

Algorithms

(Algorithm Code)

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What is an algorithm code?

- An algorithm code is also called a pseudocode
- An algorithm code represents an algorithm in a structured, modular, step-by-step format
- An algorithm code is used to show the actual working logic of an algorithm without including unnecessary keywords and information contained in a program code that is not relevant to the problem-solving logic
- An algorithm code is programming-language neutral, i.e., programmers can easily understand an algorithm code irrespective of their favorite programming language

Assignments

ALGORITHMCODE()

// Assignments

$a \leftarrow 1; a \leftarrow \left(\frac{\lfloor d \rfloor + \lceil e \rceil}{\sqrt{n} + \log_3 k} + a^b \bmod c \right)$ // comma-separated statements

currentpathcost $\leftarrow 0$ // variable names have all small letters

Static arrays

ALGORITHMCODE()

```
// Static array: Creation and assignment .....  
Create an array  $A[1 \dots n]$   
 $A[i] \leftarrow a$  // set  $i$ th value of array. time:  $\Theta(1)$   
 $a \leftarrow A[i]$  // get  $i$ th value of array. time:  $\Theta(1)$   
Create an array  $B[1 \dots n] \leftarrow [0 \dots 0]$  //  $B[i] = 0$  for all  $i \in [1, n]$   
Create an array  $C[1 \dots n] \leftarrow [1 \dots n]$  //  $C[i] = i$  for all  $i \in [1, n]$   
Create an array  $D[1 \dots n] \leftarrow B[1 \dots n]$  //  $D[i] = B[i]$  for all  $i \in [1, n]$   
 $a \leftarrow \text{Sum}(A[1 \dots n]) + \text{Max}(A[1 \dots n]) + \text{Min}(A[1 \dots n])$ 
```

Dynamic arrays

ALGORITHMCODE()

```
// Dynamic array: Creation and assignment .....  
Create a dynamic array optimalsolutionslist  $\leftarrow$  [ ]  
Create a dynamic array A  $\leftarrow$  optimalsolutionslist  
A.Add(a) // add element at last. time: $\Theta(1)^*$   
A[i]  $\leftarrow$  a // set ith value of array. time: $\Theta(1)$   
a  $\leftarrow$  A[i] // get ith value of array. time: $\Theta(1)$   
a  $\leftarrow$  A.First() // return the first element. time: $\Theta(1)$   
a  $\leftarrow$  A.Last() // return the last element. time: $\Theta(1)$ 
```

2-D matrices

ALGORITHMCODE()

```
// 2-D matrix .....  
Create a 2-D matrix  $M[1 \dots m][1 \dots n]$   
 $M[i][j] \leftarrow a$  // set  $(i, j)$ th value of matrix. time:  $\Theta(1)$   
 $a \leftarrow M[i][j]$  // get  $(i, j)$ th value of matrix. time:  $\Theta(1)$ 
```

Conditionals

ALGORITHMCODE()

```
// Conditional: If-else ladder .....  
if  $a > 0$  then  
|  $b \leftarrow 5$   
else if  $a = 0$  then  
|  $b \leftarrow 0$   
|  $c \leftarrow 0$   
else  
|  $b \leftarrow -5$ 
```


Conditionals

```
ALGORITHMCODE()
```

```
// Conditional: Compact if-else ladder .....  
if  $a > 0$  then  $b \leftarrow 5$   
else if  $a = 0$  then {  $b \leftarrow 0$ ;  $c \leftarrow 0$  }  
else  $b \leftarrow -5$ 
```

Conditionals

ALGORITHMCODE()

```
// Conditional .....  
 $a \leftarrow (b = c) ? d : e$            //  $d$  if condition true,  $e$  if condition false
```

Loops

ALGORITHMCODE()

```
// Loop:  $i$  takes values  $a, a + 1, a + 2$ , so on such that  $i \leq n$  .....  
for  $i \leftarrow a$  to  $n$  do  
| print  $A[i]$   
  
// Loop:  $i$  takes values  $n, n - 1, n - 2$ , so on such that  $i \geq a$  .....  
for  $i \leftarrow n$  downto  $a$  do  
| print  $A[i]$ 
```

Loops

ALGORITHMCODE()

```
// Loop:  $i$  takes values  $a, a + k, a + 2k$ , so on such that  $i \leq n$  .....  
for  $i \leftarrow a$  to  $n$  increment  $k$  do  
| print  $A[i]$   
  
// Loop:  $i$  takes values  $n, n - k, n - 2k$ , so on such that  $i \geq a$  .....  
for  $i \leftarrow n$  downto  $a$  decrement  $k$  do  
| print  $A[i]$ 
```

Loops

ALGORITHMCODE()

```
// Loop: i takes values n, n - k, n - 2k, so on such that i ≥ a .....  
i ← n while i ≥ a do  
| i ← i - k
```

Function invocations

```
ALGORITHMCODE()
```

```
// Function invocation .....  
output  $\leftarrow$  ANOTHERALGORITHM(a,  $A[1 \dots n]$ )  
return output
```

```
ANOTHERALGORITHM(a,  $A[1 \dots n]$ )
```

```
return  $A[a]$ 
```

Singly linked lists

ALGORITHM CODE()

```
// Singly linked list (SLL) .....  
Create a SinglyLinkedList L  
a ← L.First()           // return the first element. time:  $\Theta(1)$   
a ← L.Last()           // return the last element. time:  $\Theta(1)$   
L.AddFirst(a)          // add element at first. time:  $\Theta(1)$   
L.AddLast(a)           // add element at last. time:  $\Theta(1)$   
a ← L.RemoveFirst()   // remove element at first. time:  $\Theta(1)$   
a ← L.RemoveLast()    // remove element at last. time:  $\Theta(n)$ 
```

Circularly singly linked lists

ALGORITHMCODE()

```
// Circularly singly linked list (CSLL) .....  
Create a CircularlySinglyLinkedList L  
a ← L.First()           // return the first element. time:  $\Theta(1)$   
a ← L.Last()           // return the last element. time:  $\Theta(1)$   
L.AddFirst(a)          // add element at first. time:  $\Theta(1)$   
L.AddLast(a)           // add element at last. time:  $\Theta(1)$   
a ← L.RemoveFirst()    // remove element at first. time:  $\Theta(1)$   
a ← L.RemoveLast()     // remove element at last. time:  $\Theta(n)$   
L.Rotate()             // move first element to last. time:  $\Theta(1)$ 
```


Doubly linked lists

ALGORITHMCODE()

```
// Doubly linked list (DLL) .....  
Create a DoublyLinkedList L  
a ← L.First()           // return the first element. time:Θ(1)  
a ← L.Last()            // return the last element. time:Θ(1)  
L.AddFirst(a)           // add element at first. time:Θ(1)  
L.AddLast(a)            // add element at last. time:Θ(1)  
a ← L.RemoveFirst()    // remove element at first. time:Θ(1)  
a ← L.RemoveLast()     // remove element at last. time:Θ(1)
```

Stacks

ALGORITHMCODE()

```
// Stack (implemented using dynamic array or SLL) .....  
Create a stack  $S$   
 $S.$ Push( $a$ ) // add element at top. time: $\Theta(1)$   
 $a \leftarrow S.$ Pop() // remove element at top. time: $\Theta(1)$   
 $a \leftarrow S.$ Top() // return element at top. time: $\Theta(1)$ 
```

Queues

ALGORITHMCODE()

```
// Queue (implemented using a circular dynamic array or SLL) .....  
Create a queue Q  
Q.Enqueue(a) // add element at last. time:  $\Theta(1)$   
a ← Q.Dequeue() // remove element at first. time:  $\Theta(1)$   
a ← Q.Top() // return element at top. time:  $\Theta(1)$ 
```

Dequeues

ALGORITHMCODE()

```
// Double-ended queue (deque) .....  
Create a deque  $D$   
 $D$ .AddFirst( $a$ ) // add element at first. time: $\Theta(1)$   
 $D$ .AddLast( $a$ ) // add element at last. time: $\Theta(1)$   
 $a \leftarrow D$ .RemoveFirst() // remove element at first. time: $\Theta(1)$   
 $a \leftarrow D$ .RemoveLast() // remove element at last. time: $\Theta(1)$ 
```

Balanced search trees

ALGORITHMCODE()

```
// Balanced search tree with size  $n$  .....  
Create a BalancedSearchTree  $T$   
 $T$ .Add( $a$ ) // add element. time:  $\mathcal{O}(\log n)$   
 $T$ .Remove( $a$ ) // remove element. time:  $\mathcal{O}(\log n)$   
 $a \leftarrow T$ .Search( $a$ ) // check if element exists. time:  $\mathcal{O}(\log n)$   
 $T$ .InOrderTraversal() // inorder traversal. time:  $\Theta(n)$   
 $T$ .LevelOrderTraversal() // levelorder traversal. time:  $\Theta(n)$ 
```

Hash sets

ALGORITHMCODE()

```
// Hash set (assuming perfect hash function) .....  
Create a hash set  $H$  to elements in unordered/unordered fashion  
 $H.Add(a)$  // add element. time:  $\mathcal{O}(1)^*$   
 $H.Remove(a)$  // remove element. time:  $\mathcal{O}(1)^*$   
 $a \leftarrow H.Search(a)$  // check if element exists. time:  $\mathcal{O}(1)^*$ 
```

Hash maps

ALGORITHMCODE()

```
// Hash map (assuming perfect hash function) .....  
Create a hash map  $H$  to store unordered/unordered (key, value) pairs  
 $a \leftarrow H.GetValue(k)$  // return the value for key  $k$ . time:  $\mathcal{O}(1)^*$   
 $a \leftarrow H[k]$  // return the value for key  $k$ . time:  $\mathcal{O}(1)^*$   
 $H.Add(\langle k, v \rangle)$  // add a pair. time:  $\mathcal{O}(1)^*$   
 $H[k] \leftarrow v$  // add a pair. time:  $\mathcal{O}(1)^*$   
 $\langle k, v \rangle \leftarrow H.Remove(k)$  // return the pair with key  $k$ . time:  $\mathcal{O}(1)^*$   
 $\langle k, v \rangle \leftarrow H.Search(k)$  // search for pair with key  $k$ . time:  $\mathcal{O}(1)^*$ 
```

Priority queues

ALGORITHMCODE()

```
// Minimum-heap with size  $n$  .....  
Create a min-heap  $H$  to store (key, value) pairs  
 $H.Add(\langle k, v \rangle)$  // add a pair. time:  $\mathcal{O}(\log n)$   
 $\langle k, v \rangle \leftarrow H.Min()$  // return pair with min key. time:  $\Theta(1)$   
 $\langle k, v \rangle \leftarrow H.RemoveMin()$  // remove pair with min key. time:  $\mathcal{O}(\log n)$ 
```