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Abstract Classes and Abstract Methods

Abstract classes are italicized or have the annotation `<abstract>`.

Methods `getArea` and `getPerimeter` are overridden in `Circle` and `Rectangle`. Superclass abstract methods are generally omitted in the UML diagram for subclasses.

The # sign indicates protected modifier.
public abstract class GeometricObject {
    private String color = "white";
    private boolean filled;
    private java.util.Date dateCreated;
    protected GeometricObject() {
        dateCreated = new java.util.Date();
    }
    protected GeometricObject(String color, boolean filled) {
        dateCreated = new java.util.Date();
        this.color = color;
        this.filled = filled;
    }
    public String getColor() {   return color;  }
    public void setColor(String color) {  this.color = color;  }
    public boolean isFilled() {   return filled;  }
    public void setFilled(boolean filled) {  this.filled = filled;  }
    public java.util.Date getDateCreated() {   return dateCreated;  }
    public String toString() {
        return "created on " + dateCreated + 
               "ncolor: " + color + 
               " and filled: " + filled;
    }
    /** Abstract method getArea */
    public abstract double getArea();
    /** Abstract method getPerimeter */
    public abstract double getPerimeter();
}
public class Circle extends GeometricObject {
    private double radius;
    public Circle() {
    }
    public Circle(double radius) {
        this.radius = radius;
    }
    public double getRadius() {
        return radius;
    }
    public void setRadius(double radius) {
        this.radius = radius;
    }
    public double getArea() {
        return radius * radius * Math.PI;
    }
    public double getPerimeter() {
        return 2 * radius * Math.PI;
    }
    public double getDiameter() {
        return 2 * radius;
    }
}

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public class Rectangle extends GeometricObject {
    private double width;
    private double height;
    public Rectangle() {
        // super();
    }
    public Rectangle(double width, double height) {
        this();
        this.width = width;
        this.height = height;
    }
    public Rectangle(double width, double height, String color,
            boolean filled) {
        super(color, filled);
        this.width = width;
        this.height = height;
    }
    public double getWidth() {    return width;  }
    public void setWidth(double width) {          this.width = width;  }
    public double getHeight() {    return height;  }
    public void setHeight(double height) {          this.height = height;  }
    public double getArea() {
        return width * height;
    }
    public double getPerimeter() {
        return 2 * (width + height);
    }
}
public class TestGeometricObject1 {
    public static void main(String[] args) {
        // Declare and initialize two geometric objects
        GeometricObject geoObject1 = new Circle(5);
        GeometricObject geoObject2 = new Rectangle(5, 3);
        // Display circle
        displayGeometricObject(geoObject1);
        // Display rectangle
        displayGeometricObject(geoObject2);
        System.out.println("The two objects have the same area? " +
            equalArea(geoObject1, geoObject2));
    }

    /** A method for displaying a geometric object */
    public static void displayGeometricObject(GeometricObject object) {
        System.out.println(object); // object.toString()
        System.out.println("The area is " + object.getArea());
        System.out.println("The perimeter is " + object.getPerimeter());
    }

    /** A method for comparing the areas of two geometric objects */
    public static boolean equalArea(GeometricObject object1,
        GeometricObject object2) {
        return object1.getArea() == object2.getArea();
    }
}
abstract methods in abstract classes

- An abstract method can only be contained in an abstract class.
subclasses of abstract classes

- In a nonabstract (a.k.a., concrete) subclass extended from an abstract super-class, all the abstract methods MUST be implemented.

```java
abstract class A {
    abstract void m();
}

class B extends A {
    void m() {
    }
}
```
**subclasses of abstract classes**

- In an abstract subclass extended from an abstract super-class, we can choose:
  - to implement the inherited abstract methods OR
  - to postpone the constraint to implement the abstract methods to its nonabstract subclasses.
abstract class A {
    abstract void m();
}

abstract class B extends A {
    void m() {
    }
}

class C extends B {
}

(c) Pearson Education, Inc. & Paul Fodor (CS Stony Brook)
abstract class A{
    abstract void m();
}

abstract class B extends A{
}

public class C extends B {
    void m() {
    }
}

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abstract classes

• A subclass can be abstract even if its superclass is concrete.

• For example, the `Object` class is concrete, but a subclass, `GeometricObject`, is abstract.
abstract classes

• A subclass can override a method from its concrete superclass to define it **abstract**

• useful when we want to **force** its subclasses to implement that method, or

• the implementation of the method in the superclass is invalid in the subclass
abstract classes

• It is possible to define an abstract class that contains no abstract methods.
• This class is used as a base class for defining new subclasses.
abstract classes

• An object **cannot** be created from abstract class:
  • An abstract class cannot be instantiated using the `new` operator:

```
GeometricObject o = new GeometricObject();
```

• We still define its constructors, which are invoked in the constructors of its subclasses through **constructor chaining**.
  • For instance, the constructors of `GeometricObject` are invoked by the constructors in the `Circle` and the `Rectangle` classes.
abstract classes as types

- An abstract class can be used as a data type:
  \begin{verbatim}
  GeometricObject c = new Circle(2);
  \end{verbatim}

- We can create an array whose elements are of GeometricObject type:
  \begin{verbatim}
  GeometricObject[] geo = new GeometricObject[10];
  \end{verbatim}

- There are only null elements in the array until they are initialized with concrete objects:
  \begin{verbatim}
  geo[0] = new Circle();
  geo[1] = new Rectangle();
  \end{verbatim}
The abstract Calendar class and its GregorianCalendar subclass

• An instance of `java.util.Date` represents a specific instant in time with millisecond precision

• `java.util.Calendar` is an abstract base class for extracting detailed information such as `year`, `month`, `date`, `hour`, `minute` and `second` from a `Date` object for a specific calendar.

  • Subclasses of `Calendar` can implement specific calendar systems such as Gregorian calendar, Lunar Calendar and Jewish calendar.

    • `java.util.GregorianCalendar` is for the modern Gregorian calendar.
The GregorianCalendar Class

- Java API for the **GregorianCalendar** class:
  
  [http://docs.oracle.com/javase/8/docs/api/java/util/GregorianCalendar.html](http://docs.oracle.com/javase/8/docs/api/java/util/GregorianCalendar.html)

- `new GregorianCalendar()` constructs a default `GregorianCalendar` with the current time

- `new GregorianCalendar(year, month, date)` constructs a `GregorianCalendar` with the specified `year`, `month`, and `date`

  - The `month` parameter is 0-based, i.e., 0 is for January, 1 is for February, ..., 11 is for December.
The abstract Calendar class and its GregorianCalendar subclass

```java
java.util.GregorianCalendar
+GregorianCalendar()
+GregorianCalendar(year: int, month: int, dayOfMonth: int)
+GregorianCalendar(year: int, month: int, dayOfMonth: int, hour:int, minute: int, second: int)
```

Constructs a default calendar.

Constructs a GregorianCalendar for the current time.

Constructs a GregorianCalendar for the specified year, month, and day of month.

Constructs a GregorianCalendar for the specified year, month, day of month, hour, minute, and second. The month parameter is 0-based, that is, 0 is for January.

Returns the value of the given calendar field.

Returns the maximum value that the specified calendar field could have.

Sets the given calendar to the specified value.

Sets the calendar with the specified year, month, and date. The month parameter is 0-based, that is, 0 is for January.

Adds or subtracts the specified amount of time to the given calendar field.

Returns a Date object representing this calendar’s time value (million second offset from the Unix epoch).

Sets this calendar’s time with the given Date object.
The get Method in the Calendar Class

- The get(int field) method defined in the Calendar class is useful to extract the date and time information from a Calendar object.
- The fields are defined as constants in Calendar, as shown in the following:

<table>
<thead>
<tr>
<th>Constant</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>YEAR</td>
<td>The year of the calendar.</td>
</tr>
<tr>
<td>MONTH</td>
<td>The month of the calendar with 0 for January.</td>
</tr>
<tr>
<td>DATE</td>
<td>The day of the calendar.</td>
</tr>
<tr>
<td>HOUR</td>
<td>The hour of the calendar (12-hour notation).</td>
</tr>
<tr>
<td>HOUR_OF_DAY</td>
<td>The hour of the calendar (24-hour notation).</td>
</tr>
<tr>
<td>MINUTE</td>
<td>The minute of the calendar.</td>
</tr>
<tr>
<td>SECOND</td>
<td>The second of the calendar.</td>
</tr>
<tr>
<td>DAY_OF_WEEK</td>
<td>The day number within the week with 1 for Sunday.</td>
</tr>
<tr>
<td>DAY_OF_MONTH</td>
<td>Same as DATE.</td>
</tr>
<tr>
<td>DAY_OF_YEAR</td>
<td>The day number in the year with 1 for the first day of the year.</td>
</tr>
<tr>
<td>WEEK_OF_MONTH</td>
<td>The week number within the month.</td>
</tr>
<tr>
<td>WEEK_OF_YEAR</td>
<td>The week number within the year.</td>
</tr>
<tr>
<td>AM_PM</td>
<td>Indicator for AM or PM (0 for AM and 1 for PM).</td>
</tr>
</tbody>
</table>

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import java.util;

public class TestCalendar {
    public static void main(String[] args) {
        // Construct a Gregorian calendar for the current date and time

        Calendar calendar = new GregorianCalendar();
        System.out.println("Current time is " + new Date());
        System.out.println("YEAR: 	" + calendar.get(Calendar.YEAR));
        System.out.println("MONTH: 	" + calendar.get(Calendar.MONTH));
        System.out.println("DATE: 	" + calendar.get(Calendar.DATE));
        System.out.println("HOUR: 	" + calendar.get(Calendar.HOUR));
        System.out.println("HOUR_OF_DAY: 	" + calendar.get(Calendar.HOUR_OF_DAY));
        System.out.println("MINUTE: 	" + calendar.get(Calendar.MINUTE));
        System.out.println("SECOND: 	" + calendar.get(Calendar.SECOND));
        System.out.println("DAY_OF_WEEK: 	" + calendar.get(Calendar.DAY_OF_WEEK));
        System.out.println("DAY_OF_MONTH: 	" + calendar.get(Calendar.DAY_OF_MONTH));
        System.out.println("DAY_OF_YEAR: " + calendar.get(Calendar.DAY_OF_YEAR));
        System.out.println("WEEK_OF_MONTH: " + calendar.get(Calendar.WEEK_OF_MONTH));
        System.out.println("WEEK_OF_YEAR: " + calendar.get(Calendar.WEEK_OF_YEAR));
        System.out.println("AM_PM: " + calendar.get(Calendar.AM_PM));
        // Construct a calendar for January 1, 2020
        Calendar calendar1 = new GregorianCalendar(2020, 0, 1);
        System.out.println("January 1, 2020 is a " +
                          dayNameOfWeek(calendar1.get(Calendar.DAY_OF_WEEK)));
    }

    public static String dayNameOfWeek(int dayOfWeek) {
        switch (dayOfWeek) {
            case 1: return "Sunday";
            case 2: return "Monday";
            case 3: return "Tuesday";
            ... case 7: return "Saturday";
            default: return null;
        }
    }
}
Interfaces

• An *interface* is a class-like construct that contains only abstract methods and constants.

• Why is an interface useful?
  • An interface is similar to an abstract class, but the intent of an interface is to **specify behavior** for objects.
    • For example: specify that the objects are *comparable*, *edible*, *cloneable*, …
  • Allows multiple inheritance: a class can implement multiple interfaces.
Define an Interface

• Declaration:

```java
class InterfaceName {
    // constant declarations;
    // method signatures;
}
```
Interface Example

- The **Edible** interface specifies whether an object is edible:

```java
public interface Edible {
    public abstract String howToEat();
}
```

- The class **Chicken** implements the **Edible** interface:

```java
class Chicken extends Animal implements Edible {
    public String howToEat() {
        return "Chicken: Fry it";
    }
}
```
interface Edible {
    public abstract String howToEat(); /** Describe how to eat */
}

abstract class Animal {
}
class Chicken extends Animal implements Edible {
    public String howToEat() {
        return "Chicken: Fry it";
    }
}

class Tiger extends Animal {
} /** Does not extend Edible */

abstract class Fruit implements Edible {
}
class Apple extends Fruit {
    public String howToEat() {
        return "Apple: Make apple cider";
    }
}

class Orange extends Fruit {
    public String howToEat() {
        return "Orange: Make orange juice";
    }
}

public class TestEdible {
    public static void main(String[] args) {
        Object[] objects = {new Tiger(), new Chicken(), new Apple()};
        for (Object o:objects)
            if (o instanceof Edible)
                System.out.println(((Edible)o).howToEat());
    }
}
Omitting Modifiers in Interfaces

• In an interface:
  • All data fields are **public static final**
  • All methods are **public abstract**
  • These modifiers can be omitted:

    ```java
    public interface T1 {
        public static final int K = 1;
        public abstract void p();
    }
    ```
    Equivalent
    ```java
    public interface T1 {
        int K = 1;
        void p();
    }
    ```

• A constant defined in an interface can be accessed using `InterfaceName.CONSTANT_NAME`, for example: `T1.K`
Interfaces

• An interface is treated like a special class in Java:
  • Each interface is compiled into a separate bytecode (.class) file just like a regular class.
  • Like an abstract class, you cannot create an instance from an interface using the `new` operator

• Uses of interfaces are like for abstract classes:
  • as a data type for a variable
  • as the result of casting
The Comparable Interface

- The **Comparable** interface is defined in the `java.lang` package and it is used by `Arrays.sort`

```java
package java.lang;
public interface Comparable {
    int compareTo(Object o);
}
```
Many classes in the Java library implement `Comparable` (e.g., `String` and `Date`) to define a natural order for the objects:

```java
public class String extends Object implements Comparable {
    // class body omitted
}

public class Date extends Object implements Comparable {
    // class body omitted
}
```

- `new String().instanceof String` true
- `new String().instanceof Comparable` true
- `new java.util.Date().instanceof java.util.Date` true
- `new java.util.Date().instanceof Comparable` true
In UML, the interface and the methods are italicized
dashed lines and triangles are used to point to the interface
Writing a generic `max` Method

The `return` value from the `max` method is of the `Comparable` type. So, we need to cast it to `String` or `Date` explicitly.
Defining Classes to Implement Comparable

- We cannot use the `max` method to find the larger of two instances of `Rectangle`, because `Rectangle` does not implement `Comparable`.
- We can define a new rectangle class `ComparableRectangle` that implements `Comparable`: the instances of this new class are comparable.

```
GeometricObject

Rectangle

ComparableRectangle

«interface»
java.lang.Comparable

+compareTo(o: Object): int
```
public class ComparableRectangle extends Rectangle {
    /** Construct a ComparableRectangle with specified properties */
    public ComparableRectangle(double width, double height) {
        super(width, height);
    }

    /** Implement the compareTo method defined in Comparable */
    public int compareTo(Object o) {
        if (getArea() > ((ComparableRectangle)o).getArea())
            return 1;
        else if (getArea() < ((ComparableRectangle)o).getArea())
            return -1;
        else
            return 0;
    }

    public static void main(String[] args) {
        ComparableRectangle rectangle1 = new ComparableRectangle(4, 5);
        ComparableRectangle rectangle2 = new ComparableRectangle(3, 6);
        System.out.println(Max.max(rectangle1, rectangle2));
    }
}
Sorting an Array of Objects

- Java provides a static sort method for sorting an array of Object in the java.util.Arrays class that uses the Comparable interface:
  
  ```java
  java.util.Arrays.sort(intArray);
  ```
public class GenericSort {
    public static void main(String[] args) {
        Integer[] intArray=new Integer[]{2,4,3};
        sort(intArray); // or Arrays.sort(intArray);
        printList(intArray);
    }
    public static void sort(Object[] list) {
        Object currentMax;
        int currentMaxIndex;
        for (int i = list.length - 1; i >= 1; i--){
            currentMax = list[i];
            currentMaxIndex = i; // Find the maximum in the list[0..i]
            for (int j = i - 1; j >= 0; j--){
                if (((Comparable)currentMax).compareTo(list[j]) < 0) {
                    currentMax = list[j];
                    currentMaxIndex = j;
                }
            }
            list[currentMaxIndex] = list[i];
            list[i] = currentMax;
        }
    }
    public static void printList(Object[] list) {
        for (int i=0;i<list.length;i++) System.out.print(list[i]+" ");
    }
}

The objects are instances of the Comparable interface and they are compared using the compareTo method.
The Cloneable Interface

- Marker Interface: is an empty interface (does not contain constants or methods), but it is used to denote that a class possesses certain desirable properties to the compiler and the JVM.

```java
package java.lang;
public interface Cloneable {
}
```
- A class that implements the Cloneable interface is marked cloneable:
  - its objects can be cloned using the clone() method defined in the Object class, and we can override this method in our classes
The Cloneable Interface

- **Calendar** (in the Java library) implements **Cloneable**:

  Calendar calendar = new GregorianCalendar(2022, 1, 1);
  Calendar calendarCopy = (Calendar)(calendar.clone());
  System.out.println("calendar == calendarCopy is "+(calendar == calendarCopy));

  Displays:

  ```java
calendar == calendarCopy is false
```

  because the references are different

  ```java
System.out.println("calendar.equals(calendarCopy) is"+
calendar.equals(calendarCopy));
```

  ```java
calendar.equals(calendarCopy) is true
```

  because the **calendarCopy** is a copy of **calendar**
Implementing the **Cloneable** Interface

- If we try to create a clone of an object instance of a class that does not implement the **Cloneable** interface, it throws **CloneNotSupportedException**
- The **clone()** method in the **Object** class creates a new instance of the class of this object and initializes all its fields with exactly the contents of the corresponding fields of this object, as if by assignment (using a technique named **reflection**); the contents of the reference data fields are not cloned.
  - The **clone()** method returns an **Object** that needs to be casted
- We can override the **clone()** method from the **Object** class to create custom clones
public class SomethingCloneable implements Cloneable {
    public boolean equals(Object o) {
        return true;
    }

    public static void main(String[] args) throws CloneNotSupportedException {
        SomethingCloneable s1 = new SomethingCloneable();
        SomethingCloneable s2 = (SomethingCloneable) s1.clone();
        System.out.println("s1 == s2 is " + (s1 == s2));
        // false
        System.out.println("s1.equals(s2) is " + s1.equals(s2));
        // true
    }
}
public class House implements Cloneable, Comparable {
    private int id;
    private double area;
    private java.util.Date whenBuilt;
    public House(int id, double area) {this.id = id; this.area = area;
        whenBuilt = new java.util.Date();}
    public double getId() { return id;}
    public double getArea() { return area;}
    public java.util.Date getWhenBuilt() { return whenBuilt;}
    /** Override the protected clone method defined in the Object class, and strengthen its accessibility */
    public Object clone() {
        try {
            return super.clone();
        } catch (CloneNotSupportedException ex) {
            return null;
        }
    }
    /** Implement the compareTo method defined in Comparable */
    public int compareTo(Object o) {
        if (area > ((House)o).area)
            return 1;
        else if (area < ((House)o).area)
            return -1;
        else
            return 0;
    }
}
Shallow vs. Deep Copy

House house1 = new House(1, 1750.50);
House house2 = (House)(house1.clone());

shallow copy: if the field is of reference type, the object’s reference is copied rather than its content
For *deep copying*, we can override the clone method with custom object creation:

```java
public class House implements Cloneable {
    ...
    public Object clone() { // deep copy
        try {
            House h = (House)(super.clone());
            h.whenBuilt = (Date)(whenBuilt.clone());
            return h;
        } catch (CloneNotSupportedException ex) {
            return null;
        }
    }
    ...
}
```
For *deep copying*, we can override the clone method with custom object creation:

```java
public class House implements Cloneable {
    
    public Object clone() { // deep copy
        Date whenBuilt2 = (Date)(whenBuilt.clone());
        House h = new House(id, area, whenBuilt2);
        return h;
    }

    
    
}
```
Interfaces vs. Abstract Classes

- In an interface, the data fields must be constants; an abstract class can have variable data fields.
- Interfaces don't have constructors; all abstract classes have constructors.
- Each method in an interface has only a signature without implementation (i.e., only abstract methods); an abstract class can have concrete methods.

<table>
<thead>
<tr>
<th></th>
<th>Variables</th>
<th>Constructors</th>
<th>Methods</th>
</tr>
</thead>
<tbody>
<tr>
<td>Interfaces</td>
<td>All variables must be public static final</td>
<td>No constructors. An interface cannot be instantiated using the new operator.</td>
<td>All methods must be public abstract methods</td>
</tr>
<tr>
<td>Abstract classes</td>
<td>No restrictions</td>
<td>Constructors are invoked by subclasses through constructor chaining. An abstract class cannot be instantiated using the new operator.</td>
<td>No restrictions.</td>
</tr>
</tbody>
</table>
Inheritance: Interfaces & Classes

- An interface can extend any number of other interfaces
- There is no root for interfaces
- A class can implement any number of interfaces

![Diagram showing inheritance relationships between classes and interfaces]
Conflicting interfaces

- Errors detected by the compiler:
  - If a class implements two interfaces with conflicting information, like:
    - two same constants with different values, or
    - two methods with same signature but different return type
Whether to use a class or an interface?

- **Strong is-a**: a relationship that clearly describes a parent-child relationship
  - For example: a student is a person
  - Should be modeled using class inheritance
- **Weak is-a (or is-kind-of)**: indicates that an object possesses a certain property
  - For example: all strings are comparable, all dates are comparable
  - Should be modeled using interfaces
- You can also use interfaces to circumvent single inheritance restriction if multiple inheritance is desired
Wrapper Classes

- Primitive data types in Java ➔ Better performance
- However, data structures (ArrayList) expect objects as elements
- Each primitive type has a wrapper class: Boolean, Character, Short, Byte, Integer, Long, Float, Double

```
java.lang.Object
- Double
- Float
- Long
- Integer
- Short
- Byte
- java.lang.Comparable
- java.lang.Object
```

- The wrapper classes do not have no-arg constructors
- The instances of all wrapper classes are immutable: their internal values cannot be changed once the objects are created
Wrapper Classes

• Each wrapper class overrides the `toString` and `equals` methods defined in the `Object` class.
• Since these classes implement the `Comparable` interface, the `compareTo` method is also implemented in these classes.
The **Number** Class

- Each numeric wrapper class extends the abstract `Number` class:
  - The abstract **`Number`** class contains the methods `doubleValue`, `floatValue`, `intValue`, `longValue`, `shortValue`, and `byteValue` to "convert" objects into primitive type values
  - The methods `doubleValue`, `floatValue`, `intValue`, `longValue` are **abstract**
    - The methods `byteValue` and `shortValue` are not **abstract**, which simply return `(byte)intValue()` and `(short)intValue()`, respectively
  - Each numeric wrapper class implements the abstract methods `doubleValue`, `floatValue`, `intValue` and `longValue`
The **Integer** and **Double** Classes

### `java.lang.Number`
- `byteValue()`: byte
- `shortValue()`: short
- `intValue()`: int
- `longValue()`: long
- `floatValue()`: float
- `doubleValue()`: double

### `java.lang.Integer`
- `-value`: int
- `+MAX_VALUE`: int
- `+MIN_VALUE`: int
- `+Integer(value: int)`
- `+Integer(s: String)`
- `valueOf(s: String): Integer`
- `valueOf(s: String, radix: int): Integer`
- `parseInt(s: String): int`
- `parseInt(s: String, radix: int): int`

### `java.lang.Comparable`
- `compareTo(o: Object): int`

### `java.lang.Double`
- `-value`: double
- `+MAX_VALUE`: double
- `+MIN_VALUE`: double
- `+Double(value: double)`
- `+Double(s: String)`
- `valueOf(s: String): Double`
- `valueOf(s: String, radix: int): Double`
- `parseDouble(s: String): double`
- `parseDouble(s: String, radix: int): double`
Wrapper Classes

• You can construct a wrapper object either from a primitive data type value or from a string representing the numeric value

• The constructors for `Integer` and `Double` are:

```java
public Integer(int value)
public Integer(String s)
public Double(double value)
public Double(String s)
```
Numeric Wrapper Class Constants

- Each numerical wrapper class has the constants `MAX_VALUE` and `MIN_VALUE`:
  - `MAX_VALUE` represents the maximum value of the corresponding primitive data type
  - For `Float` and `Double`, `MIN_VALUE` represents the minimum positive float and double values
    - The maximum integer: 2,147,483,647
    - The minimum positive float: 1.4E-45
    - The maximum double floating-point number: 1.79769313486231570e+308d
The `static` `valueOf` methods

- The numeric wrapper classes have a `static` method `valueOf(String s)` to create a new object initialized to the value represented by the specified string:

  ```java
  Double doubleObject = Double.valueOf("12.4");
  Integer integerObject = Integer.valueOf("12");
  ```

- Each numeric wrapper class has overloaded parsing methods to parse a numeric string into an appropriate numeric value:

  ```java
  double d = Double.parseDouble("12.4");
  int i = Integer.parseInt("12");
  ```
Wrapper Classes

• Automatic Conversion Between Primitive Types and Wrapper Class Types:
  • Since JDK 1.5, Java allows primitive type and wrapper classes to be converted automatically:
    • **boxing** of primitive types into wrapper types when objects are needed
      
      ```
      Integer[] intArray = {new Integer(2), new Integer(4), new Integer(3)};
      Equivalent
      Integer[] intArray = {new Integer(2), new Integer(4), new Integer(3)};
      ```

    • **unboxing** of wrapper types into primitive types when primitive types are needed
      ```
      int n = intArray[0] + intArray[1] + intArray[2];
      ```

      Unboxing
Arrays are objects

- Arrays are objects:
  
  - An array is an instance of the `Object` class
    
    ```java
    new int[10] instanceof Object true
    ```
  
  - If `A` is a subclass of `B`, every instance of `A[]` is an instance of `B[]`
    
    ```java
    new GregorianCalendar[10] instanceof Calendar[] true
    new Calendar[10] instanceof Object[] true
    new Calendar[10] instanceof Object true
    ```
  
  - Although an `int` value can be assigned to a `double` type variable, `int[]` and `double[]` are two incompatible types because they are not classes:
    
    - We cannot assign an `int[]` array to a variable of `double[]` array: compiler error: `double[] a = new int[10];`
BigInteger and BigDecimal

- **BigInteger** and **BigDecimal** classes in the `java.math` package:
  - For computing with very large integers or high precision floating-point values
    - **BigInteger** can represent an integer of any size
    - **BigDecimal** has no limit for the precision (as long as it’s finite=terminates)
  - Both are immutable
  - Both extend the **Number** class and implement the **Comparable** interface.
BigInteger and BigDecimal

BigInteger a = new BigInteger("9223372036854775807");
BigInteger b = new BigInteger("2");
BigInteger c = a.multiply(b); // 9223372036854775807 * 2
System.out.println(c);

18446744073709551614

BigDecimal a = new BigDecimal(1.0);
BigDecimal b = new BigDecimal(3);
BigDecimal c = a.divide(b, 20, BigDecimal.ROUND_UP);
System.out.println(c);

0.33333333333333333334
import java.math.*;

public class LargeFactorial {
    public static void main(String[] args) {
        System.out.println("50! is \n" + factorial(50));
    }

    public static BigInteger factorial(long n) {
        BigInteger result = BigInteger.ONE;
        for (int i = 1; i <= n; i++)
            result = result.multiply(new BigInteger(i + ""));
        return result;
    }
}

30414093201713378043612608166064768844377641
568960512000000000000
Case Study: The **Rational Class**

```
java.lang.Number
+byteValue(): byte
+shortValue(): short
+intValue(): int
+longValue(): long
+floatValue(): float
+doubleValue(): double

java.lang.Comparable
compareTo(Object): int
```

```
Rational

-numberator: long
-denominator: long

+Rational()
+Rational(numerator: long, denominator: long)
+getNumerator(): long
+getDenominator(): long
+add(secondRational: Rational): Rational
+multiply(secondRational: Rational): Rational
+subtract(secondRational: Rational): Rational
+divide(secondRational: Rational): Rational
+toString(): String
-gcd(n: long, d: long): long
```

add, subtract, multiply, divide
public class Rational extends Number implements Comparable {
    private long numerator = 0;
    private long denominator = 1;
    public Rational() { this(0, 1); }
    public Rational(long numerator, long denominator) {
        long gcd = gcd(numerator, denominator);
        this.numerator = ((denominator > 0) ? 1 : -1) * numerator / gcd;
        this.denominator = Math.abs(denominator) / gcd;
    }
    private static long gcd(long n, long d) {
        long n1 = Math.abs(n);
        long n2 = Math.abs(d);
        int gcd = 1;
        for (int k = 1; k <= n1 && k <= n2; k++) {
            if (n1 % k == 0 && n2 % k == 0)
                gcd = k;
        }
        return gcd;
    }
    public Rational add(Rational secondRational) {
        long n = numerator * secondRational.getDenominator() +
                  denominator * secondRational.getNumerator();
        long d = denominator * secondRational.getDenominator();
        return new Rational(n, d);
    }
}
public Rational subtract(Rational secondRational) {
    ...                       // or implement inverse and use add method
    \( \frac{a}{b} - \frac{c}{d} = \frac{ad - bc}{bd} \)
    \( -\frac{a}{b} = \frac{-a}{b} \)
} // multiply, divide

/** Override the abstract intValue method in java.lang.Number */
public int intValue() {   return (int)doubleValue();  }
public double doubleValue() {
    return ((double)numerator)/denominator;
}
// ... Override all the abstract *Value methods in java.lang.Number

/** Override the compareTo method in java.lang.Comparable */
public int compareTo(Object o) {
    if (((this.subtract((Rational)o)).getNumerator() > 0) return 1;
    else if (((this.subtract((Rational)o)).getNumerator()<0) return -1;
    else return 0;
}
public static void main(String[] args) {
    Rational r1 = new Rational(4, 2);
    Rational r2 = new Rational(2, 3);
    System.out.println(r1 + " + " + r2 + " = " + r1.add(r2));
}