

## Lecture 1: Introduction

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## 1 Introduction

Cryptography has many applications in modern day life. Almost every online service uses cryptography in some form. Some examples include

- Online banking
- E-commerce
- E-mail
- https browsing

The basic idea of cryptography is to have a mechanism of making secret communication between two parties such that an eavesdropper cannot understand the message being transferred even if he can read the text.

**Definition 1** *Cipher* : A cipher is defined by its 3 components.  $E(k,m) \rightarrow c$  and  $m \leftarrow D(c,k)$  are encryption and decryption algorithms, and  $k$  is the secret key.  $E$  can be randomized such that  $c$  changes every time

**Definition 2** *Symmetric Cipher*: If  $k$  is same for  $E$  and  $D$ , it is called a Symmetric Cipher

## 2 Historical Ciphers

### 2.1 Caesar Cipher

It was used by Julius Caesar to communicate with his generals and is thus named after him

- Encryption:  
The key( $k$ ) is a number between 1 to 25. The encrypted text is obtained by shifting each alphabet by 'k'
- Breaking the cypher:
  - Brute Force: Since the key space is just 25, each key can be tried to de-cypher the text.
  - Visible patterns and letter frequencies: Frequency of characters do not change in this cypher, they just shift by  $k$  letters. So a simple frequency analysis will break this cypher

## 2.2 Substitution Cipher

In Substitution Cipher random permutation of alphabets are chosen as following {A → T ,B → J, C → Z,....} (No repeating)

- Encryption:  
Plain text letters are mapped according to the substitution (key)
- Decryption:  
Decrypt using the same keys.
- Cannot break by brute forcing for the key since possible number of keys is 26! which is approximately  $2^{88}$
- Can be broken by frequency analysis.

## 2.3 Frequency Analysis

Following are frequencies of letters,bigrams and double letters in English:

Letters								
e	t	a	o	i	n	s	r	h
12.49%	9.28%	8.04%	7.64%	7.57%	7.23%	6.51%	6.28%	5.05%

  

Bigrams											
th	he	in	er	an	re	on	at	en	nd	ti	es
3.58%	3.08%	2.43%	2.05%	1.99%	1.85%	1.76%	1.49%	1.45%	1.35%	1.34%	1.34%

  

Double Letters										
ll	ss	ee	oo	tt	ff	pp	rr	mm	cc	nn
0.58%	0.41%	0.38%	0.21%	0.17%	0.15%	0.14%	0.12%	0.10%	0.08%	0.07%

How to break substitution cipher ?

- Collect a long ciphertext because frequency patterns will not change.
- Compute frequencies of various letters.
- Reconstruct the key using frequencies like the most frequent letter is "E" and the second most frequent letter is "T" and so on. Even bigrams and trigrams can be used.

## 2.4 Vignere Cipher

In Vignere Cipher a random keyword is used to shift the letters.If the length of keyword is less than ciphertext repeat the process.

- let keyword be "CAB"

- Alphabets A-Z are mapped from 0 to 25
- shift using word "CAB" = 201
- For example lets take message "HELLO" key will be "CABCA" so it will be encrypted as H → J, E → E, L → M, L → N, O → O as "JEMNO"
- Even Vigenere Cipher can be broken by frequency analysis by guessing key length and analyzing frequencies.

## 2.5 Rotor Machines

Encryption based on rotor machines.

Following is a Hebern rotor.



- Rotor encodes the key
- Typed symbol is encrypted with the next symbol on the rotor
- As a letter is typed rotor moves changing the key each time.
- A Cycle is measured after which the key starts repeating
- Then came machines with more rotors, more rotors means bigger the key space.  
Following is Enigma rotor machine



- More rotors means more keys approximately  $2^{36}$  in Enigma with 3 rotors.
- But these are susceptible to known cryptanalysis methods.
- Friedman had several important cryptanalysis methods for Hebern.
- Even improved and highly optimized by others.
- Turing designed a machine to search for Enigma key from known ciphertexts/plaintext pairs.

## 2.6 Digital Age

- In 1974 Data Encryption Standard (DES) was designed by IBM in response to governments call for a good encryption standard
- DES has roughly 256 keys and is not considered safe with todays computing powers.
- Advanced Encryption Standard (AES):
  - AES is designed by Vincent Rijmen and Joan Daemen in 1998 and is originally called Rijndael.
  - Selected and standardized by the US government through intense competition.

- AES comes with different key sizes and other parameters (typical for such ciphers)
- There are many other ciphers today, for example Salsa, Twofish etc.,

## 2.7 As of today

- Even as of today design of such symmetric ciphers is an ongoing process.
- Ciphers like AES are not yet broken officially.
- Weaknesses created by replacing parameters with new parameters or using new ciphers are discovered.
- These ciphers are quite fast and practical to use. So practical applications will always rely on them as the main method. A different approach to designing ciphers will be:
  - Taking the cryptanalysis out of the equation altogether and proving the cipher is hard to break.
  - Although it is possible and practical, slow speed is its main drawback and might not be as fast as say AES.

## 2.8 Beyond Secret Communication

- In future classes study of encryption schemes that allow secret communication will be discussed in detail.
- Cryptography can do a lot more than secure communication. For example
  - Digital Signatures :  
A digital signature is a mathematical scheme for demonstrating the authenticity of digital messages or documents. A valid digital signature gives a recipient reason to believe that the message was created by a known sender (authentication), that the sender cannot deny having sent the message (non-repudiation), and that the message was not altered in transit (integrity).
  - Digital Cash:  
Digital cash mimics the functionality of paper cash. More technically, digital cash is a payment message bearing a digital signature which functions as a medium of exchange or store of value.
  - Electronic voting :  
An electronic voting system works as follows: before voting, a voter must first communicate with a registration authority, who provides the voter with a token. This token is used to vote: it is given to the party in charge of tabulation.
  - Zero Knowledge Proofs:  
A zero-knowledge proof or zero-knowledge protocol is a method by which one party (the prover) can prove to another party (the verifier) that a given statement is true, without conveying any information apart from the fact that the statement is indeed true.

– Secure multiparty computation:

Secure multi-party computation is also known as secure computation, multi party computation/MPC, or privacy-preserving computation with the goal of creating methods for parties to jointly compute a function over their inputs while keeping those inputs private.

Always use Provable security approach and strive for constructions that are mathematically proven hard to break.

## 2.9 Cryptography as a rigorous science

- Functionality: Understanding what needs to be done.
- Threat Model: Who and what are we protecting from and propose a construction
- Proving that breaking the construction is either impossible, or at least as hard as solving some known "hard problem".

## 2.10 Useful Resources

<http://norvig.com/mayzner.htm>