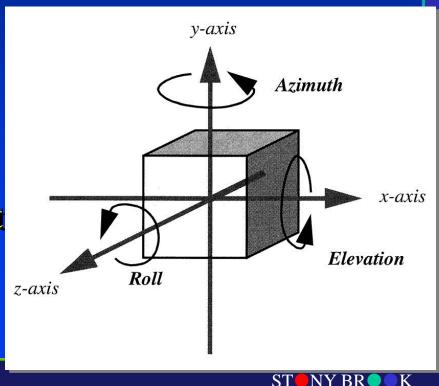
- Changing *yaw* = rotating focal point about the up-vector
- Changing *pitch* = rotating focal point about cross product of view vector and up vector
- Dollying moves camera position along view vector (dollying in and out)
- Once camera attributes are set, objects are *projected* from 3D onto the 2D image plane
- Camera attributes determine which rays of light (that bounced off objects) will enter the camera and contribute to the rendered image

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Actor Geometry: Actor Location and Orientation

- Rotations take place around the origin of the actor
- They are applied as a camera azimuth, elevation and roll, *in that order* – remember, order counts!
- VTK uses this orientation vector-based approach since it is very natural to manipulate objects in this fashion



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- Nuisance to manipulate the camera by changing all those parameters
- Usually its easier to specify camera movements with respect to the camera's *focal point*, the position in space which the camera is pointing at
- Consider taking a portrait (physical analogy):
 - Move around the person
 - Move forward and backward w.r.t. to person
 - Move camera up and down
 - Rotate camera while standing still

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Model Coordinate System

- Coordinate system used to define an object or actor
- Coordinate system will be a natural choice
 - Example: A football might be described using a cylindrical coordinate system
 - What coordinate system might we use for a planet?
- System choice of person who created the object
- Units are application-dependent: inches, meters, cubits, etc.

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Object Representations

- List of vertices: $v_1, v_2, ..., v_n$, each given as (x_i, y_i, z_i)
- List of edges: (v_1, v_3) , (v_4, v_7) , ..., (v_i, v_j) ,...
- List of faces: (e_1, e_3, e_4) , (e_2, e_5, e_8) ,OR
- List of faces: (v_1, v_3, v_5) , (v_6, v_7, v_9) , ...
- When a vertex's position is changed due to transformation, all edges and polygons that include the vertex are consequently changed
- If we apply the same transformations to all vertices, the entire polygonal mesh moves as a unit, which is what we want

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World Coordinate System

- 3D space in which our actors are positioned
- Each actor's model coordinate system has some position and orientation inside the world space
- Many model coordinate systems, only one world coordinate system
- Each actor rotates, scales and translates itself into the world coordinate system
- Lights and cameras are specified with respect to the world coordinate system
- Does a camera have its own coordinate system?

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World Coordinate System

• Example:

- Specify each of our bodies with a cylindrical coordinate system with the head as the origin
- We position ourselves in the room (the world coordinate system) by giving the position of our heads w.r.t. the origin of the room (perhaps some corner)



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View Coordinate System

- Represents what is visible to the camera
- Given by (x,y,z) values
- x, y in [-1, 1]
- z is some depth > 0
- x, y give location of some object in the image plane
- z give distance of object from camera
- A matrix is used to convert from world coordinates into view coordinates (i.e., projection!)
- Perspective effect can be accommodated by this matrix

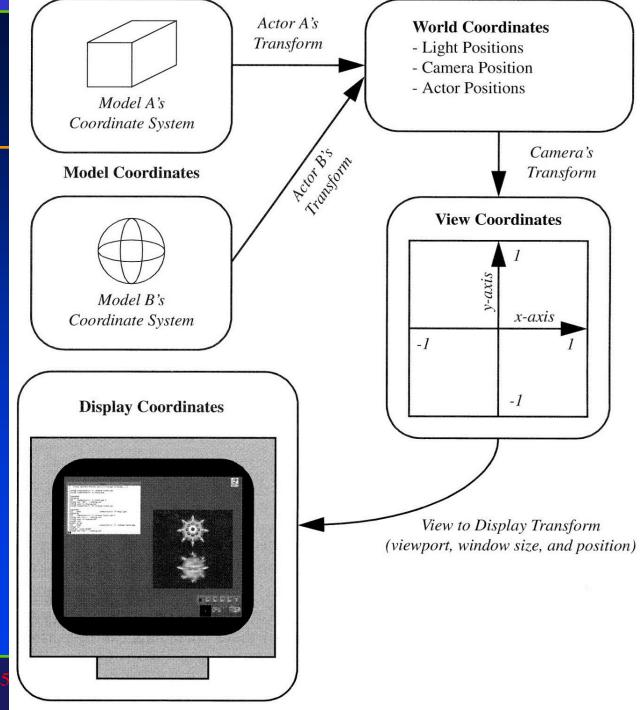


Display Coordinate System

- x, y are pixel values on screen
- z is still the depth
- What are restrictions on x and y?
- Window size helps determine valid range for x, y
- Display can be divided into multiple *viewports*, each of which has its own coordinate system
- Must select which viewport is used for rendering

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Coordinate Systems



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Coordinate Systems (Computer Graphics Pipeline)

- 1. Model coordinates are transformed into
- 2. World coordinates, which are transformed into
- 3. View coordinates, which are transformed into
- 4. Display coordinates, which correspond to pixel positions on the screen

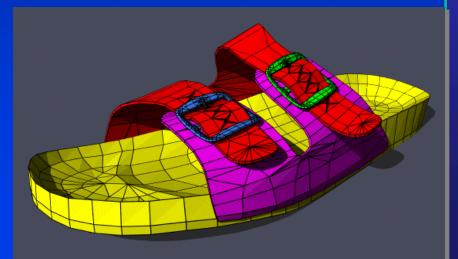
Transformations from one coordinate system to another take place via *coordinate* transformations, which we'll look at now Department of Computer Science

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Coordinate Transformations

- Coordinate transformations allow us to translate, scale and rotate our models in our virtual scene
- In Computer Graphics and Visualization, objects are often represented as meshes consisting of polygons, edges and vertices
- Two vertices define an edge
- Three or more edges define a polygon
- To transform an object, we apply the transformations to the vertices of the mesh





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Coordinate Transformations

- Rather than represent 3D points using three coordinates (x,y,z), we will use four: (x,y,z,w)
- This approach is called homogeneous coordinates
- Transformations will be represented by (4 x 4) matrices
- Why not (3 x 3)?
- Because some transformations including translation cannot be represented by (3 x 3) matrices
- Most of the time w = 1, but there are special transformations for which w ≠ 1

Coordinate Transformations: Translation

- Suppose we wish to translate the point (x,y,z) by the vector (t_x, t_y, t_z)
- This *translation transformation* can be described by the *translation matrix*:

$$\Gamma_{\rm T} = \begin{bmatrix} 1 & 0 & 0 & t_{\rm x} \\ 0 & 1 & 0 & t_{\rm y} \\ 0 & 0 & 1 & t_{\rm z} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

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Coordinate Transformations: Translation

• The new position is given by post-multiplying our point by the translation matrix:

$$\begin{bmatrix} \mathbf{x'} \\ \mathbf{y'} \\ \mathbf{z'} \\ \mathbf{x'} \\ \mathbf{w'} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & \mathbf{t}_{\mathbf{x}} \\ 0 & 1 & 0 & \mathbf{t}_{\mathbf{y}} \\ 0 & 0 & 1 & \mathbf{t}_{\mathbf{z}} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \\ \mathbf{z} \\ 1 \end{bmatrix}$$

• The new position of our point is (x', y', z')

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Coordinate Transformations: Translation

• We can see that the matrix-vector multiplication is equivalent to the following formulas:

$$\begin{bmatrix} \mathbf{x'} \\ \mathbf{y'} \\ \mathbf{z'} \\ \mathbf{x'} \\ \mathbf{w'} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & \mathbf{t}_{\mathbf{x}} \\ 0 & 1 & 0 & \mathbf{t}_{\mathbf{y}} \\ 0 & 0 & 1 & \mathbf{t}_{\mathbf{z}} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \\ \mathbf{z} \\ 1 \end{bmatrix}$$

$$x' = x + t_x$$
$$y' = y + t_y$$
$$z' = z + t_z$$



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Coordinate Transformations: Scaling

• We can scale a mesh by applying the *scaling transformation* to each of its vertices:

$$T_{S} = \begin{bmatrix} s_{x} & 0 & 0 & 0 \\ 0 & s_{y} & 0 & 0 \\ 0 & 0 & s_{z} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

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Coordinate Transformations: Scaling

- When $s_x = s_y = s_z$, we call it *uniform scaling*
- Otherwise, we have *non-uniform scaling*

 Suppose someone said to you that it makes no sense to apply scaling to vertices

Coordinate Transformations: Rotation

 We can rotate a vertex about one of the major axes by some angle θ using one of the *rotation matrices*:

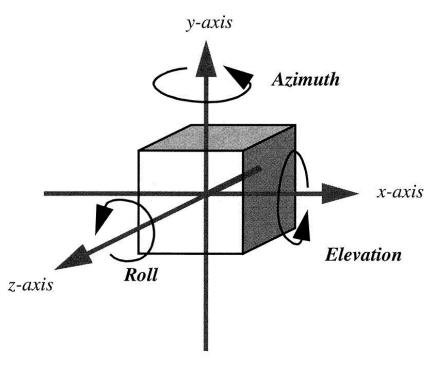
$$T_{R_{x}} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_{R_{y}} = \begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
$$T_{R_{z}} = \begin{bmatrix} \cos \theta - \sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

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Actor Geometry: Actor Location and Orientation

- The modeling transformations we looked at earlier allow us to change the location and orientation of objects
- It's often useful to associate (i.e., store) an *orientation vector* (O_x, O_y, O_z) for each actor
- This vector implicitly defines the three rotation matrices



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Coordinate Transformations

- Transformations can be *composed* by *right-multiplying* transformation matrices
- Example: a sequence (S R_z T R_y) would indicate:
 - 1. A rotation about the Y axis, followed by
 - 2. A translation, followed by
 - 3. A rotation about the Z axis, followed by
 - 4. A scaling
- So beware and remember: matrix multiplication is associative but it isn't commutative



Coordinate Transformations

- The above transformations can be applied to objects in the scene – these are referred to as the *modeling transformations*
- The camera (viewpoint) can also be transformed by the viewing transformation
- What transformation(s) might not make sense to apply to the viewpoint?
- *Projection transformation* is applied after modeling transformations to project the 3D actors onto the screen
- We won't study projection transformations in greater

 details in this course
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Camera Attributes

- *Projection* method of projection determines how 3D objects are drawn on the *image plane*, or screen
- Orthographic projection all rays of light are parallel to the projection vector
- 3D points are projected onto the screen along the same direction
- The perceived size of an object is not a function of its distance from the camera

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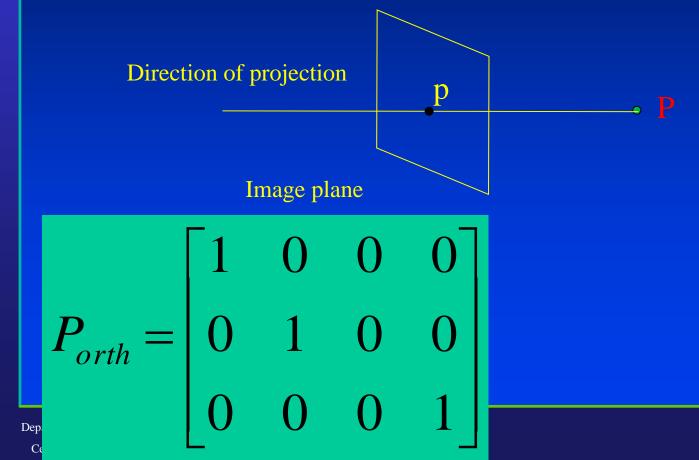


Orthographic Camera Model

Infinite Projection matrix - last row is (0,0,0,1)

Good Approximations – object is far from the camera (relative to its size)

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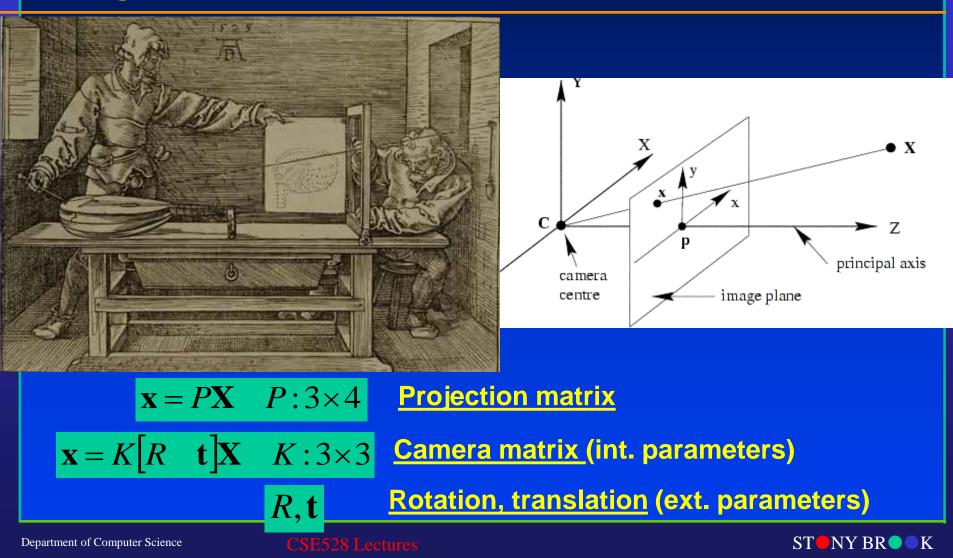
Camera Attributes

- *Perspective projection* all light rays travel through a central point, such as the viewpoint
- Objects appear smaller as their distances increase from the viewpoint, and vice versa
- This is what happens in real life
- Simulating perspective projection requires a view angle
- View angle and clipping planes define a *view frustum*, a truncated pyramid; one type of *viewing volume*
- In orthographic projection, we have a rectangular view volume instead because the light rays are parallel!!!

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Projective Camera Model



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