OLAP and Data Mining

Chapter 17

OLTP Compared With OLAP

• On Line Transaction Processing – OLTP

- Maintains a database that is an accurate model of some realworld enterprise. Supports day-to-day operations. Characteristics:
 - Short simple transactions
 - Relatively frequent updates
 - Transactions access only a small fraction of the database
- On Line Analytic Processing OLAP
 - Uses information in database to guide strategic decisions. Characteristics:
 - Complex queries
 - Infrequent updates
 - Transactions access a large fraction of the database
 - Data need not be up-to-date

The Internet Grocer

• OLTP-style transaction:

 John Smith, from Schenectady, N.Y., just bought a box of tomatoes; charge his account; deliver the tomatoes from our Schenectady warehouse; decrease our inventory of tomatoes from that warehouse

- OLAP-style transaction:
 - How many cases of tomatoes were sold in all northeast warehouses in the years 2000 and 2001?

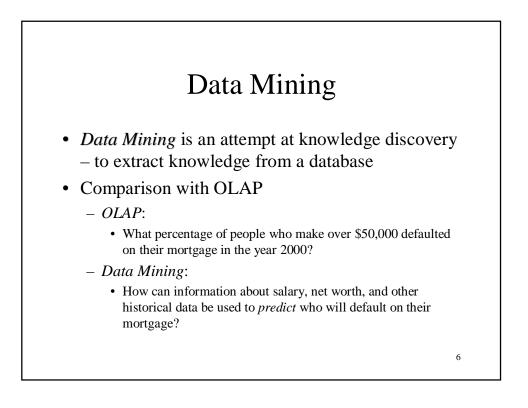
OLAP: Traditional Compared with Newer Applications

- Traditional OLAP queries
 - Uses data the enterprise gathers in its usual activities, perhaps in its OLTP system
 - Queries are ad hoc, perhaps designed and carried out by non-professionals (managers)
- Newer Applications (e.g., Internet companies)
 - Enterprise actively gathers data it wants, perhaps purchasing it
 - Queries are sophisticated, designed by professionals, and used in more sophisticated ways

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The Internet Grocer

- Traditional
 - How many cases of tomatoes were sold in all northeast warehouses in the years 2000 and 2001?
- Newer
 - Prepare a profile of the grocery purchases of John Smith for the years 2000 and 2001 (so that we can customize our marketing to him and get more of his business)



Data Warehouses

- OLAP and data mining databases are frequently stored on special servers called *data warehouses*:
 - Can accommodate the huge amount of data generated by OLTP systems
 - Allow OLAP queries and data mining to be run offline so as not to impact the performance of OLTP

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OLAP, Data Mining, and Analysis

- The "A" in OLAP stands for "Analytical"
- Many OLAP and Data Mining applications involve sophisticated analysis methods from the fields of mathematics, statistical analysis, and artificial intelligence
- Our main interest is in the database aspects of these fields, not the sophisticated analysis techniques

Fact Tables

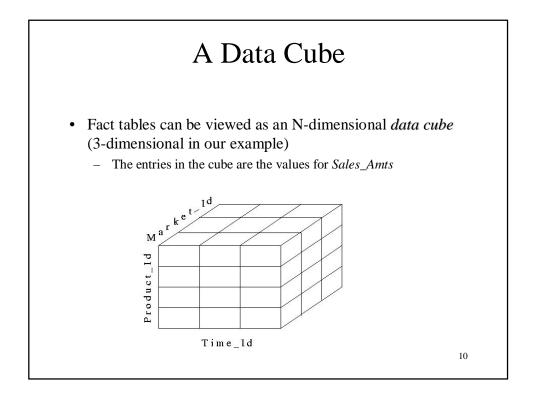
- Many OLAP applications are based on a *fact table*
- For example, a supermarket application might be based on a table

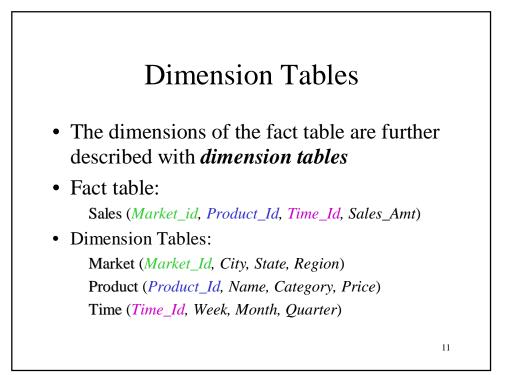
Sales (Market_Id, Product_Id, Time_Id, Sales_Amt)

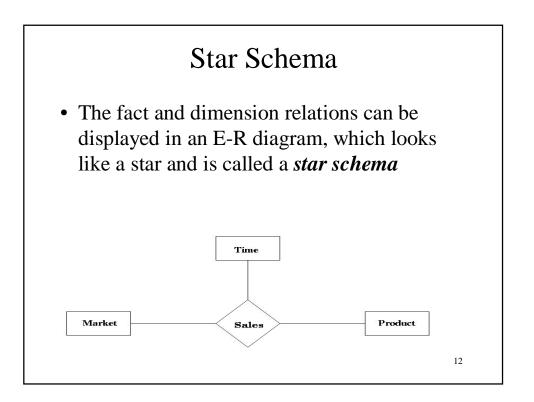
- The table can be viewed as *multidimensional*
 - Market_Id, Product_Id, Time_Id are the dimensions that represent specific supermarkets, products, and time intervals

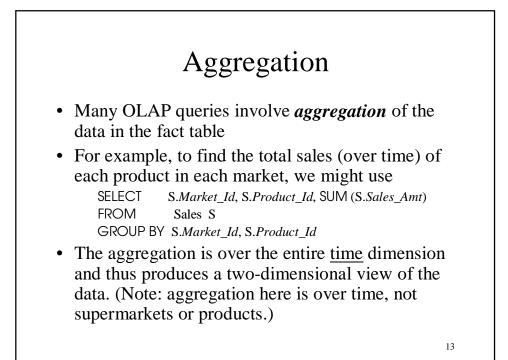
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- Sales_Amt is a function of the other three





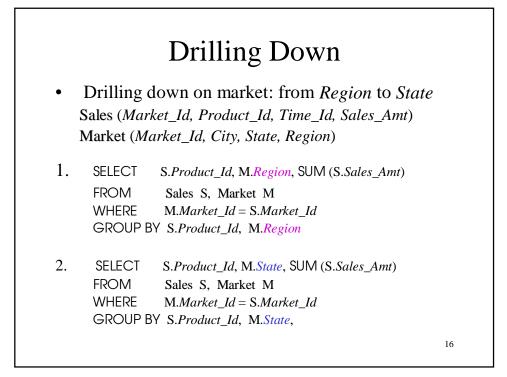


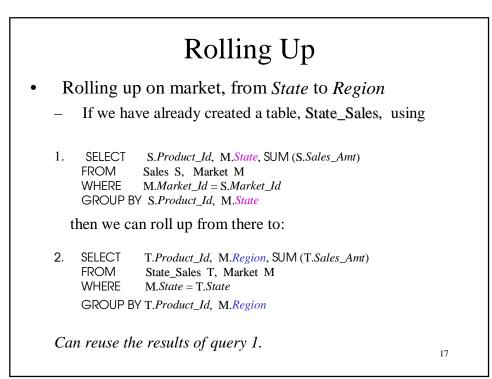


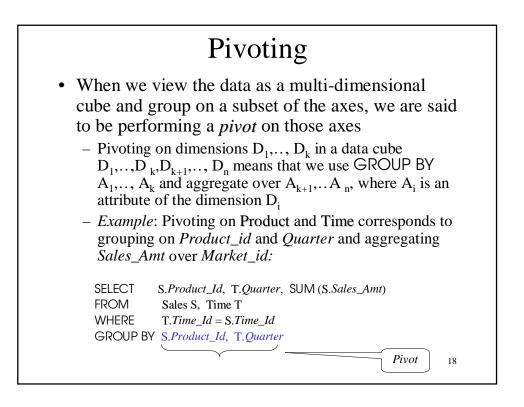
Aggregation over Time • The output of the previous query Market Id **M**1 M2 M3 M4 SUM(Sales_Amt) 3003 **P1** 1503 . . . Product_Id P2 6003 2402 . . . P3 4503 3 • • • 7503 7000 P4 . . . P5 ••• 14

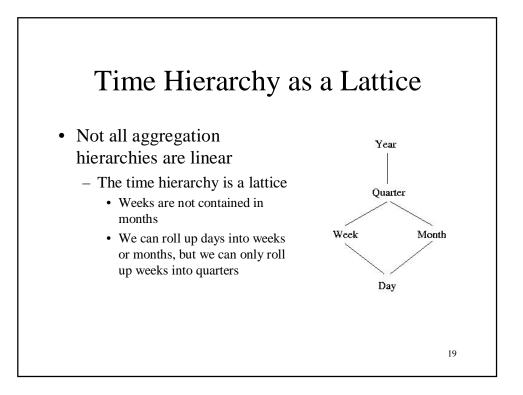
Drilling Down and Rolling Up

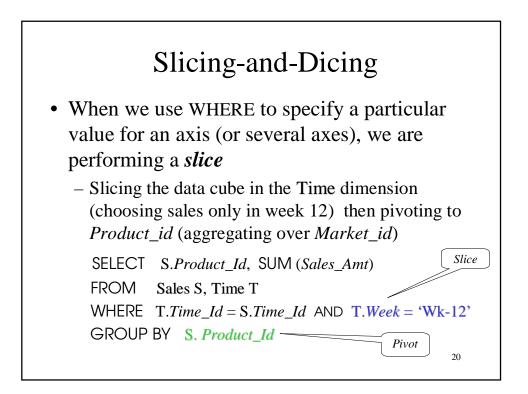
- Some dimension tables form an *aggregation hierarchy* Market_Id → City → State → Region
- Executing a series of queries that moves down a hierarchy (*e.g.*, from aggregation over regions to that over states) is called *drilling down*
 - Requires the use of the fact table or information more specific than the requested aggregation (*e.g.*, cities)
- Executing a series of queries that moves up the hierarchy (e.g., from states to regions) is called *rolling up*
 - Note: In a rollup, coarser aggregations can be computed using prior queries for finer aggregations

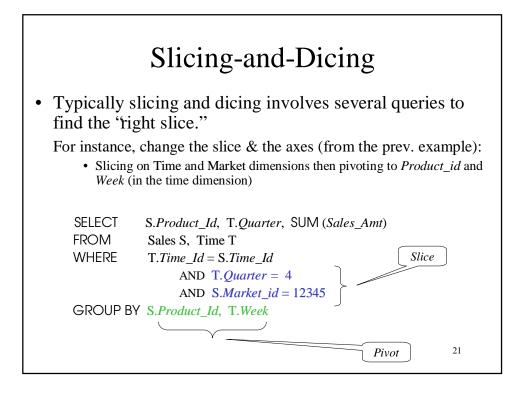




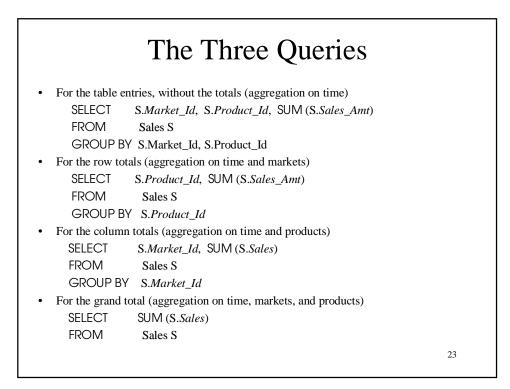


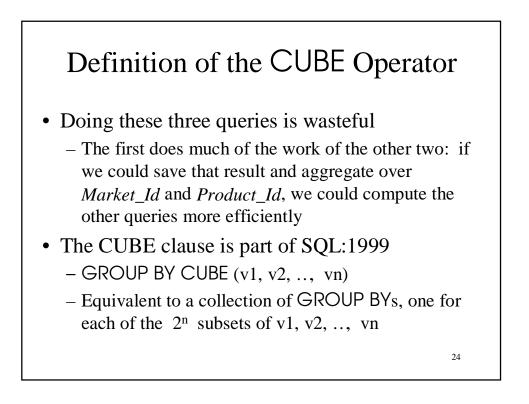






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	Fo construct the follow queries (next slide)	wing ta	ble, wo	uld tak	e 4
		Ì	Market_	_Id	
		M1	M2	M3	Total
Product_Id	SUM(Sales_Amt)				
	P1	3003	1503		
	P2	6003	2402		
duc	P3	Market_Id M1 M2 M Amt) 1503 P1 3003 1503 P2 6003 2402			
Pro	P4	7503	7000	••••	•••
	Total				

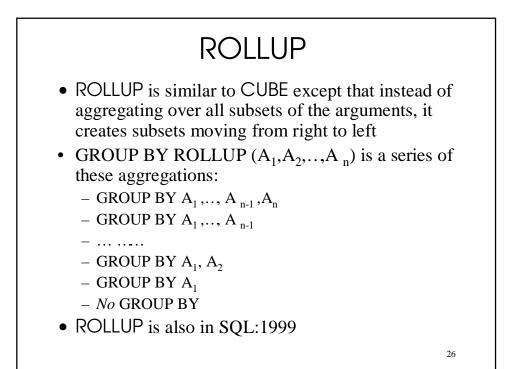


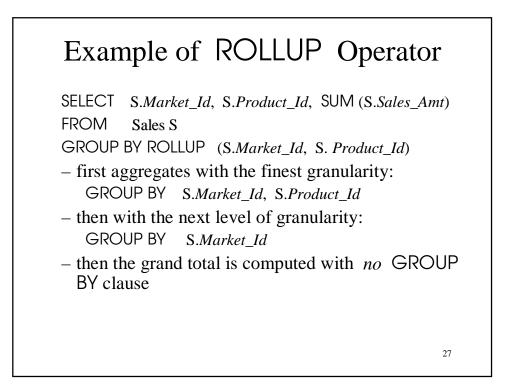


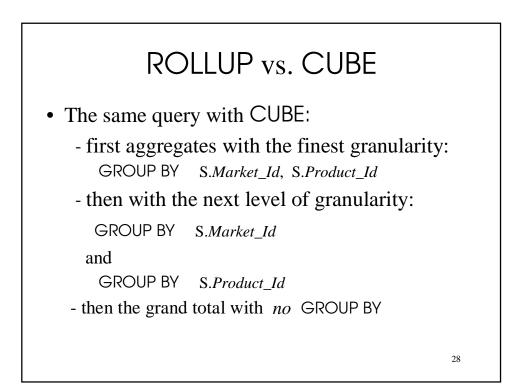
Example of CUBE Operator

• The following query returns all the information needed to make the previous products/markets table:

SELECT S.*Market_Id*, S.*Product_Id*, SUM (S.*Sales_Amt*) FROM Sales S GROUP BY CUBE (S.*Market_Id*, S.*Product_Id*)







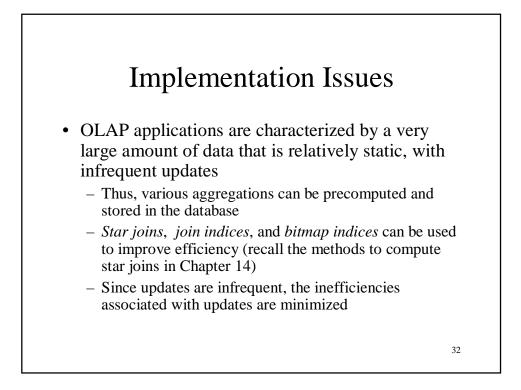
Materialized Views

The CUBE operator is often used to precompute aggregations on all dimensions of a fact table and then save them as a *materialized views* to speed up future queries

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MOLAP

- No standard query language for MOLAP databases
- Many MOLAP vendors (and many ROLAP vendors) provide proprietary visual languages that allow casual users to make queries that involve pivots, drilling down, or rolling up



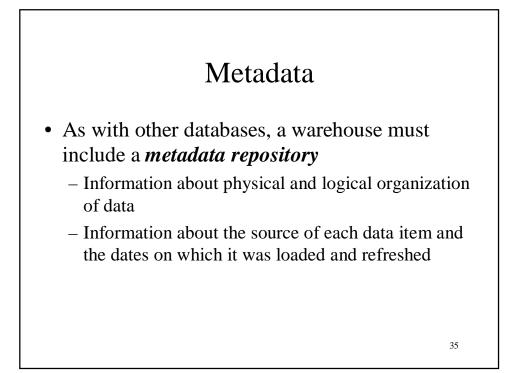
Data Warehouse

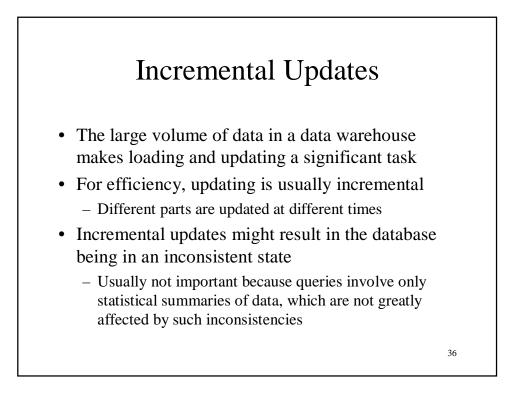
- Data (often derived from OLTP) for both OLAP and data mining applications is usually stored in a special database called a *data warehouse*
- Data warehouses are generally large and contain data that has been gathered at different times from DBMSs provided by different vendors and with different schemas
- Populating such a data warehouse is not trivial

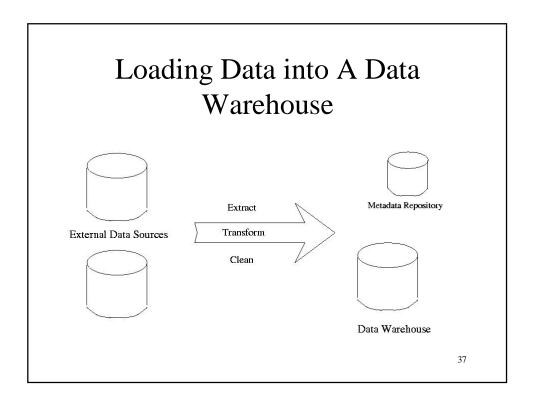
Issues Involved in Populating a Data Warehouse

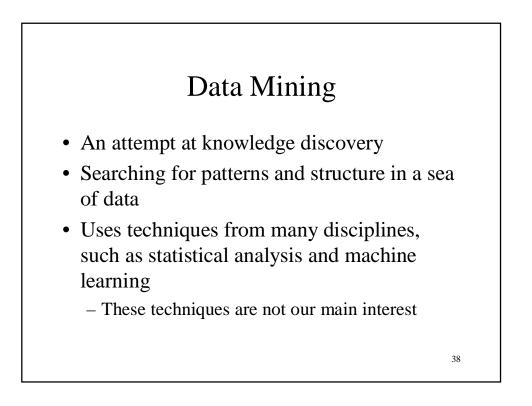
- Transformations
 - Syntactic: syntax used in different DMBSs for the same data might be different
 - Attribute names: SSN vs. Ssnum
 - Attribute domains: Integer vs. String
 - Semantic: semantics might be different
 - Summarizing sales on a daily basis vs. summarizing sales on a monthly basis
- Data Cleaning
 - Removing errors and inconsistencies in data

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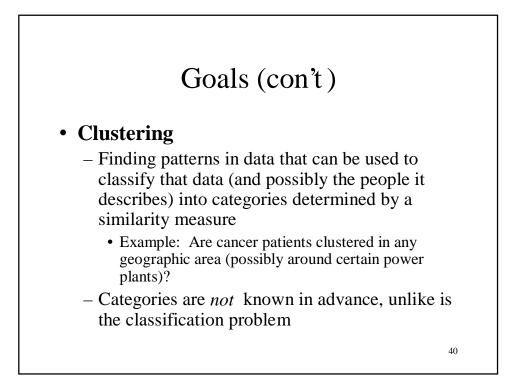




Goals of Data Mining

Association

- Finding patterns in data that associate instances of that data to related instances
 - Example: what types of books does a customer buy
- Classification
 - Finding patterns in data that can be used to classify that data (and possibly the people it describes)
 - Example 'high -end buyers" and 'low -end" buyers
 - This classification might then be used for Prediction
 - Which bank customers will default on their mortgages?
 - Categories for classification are known in advance



Associations

- An *association* is a correlation between certain values in a database (in the same or different columns)
 - In a convenience store in the early evening, a large percentage of customers who bought diapers also bought beer

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• This association can be described using the notation

Purchase_diapers => Purchase_beer

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Ascertain an Association

- To ascertain that an association exists, both the confidence and the support must be above a certain threshold
 - Confidence states that there is a high probability, given the data, that someone who purchased diapers also bought beer
 - Support states that the data shows a large percentage of people who purchased both diapers and beer (so that the confidence measure is not an accident)

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A Priori Algorithm for Computing Associations
Based on this observation:

If the support for A => B is larger than T, then the support for A and B must separately be larger than T
Find all items whose support is larger than T
Requires checking n items
If there are m items with support > T (presumably, n<<n), find all pairs of such items whose support is larger than T

Requires checking m(m-1) pairs
If there are p pairs with support > T, compute the confidence for each pair
Requires checking p pairs

Classification

- *Classification* involves finding patterns in data items that can be used to place those items in certain categories. That classification can then be used to predict future outcomes.
 - A bank might gather data from the application forms of past customers who applied for a mortgage and classify them as defaulters or non-defaulters.

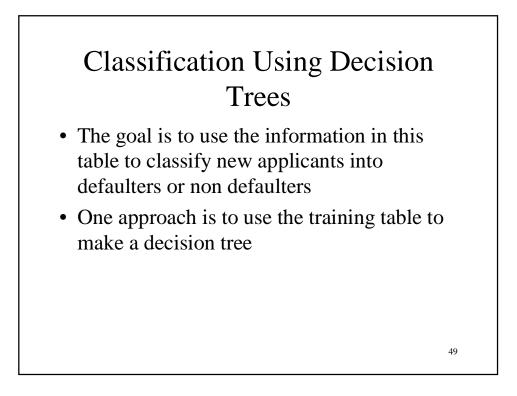
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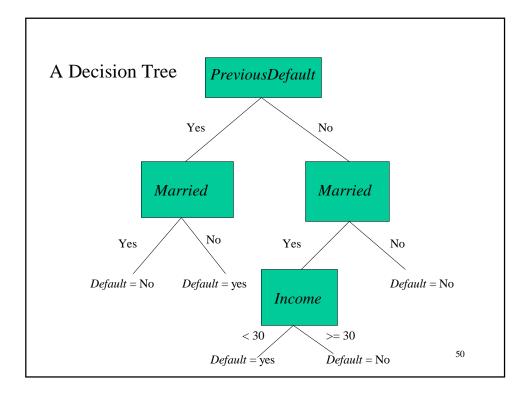
 Then when new customers apply, they might use the information on their application forms to predict whether or not they would default

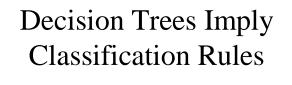
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Example: Loan Risk Evaluation
Suppose the bank used only three types of information to do the classification
Whether or not the applicant was married
Whether or not the applicant had previously defaulted
The applicants current income
The data about previous applicants might be stored in a table called the *training table*

Id	Married	PreviousDefault	Income	Default (outcome)
C1	Yes	No	50	No
C2	Yes	No	100	No
C3	No	Yes	135	Yes
C4	Yes	No	125	No
C5	Yes	No	50	No
C6	No	No	30	No
C7	Yes	Yes	10	No
C8	Yes	No	10	Yes
C9	Yes	No	75	No
C10	Yes	Yes	45	No

Id	Married	PreviousDefault	Income	Default (outcome)
C11	Yes	No	60	Yes
C12	No	Yes	125	Yes
C13	Yes	Yes	20	No
C14	No	No	15	No
C15	No	No	60	No
C16	Yes	No	15	Yes
C17	Yes	No	35	No
C18	No	Yes	160	Yes
C19	Yes	No	40	No
C20	Yes	No	30	No





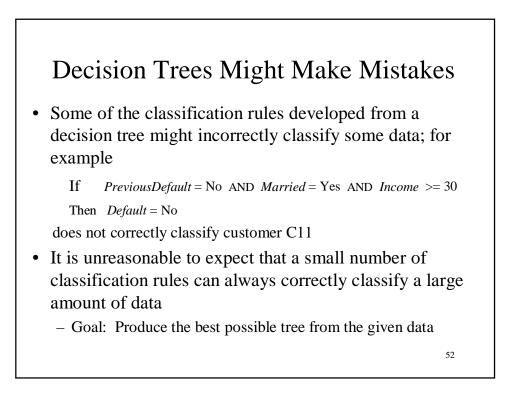


- Each classification rule implied by the tree corresponds to a path from the root to a leaf
- For example, one such rule is If

PreviousDefault = No AND *Married* = Yes AND *Income* < 30 **Then**

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Default = Yes



Producing a Decision Tree From a Training Set

- Several algorithms have been developed for constructing a decision tree from a training set
 We discuss the *ID3 algorithm*
- ID3 starts by selecting the attribute to be used at the top level of the tree to make the first decision
- This decision yields the nodes at the second level of the tree. The procedure repeats on each of these nodes

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Properties of the Entropy $-\sum p_i \log_2 p_i$

• Entropy determines the degree of randomness in the data:

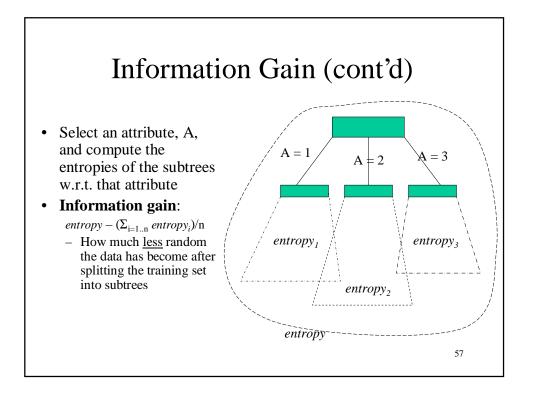
 $-p_{yes} = p_{no} = \frac{1}{2} - data \ is \ completely \ random$ entropy = -\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \log_2 \frac{1}{2} = \frac{1}{2} + \frac{1}{2} = 1

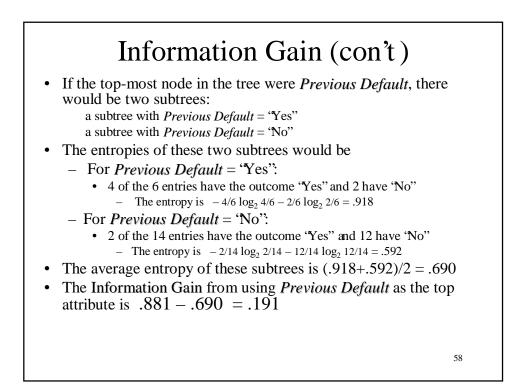
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$$p_{yes} = 1$$
, $p_{no} = 0$ or $p_{no} = 1$, $p_{yes} = 0$ - data is totally nonrandom
entropy = -1 log₂ 1 - 0 log₂ 0 = 0

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• The lower the entropy – the less randomness is in the data ≡ the more information is in the data

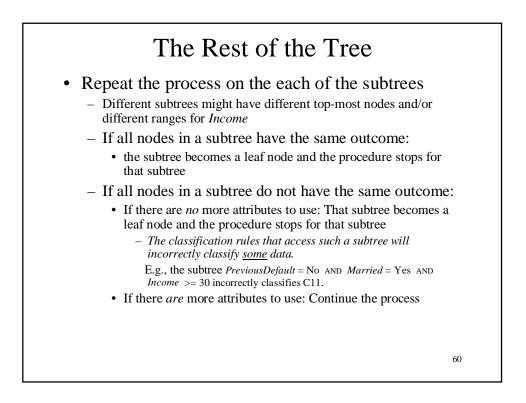
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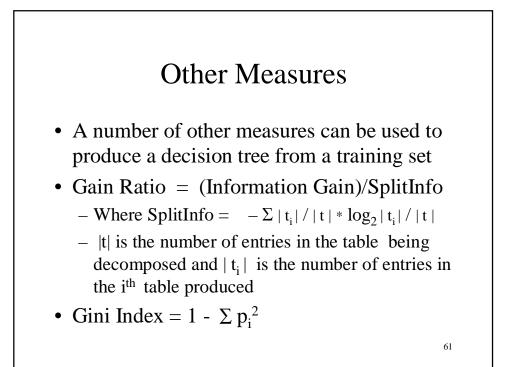


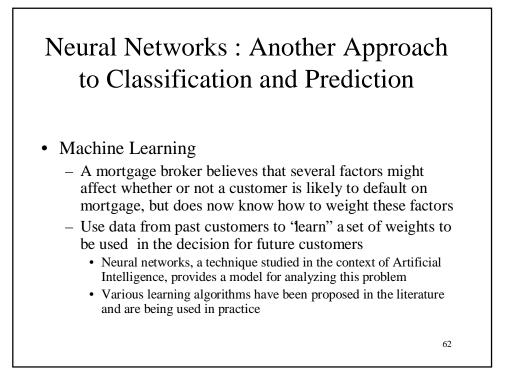


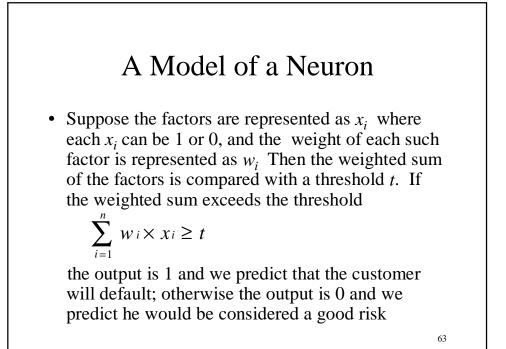
Comparing Information Gains

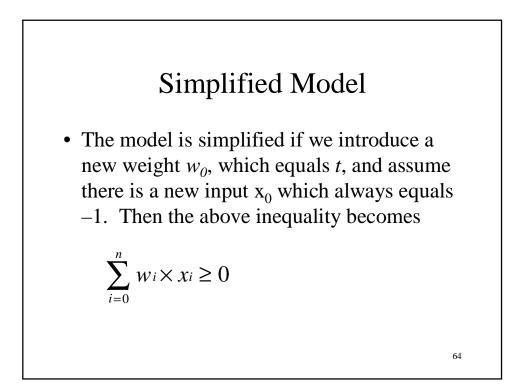
- *Previous Default* as the top-most attribute – The information gain = .191
- *Married* as the top-most attribute
 - The information gain = .036
- *Income* as the top-most attribute
 - Must compute information gain for all possible ranges
 - For example for the range Income < 50 and Income >= 50 the Information Gain is .031
- The maximum Information Gain turns out to be for the attribute *Previous Default*, so we select that as the top-most attribute in the decision tree











Step-Function Activation

- This model is said to have **step-function** activation
 - Its output is 1 if the weighted sum of the inputs is greater than or equal to 0
 - Its output is 0 otherwise
- Neurons with this activation function are sometimes called **perceptrons**.
- Later we will discuss another activation function

Perceptron Learning Algorithm

- Set the values of each weight (and threshold) to some small random number
- Apply the inputs one at a time and compute the outputs
- If the desired output for some input is d and the actual output is y, change each weight w_i by

$$\Delta w_i = \eta \times x_i \times (d - y)$$

where η is a small constant called the **learning factor**

• Continue until some termination condition is met

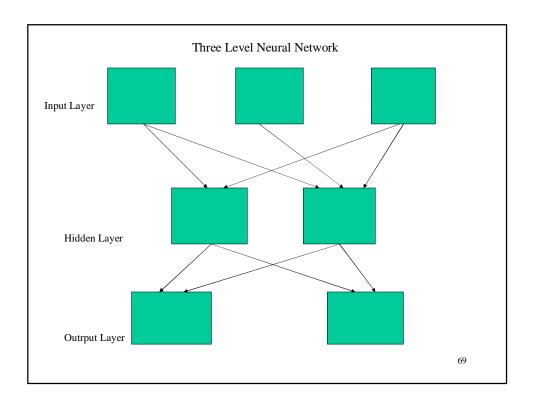
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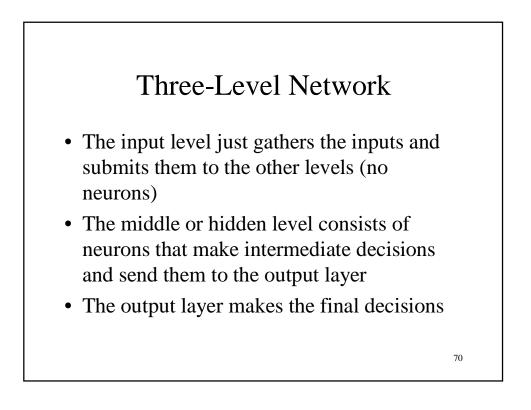
Rationale for Learning Algorithm

- If there is no error, no change in the weights are made
- If there is an error, each weight is changed in the direction to decrease the error
 - For example if the output is 0 and the desired output is 1, the weights of all the inputs that were 1 are increased and the threshold is decreased.

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Correctness and Problems with Perceptron Learning Algorithm
If the decision can always be made correctly by a single neuron, this algorithm will eventually 'learn'' the correct weights
The problem is that, for most applications, the decision cannot be made, even approximately, by a single neuron
We therefore consider networks of such neurons





The Sigmoid Activation Function

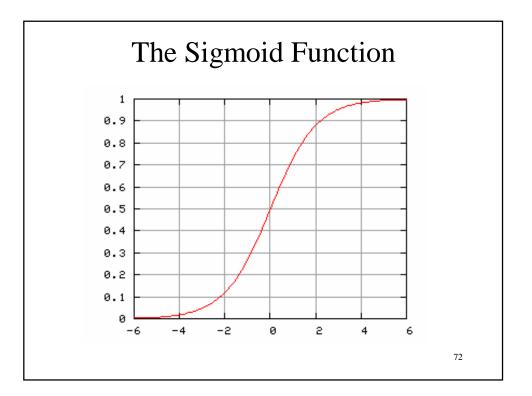
- To mathematically derive a learning algorithm for such a neural network, we must take derivatives
 - But we cannot take derivatives of the step function activation function
- Therefore we must use a continuous activation function
 - A common such activation function is the sigmoid function

$$y = 1/(1+e^{-X})$$

where

$$X = \sum_{i=0}^{n} w_i \times x_i$$





Properties of Sigmoid Function

- In some sense the sigmoid function is similar to the step function
 - It has the value .5 for x = 0
 - It becomes asymptotic to 1 for large positive values of x
 - It becomes asymptotic to θ for large negative values of x
- However it is continuous and, as can be easily computed, has the derivative

$$\frac{\partial y}{\partial X} = e^{-X} / (1 + e^{-X})^2 = y \times (1 - y)$$

which is used in many of the following computations

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Learning Algorithm for a Single Sigmoid Neuron

- The idea is to take the derivative of the squared error with respect to each of the weights and change each weight by a small multiple of the negative of that derivative
 - Called the Gradient Descent Approach
 - Move in the direction towards the minimum of the function

$$\Delta w_i = -\eta \times \frac{\partial (d-y)^2}{\partial w_i}$$

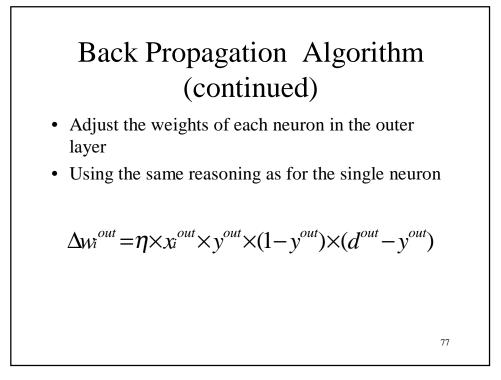
The Algorithm for One Neuron (continued)

• After a bit of math, and using the previous result for the derivative of the sigmoid function, we get

$$\Delta w_i = \eta \times x_i \times y \times (1 - y) \times (d - y)$$

Back Propogation Algorithm for 3-Level Neural Network

- Initially set the values of all weights to some small random number
- Apply the inputs from the learning set one at a time and, for each input, compute the outputs of the neurons in the output layer



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Back Propagation Algorithm (continued)

- Now consider neurons in the hidden layer. Assume first that there is only one neuron in the output layer
- Using the same reasoning as before, the gradient descent method tells us that

$$\Delta w_i^{mid} = -\eta \times \frac{\partial (d^{out} - y^{out})^2}{\partial w_i^{mid}}$$

Back Propagation Algorithm (continued)

• Doing the math, we get

$$\Delta w_i^{mid} = \eta \times x_i^{mid} \times \delta^{mid}$$

where

$$\delta^{mid} = y^{mid} \times (1 - y^{mid}) \times w^{midout} \times \delta^{out}$$

and where δ^{out} was previously computed (the back propagation property)

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Back Propagation Algorithm (continued)

• If there is more than one neuron in the output layer, we compute

$$\Delta w_i^{mid} = -\eta \times \frac{\partial \sum_j (d_j^{out} - y_j^{out})^2}{\partial w_i^{mid}}$$

$$= \eta \times x i^{mid} \times \delta^{mid}$$

where

$$\delta^{mid} = y^{mid} \times (1 - y^{mid}) \times \sum_{j} (w_{j}^{mid/out} \times \delta_{j}^{out})$$

Back Propagation Algorithm (continued)

- Continue the training until some termination condition is met
 - The data in the training set has been used some fixed number of times
 - The number of errors has stopped decreasing significantly
 - The weights have stopped changing significantly
 - The number of errors has reached some predetermined level

Clustering

- Given:
 - a set of items
 - characteristic attributes for the items
 - a similarity measure based on those attributes
- *Clustering* involves placing those items into *clusters*, such that items in the same cluster are close according to the similarity measure
 - Different from Classification: there the categories are known in advance
- For example, cancer patients might have the attribute *location*, and might be placed in clusters with similar locations.

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Example: Clustering Students by Age

Student Id	Age	GPA
S 1	17	3.9
S2	17	3.5
S3	18	3.1
S4	20	3.0
S5	23	3.5
S6	26	2.6

K-Means Algorithm

- To cluster a set of items into *k* categories
 - 1. Pick *k* items at random to be the (initial) centers of the clusters (so each selected item is in its own cluster)
 - 2. Place each item *in the training set* in the cluster to which it is closest to the center
 - 3. Recalculate the centers of each cluster as the mean of the items in that cluster
 - 4. Repeat the procedure starting at Step 2 until there is no change in the membership of any cluster

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The Hiearchical or Aglomerative Algorithm

- Number of clusters is not fixed in advance
- Initially select each item in the training set as the center of its own cluster
- Select two clusters to merge into a single center
 - One approach it to pick the clusters whose centers are closest according to some measure (e.g., Euclidian distance)
- Continue until some termination condition is reached (e.g., the number of clusters falls below some limit)

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