

Data Mining:

Concepts and Techniques

— Chapter 6 —

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Chapter 6. Classification and Prediction

- What is classification? What is prediction? 
- Issues regarding classification and prediction
- Classification by decision tree induction
- Bayesian classification
- Rule-based classification
- Classification by back propagation
- Support Vector Machines (SVM)
- Associative classification
- Lazy learners (or learning from your neighbors)
- Other classification methods
- Prediction
- Accuracy and error measures
- Ensemble methods
- Model selection
- Summary

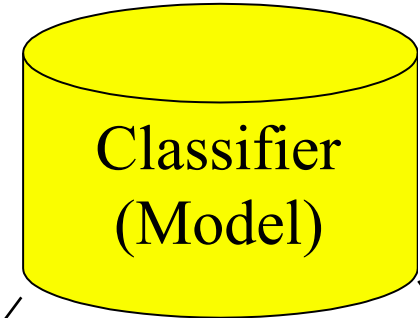
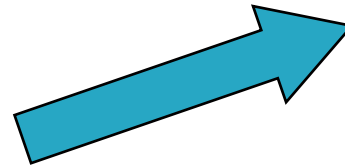
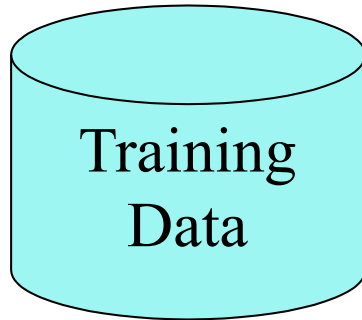
Classification vs. Prediction

- **Classification**
 - predicts categorical class labels (discrete or nominal)
 - classifies data (constructs a model) based on the training set and the values (**class labels**) in a classifying attribute and uses it in classifying new data
- **Prediction**
 - models continuous-valued functions, i.e., predicts unknown or missing values
- Typical applications
 - Credit approval
 - Target marketing
 - Medical diagnosis
 - Fraud detection

Classification—A Two-Step Process

- **Model construction**: describing a set of predetermined classes
 - Each tuple/sample is assumed to belong to a predefined class, as determined by the **class label attribute**
 - The set of tuples used for model construction is **training set**
 - The model is represented as classification rules, decision trees, or mathematical formulae
- **Model usage**: for classifying future or unknown objects
 - **Estimate accuracy** of the model
 - The known label of test sample is compared with the classified result from the model
 - Accuracy rate is the percentage of test set samples that are correctly classified by the model
 - Test set is independent of training set, otherwise over-fitting will occur
 - If the accuracy is acceptable, use the model to **classify data** tuples whose class labels are not known

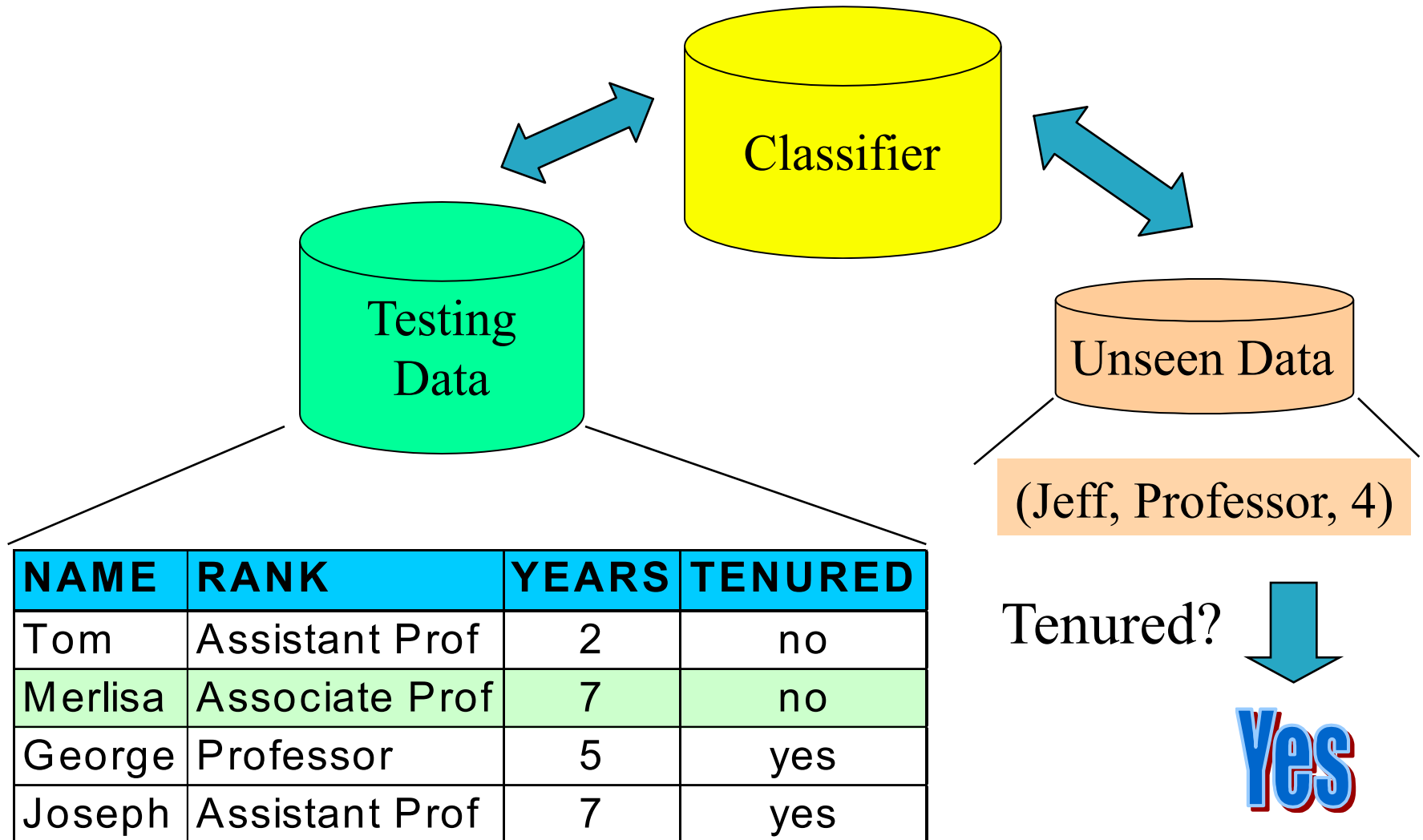
Process (1): Model Construction



NAME	RANK	YEARS	TENURED
Mike	Assistant Prof	3	no
Mary	Assistant Prof	7	yes
Bill	Professor	2	yes
Jim	Associate Prof	7	yes
Dave	Assistant Prof	6	no
Anne	Associate Prof	3	no

IF rank = 'professor'
OR years > 6
THEN tenured = 'yes'


Process (2): Using the Model in Prediction



Supervised vs. Unsupervised Learning

- **Supervised learning (classification)**
 - Supervision: The training data (observations, measurements, etc.) are accompanied by labels indicating the class of the observations
 - New data is classified based on the training set
- **Unsupervised learning (clustering)**
 - The class labels of training data is unknown
 - Given a set of measurements, observations, etc. with the aim of establishing the existence of classes or clusters in the data

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Issues: Data Preparation

- Data cleaning
 - Preprocess data in order to reduce noise and handle missing values
- Relevance analysis (feature selection)
 - Remove the irrelevant or redundant attributes
- Data transformation
 - Generalize and/or normalize data

Issues: Evaluating Classification Methods

- Accuracy
 - classifier accuracy: predicting class label
 - predictor accuracy: guessing value of predicted attributes
- Speed
 - time to construct the model (training time)
 - time to use the model (classification/prediction time)
- Robustness: handling noise and missing values
- Scalability: efficiency in disk-resident databases
- Interpretability
 - understanding and insight provided by the model
- Other measures, e.g., goodness of rules, such as decision tree size or compactness of classification rules

Chapter 6. Classification and Prediction

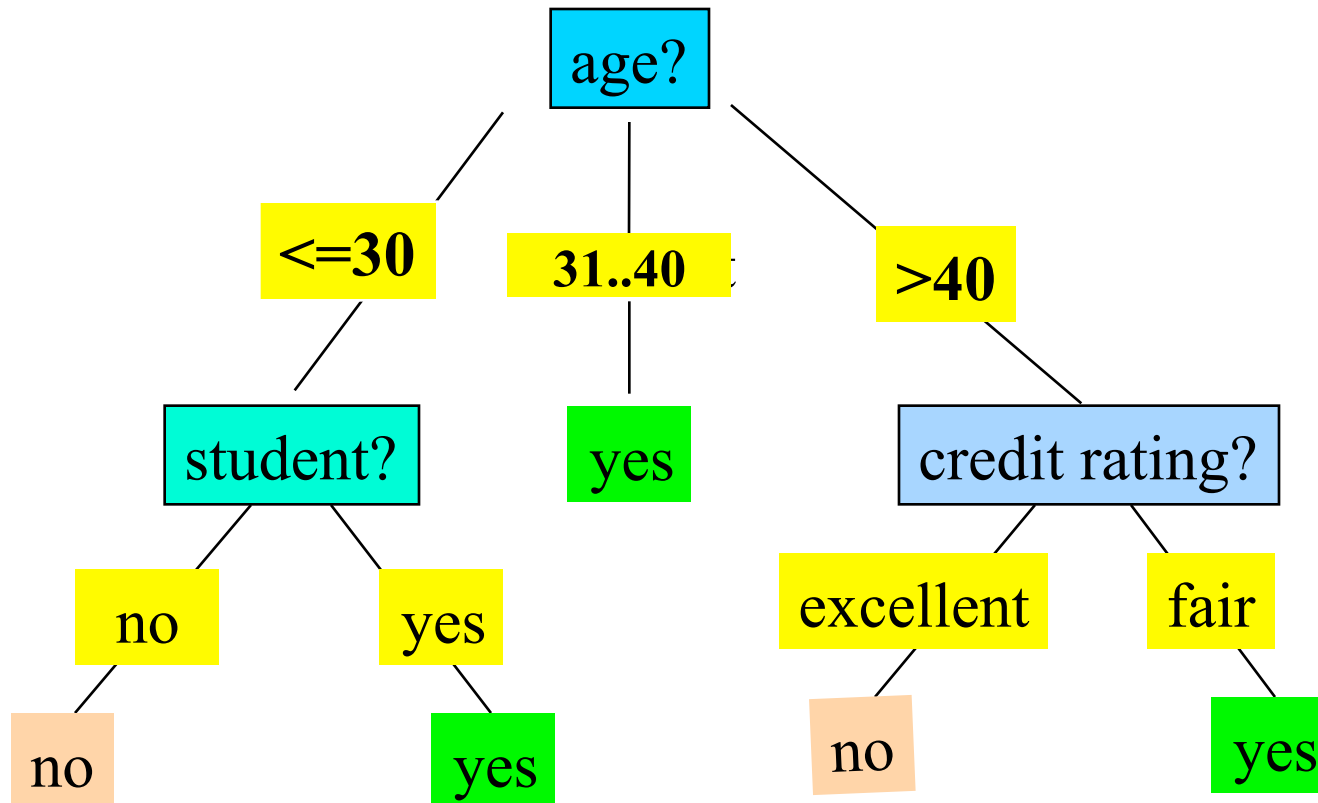
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Decision Tree Induction: Training Dataset

This follows an example of Quinlan's ID3 (Playing Tennis)

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

Output: A Decision Tree for “*buys_computer*”



Algorithm for Decision Tree Induction

- Basic algorithm (a greedy algorithm)
 - Tree is constructed in a **top-down recursive divide-and-conquer manner**
 - At start, all the training examples are at the root
 - Attributes are categorical (if continuous-valued, they are discretized in advance)
 - Examples are partitioned recursively based on selected attributes
 - Test attributes are selected on the basis of a heuristic or statistical measure (e.g., **information gain**)
- Conditions for stopping partitioning
 - All samples for a given node belong to the same class
 - There are no remaining attributes for further partitioning – **majority voting** is employed for classifying the leaf
 - There are no samples left

Attribute Selection Measure: Information Gain (ID3/C4.5)

- Select the attribute with the highest information gain
- Let p_i be the probability that an arbitrary tuple in D belongs to class C_i , estimated by $|C_{i,D}|/|D|$
- **Expected information** (entropy) needed to classify a tuple in D :

$$Info(D) = - \sum_{i=1}^m p_i \log_2(p_i)$$

- **Information** needed (after using A to split D into v partitions) to classify D :

$$Info_A(D) = \sum_{j=1}^v \frac{|D_j|}{|D|} \times I(D_j)$$

- **Information gained** by branching on attribute A

$$Gain(A) = Info(D) - Info_A(D)$$

Attribute Selection: Information Gain

- Class P: buys_computer = "yes"

- Class N: buys_computer = "no"

$$Info(D) = I(9,5) = -\frac{9}{14} \log_2\left(\frac{9}{14}\right) - \frac{5}{14} \log_2\left(\frac{5}{14}\right) = 0.940$$

$$Info_{age}(D) = \frac{5}{14} I(2,3) + \frac{4}{14} I(4,0) + \frac{5}{14} I(3,2) = 0.694$$

age	p_i	n_i	$I(p_i, n_i)$
≤ 30	2	3	0.971
31...40	4	0	0
> 40	3	2	0.971

$\frac{5}{14} I(2,3)$ means "age ≤ 30 " has 5 out of 14 samples, with 2 yes'es and 3 no's. Hence

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

Similarly,

$$Gain(income) = 0.029$$

$$Gain(student) = 0.151$$

$$Gain(credit_rating) = 0.048$$

age	income	student	credit_rating	buys_computer
≤ 30	high	no	fair	no
≤ 30	high	no	excellent	no
31...40	high	no	fair	yes
> 40	medium	no	fair	yes
> 40	low	yes	fair	yes
> 40	low	yes	excellent	no
31...40	low	yes	excellent	yes
≤ 30	medium	no	fair	no
≤ 30	low	yes	fair	yes
> 40	medium	yes	fair	yes
≤ 30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
> 40	medium	no	excellent	no

Computing Information-Gain for Continuous-Value Attributes

- Let attribute A be a continuous-valued attribute
- Must determine the *best split point* for A
 - Sort the value A in increasing order
 - Typically, the midpoint between each pair of adjacent values is considered as a possible *split point*
 - $(a_i + a_{i+1})/2$ is the midpoint between the values of a_i and a_{i+1}
 - The point with the *minimum expected information requirement* for A is selected as the split-point for A
- Split:
 - D_1 is the set of tuples in D satisfying $A \leq \text{split-point}$, and D_2 is the set of tuples in D satisfying $A > \text{split-point}$

Gain Ratio for Attribute Selection (C4.5)

- Information gain measure is biased towards attributes with a large number of values
- C4.5 (a successor of ID3) uses gain ratio to overcome the problem (normalization to information gain)

$$\text{SplitInfo}_A(D) = - \sum_{j=1}^v \frac{|D_j|}{|D|} \times \log_2 \left(\frac{|D_j|}{|D|} \right)$$

- $\text{GainRatio}(A) = \text{Gain}(A) / \text{SplitInfo}(A)$
- Ex. $\text{SplitInfo}_A(D) = -\frac{4}{14} \times \log_2 \left(\frac{4}{14} \right) - \frac{6}{14} \times \log_2 \left(\frac{6}{14} \right) - \frac{4}{14} \times \log_2 \left(\frac{4}{14} \right) = 0.926$
 - $\text{gain_ratio}(\text{income}) = 0.029 / 0.926 = 0.031$
- The attribute with the maximum gain ratio is selected as the splitting attribute

Gini index (CART, IBM IntelligentMiner)

- If a data set D contains examples from n classes, gini index, $gini(D)$ is defined as

$$gini(D) = 1 - \sum_{j=1}^n p_j^2$$

where p_j is the relative frequency of class j in D

- If a data set D is split on A into two subsets D_1 and D_2 , the $gini$ index $gini_A(D)$ is defined as

$$gini_A(D) = \frac{|D_1|}{|D|} gini(D_1) + \frac{|D_2|}{|D|} gini(D_2)$$

- Reduction in Impurity:

$$\Delta gini(A) = gini(D) - gini_A(D)$$

- The attribute provides the smallest $gini_{split}(D)$ (or the largest reduction in impurity) is chosen to split the node (*need to enumerate all the possible splitting points for each attribute*)

Gini index (CART, IBM IntelligentMiner)

- Ex. D has 9 tuples in `buys_computer = "yes"` and 5 in "no"

$$gini(D) = 1 - \left(\frac{9}{14}\right)^2 - \left(\frac{5}{14}\right)^2 = 0.459$$

- Suppose the attribute `income` partitions D into 10 in D_1 : {low, medium} and 4 in D_2
$$gini_{income \in \{low, medium\}}(D) = \left(\frac{10}{14}\right)Gini(D_1) + \left(\frac{4}{14}\right)Gini(D_2)$$
$$= \frac{10}{14} \left(1 - \left(\frac{6}{10}\right)^2 - \left(\frac{4}{10}\right)^2\right) + \frac{4}{14} \left(1 - \left(\frac{1}{4}\right)^2 - \left(\frac{3}{4}\right)^2\right)$$
$$= 0.450$$
$$= Gini_{income \in \{high\}}(D)$$

but $gini_{\{medium, high\}}$ is 0.30 and thus the best since it is the lowest

- All attributes are assumed continuous-valued
- May need other tools, e.g., clustering, to get the possible split values
- Can be modified for categorical attributes

Comparing Attribute Selection Measures

- The three measures, in general, return good results but
 - Information gain:
 - biased towards multivalued attributes
 - Gain ratio:
 - tends to prefer unbalanced splits in which one partition is much smaller than the others
 - Gini index:
 - biased to multivalued attributes
 - has difficulty when # of classes is large
 - tends to favor tests that result in equal-sized partitions and purity in both partitions

Other Attribute Selection Measures

- CHAID: a popular decision tree algorithm, measure based on χ^2 test for independence
- C-SEP: performs better than info. gain and gini index in certain cases
- G-statistics: has a close approximation to χ^2 distribution
- MDL (Minimal Description Length) principle (i.e., the simplest solution is preferred):
 - The best tree as the one that requires the fewest # of bits to both (1) encode the tree, and (2) encode the exceptions to the tree
- Multivariate splits (partition based on multiple variable combinations)
 - CART: finds multivariate splits based on a linear comb. of attrs.
- Which attribute selection measure is the best?
 - Most give good results, none is significantly superior than others

Overfitting and Tree Pruning

- **Overfitting:** An induced tree may overfit the training data
 - Too many branches, some may reflect anomalies due to noise or outliers
 - Poor accuracy for unseen samples
- **Two approaches to avoid overfitting**
 - **Prepruning:** Halt tree construction early—do not split a node if this would result in the goodness measure falling below a threshold
 - Difficult to choose an appropriate threshold
 - **Postpruning:** Remove branches from a “fully grown” tree—get a sequence of progressively pruned trees
 - Use a set of data different from the training data to decide which is the “best pruned tree”

Enhancements to Basic Decision Tree Induction

- Allow for continuous-valued attributes
 - Dynamically define new discrete-valued attributes that partition the continuous attribute value into a discrete set of intervals
- Handle missing attribute values
 - Assign the most common value of the attribute
 - Assign probability to each of the possible values
- Attribute construction
 - Create new attributes based on existing ones that are sparsely represented
 - This reduces fragmentation, repetition, and replication

Classification in Large Databases

- Classification—a classical problem extensively studied by statisticians and machine learning researchers
- Scalability: Classifying data sets with millions of examples and hundreds of attributes with reasonable speed
- Why decision tree induction in data mining?
 - relatively faster learning speed (than other classification methods)
 - convertible to simple and easy to understand classification rules
 - can use SQL queries for accessing databases
 - comparable classification accuracy with other methods

Scalable Decision Tree Induction Methods

- **SLIQ** (EDBT' 96 — Mehta et al.)
 - Builds an index for each attribute and only class list and the current attribute list reside in memory
- **SPRINT** (VLDB' 96 — J. Shafer et al.)
 - Constructs an attribute list data structure
- **PUBLIC** (VLDB' 98 — Rastogi & Shim)
 - Integrates tree splitting and tree pruning: stop growing the tree earlier
- **RainForest** (VLDB' 98 — Gehrke, Ramakrishnan & Ganti)
 - Builds an AVC-list (attribute, value, class label)
- **BOAT** (PODS' 99 — Gehrke, Ganti, Ramakrishnan & Loh)
 - Uses bootstrapping to create several small samples

Scalability Framework for RainForest

- Separates the scalability aspects from the criteria that determine the quality of the tree
- Builds an AVC-list: **AVC (Attribute, Value, Class_label)**
- **AVC-set** (of an attribute X)
 - Projection of training dataset onto the attribute X and class label where counts of individual class label are aggregated
- **AVC-group** (of a node n)
 - Set of AVC-sets of all predictor attributes at the node n

Rainforest: Training Set and Its AVC Sets

Training Examples

age	income	student	credit_rating	comp
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
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<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

AVC-set on *Age*

Age	Buy_Computer	
	yes	no
<=30	3	2
31..40	4	0
>40	3	2

AVC-set on *income*

income	Buy_Computer	
	yes	no
high	2	2
medium	4	2
low	3	1

AVC-set on *Student*

student	Buy_Computer	
	yes	no
yes	6	1
no	3	4

AVC-set on *credit_rating*

Credit rating	Buy_Computer	
	yes	no
fair	6	2
excellent	3	3

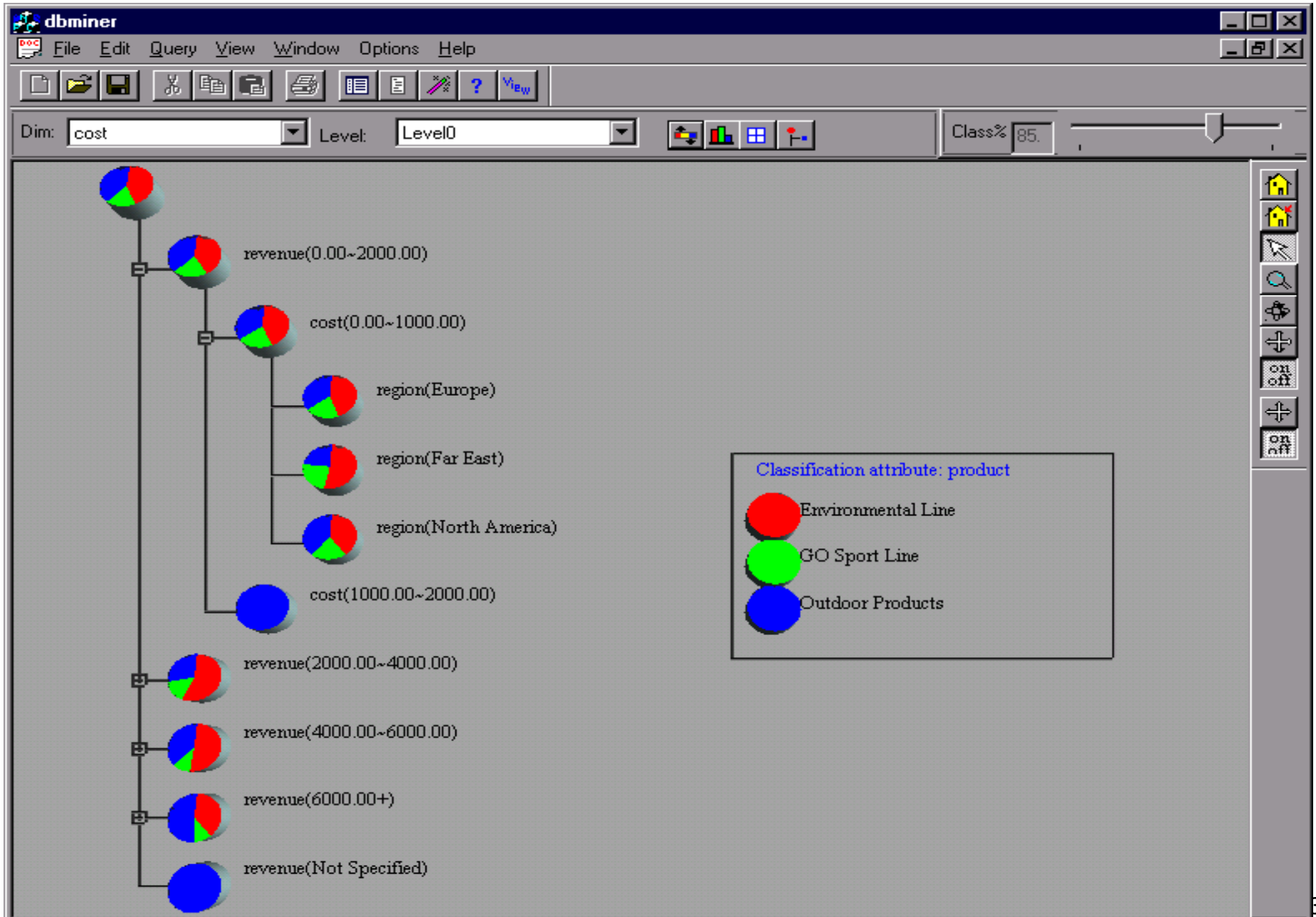
Data Cube-Based Decision-Tree Induction

- Integration of generalization with decision-tree induction (Kamber et al.' 97)
- Classification at primitive concept levels
 - E.g., precise temperature, humidity, outlook, etc.
 - Low-level concepts, scattered classes, bushy classification-trees
 - Semantic interpretation problems
- Cube-based multi-level classification
 - Relevance analysis at multi-levels
 - Information-gain analysis with dimension + level

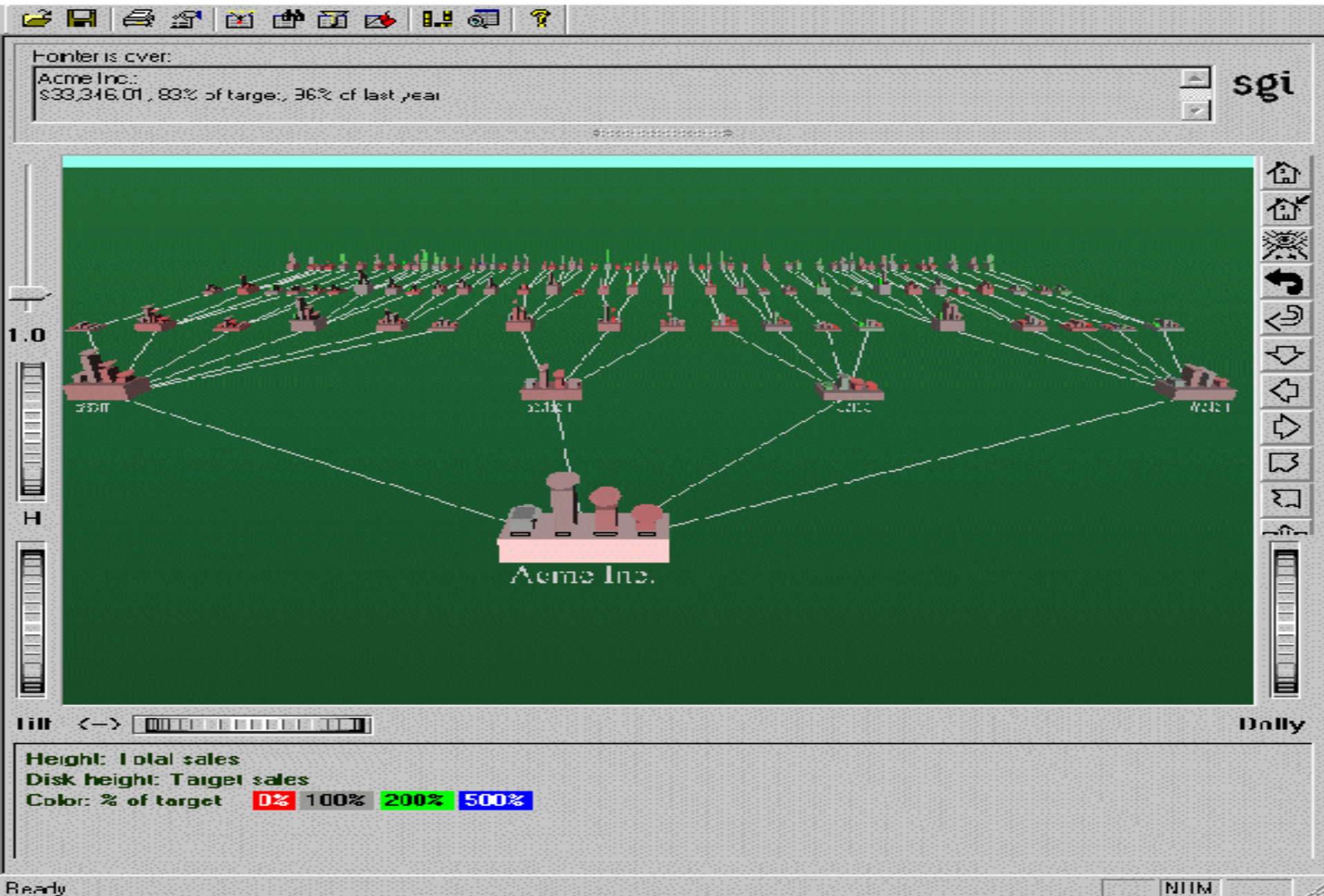
BOAT (Bootstrapped Optimistic Algorithm for Tree Construction)

- Use a statistical technique called *bootstrapping* to create several smaller samples (subsets), each fits in memory
- Each subset is used to create a tree, resulting in several trees
- These trees are examined and used to construct a new tree T'
 - It turns out that T' is very close to the tree that would be generated using the whole data set together
- Adv: requires only two scans of DB, an incremental alg.

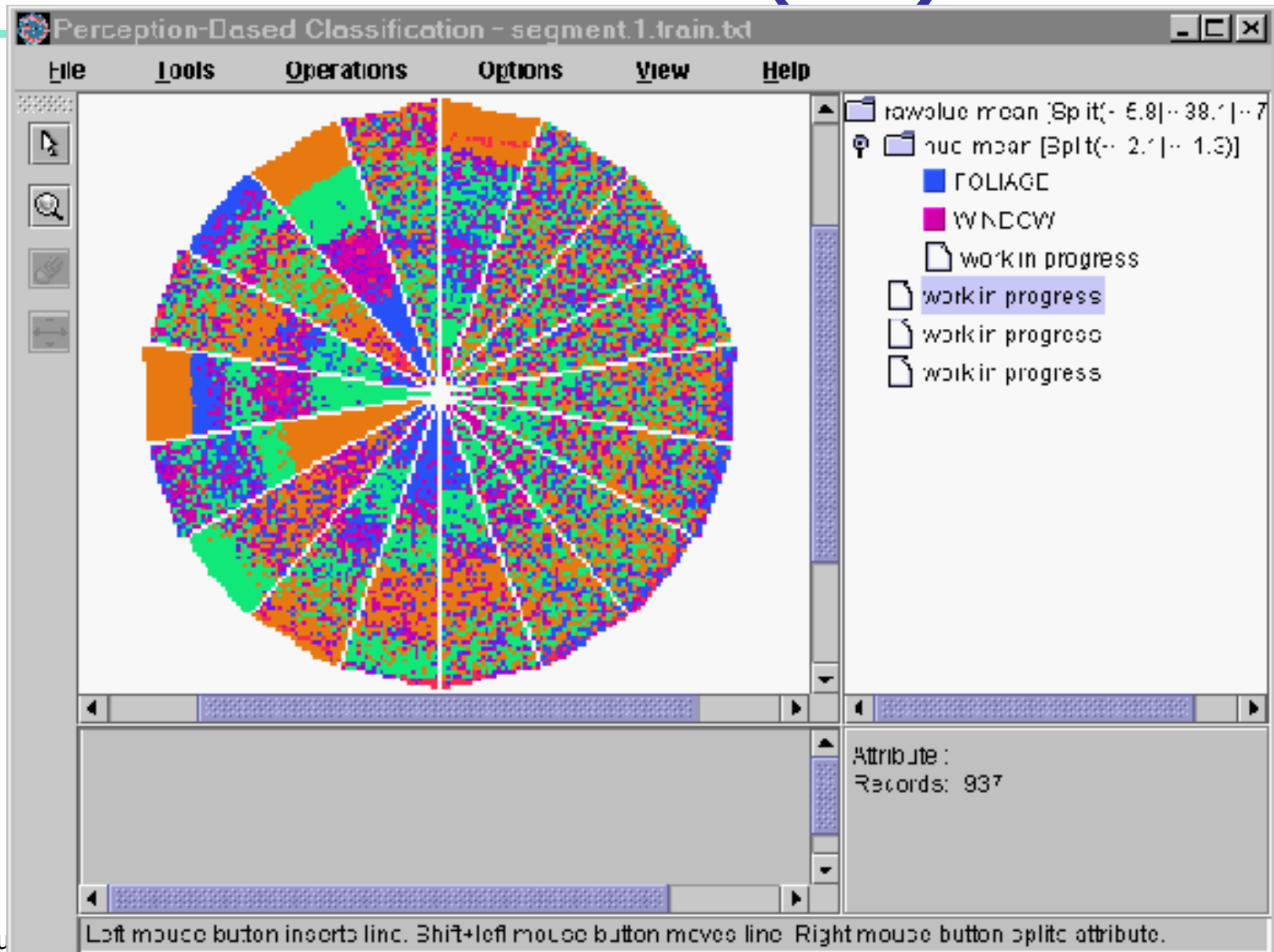
Presentation of Classification Results




Visualization of a Decision Tree in SGI/MineSet 3.0



Interactive Visual Mining by Perception-Based Classification (PBC)



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Bayesian Classification: Why?

- A statistical classifier: performs *probabilistic prediction*, *i.e.*, predicts class membership probabilities
- Foundation: Based on Bayes' Theorem.
- Performance: A simple Bayesian classifier, *naïve Bayesian classifier*, has comparable performance with decision tree and selected neural network classifiers
- Incremental: Each training example can incrementally increase/decrease the probability that a hypothesis is correct — prior knowledge can be combined with observed data
- Standard: Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

Bayesian Theorem: Basics

- Let \mathbf{X} be a data sample (“*evidence*”): class label is unknown
- Let H be a *hypothesis* that X belongs to class C
- Classification is to determine $P(H|\mathbf{X})$, the probability that the hypothesis holds given the observed data sample \mathbf{X}
- $P(H)$ (*prior probability*), the initial probability
 - E.g., \mathbf{X} will buy computer, regardless of age, income, ...
- $P(\mathbf{X})$: probability that sample data is observed
- $P(\mathbf{X}|H)$ (*posteriori probability*), the probability of observing the sample \mathbf{X} , given that the hypothesis holds
 - E.g., Given that \mathbf{X} will buy computer, the prob. that X is 31, 40, medium income

Bayesian Theorem

- Given training data \mathbf{X} , *posteriori probability of a hypothesis* H , $P(H|\mathbf{X})$, follows the Bayes theorem

$$P(H|\mathbf{X}) = \frac{P(\mathbf{X}|H)P(H)}{P(\mathbf{X})}$$

- Informally, this can be written as
posteriori = likelihood x prior/evidence
- Predicts \mathbf{X} belongs to C_2 iff the probability $P(C_i|\mathbf{X})$ is the highest among all the $P(C_k|\mathbf{X})$ for all the k classes
- Practical difficulty: require initial knowledge of many probabilities, significant computational cost

Towards Naïve Bayesian Classifier

- Let D be a training set of tuples and their associated class labels, and each tuple is represented by an n -D attribute vector $\mathbf{X} = (x_1, x_2, \dots, x_n)$
- Suppose there are m classes C_1, C_2, \dots, C_m .
- Classification is to derive the maximum posteriori, i.e., the maximal $P(C_i|\mathbf{X})$
- This can be derived from Bayes' theorem

$$P(C_i|\mathbf{X}) = \frac{P(\mathbf{X}|C_i)P(C_i)}{P(\mathbf{X})}$$

- Since $P(\mathbf{X})$ is constant for all classes, only

$$P(C_i|\mathbf{X}) = P(\mathbf{X}|C_i)P(C_i)$$

needs to be maximized

Derivation of Naïve Bayes Classifier

- A simplified assumption: attributes are conditionally independent (i.e., no dependence relation between attributes):

$$P(\mathbf{X} | C_i) = \prod_{k=1}^n P(x_k | C_i) = P(x_1 | C_i) \times P(x_2 | C_i) \times \dots \times P(x_n | C_i)$$

- This greatly reduces the computation cost: Only counts the class distribution
- If A_k is categorical, $P(x_k | C_i)$ is the # of tuples in C_i having value x_k for A_k divided by $|C_i, D|$ (# of tuples of C_i in D)
- If A_k is continuous-valued, $P(x_k | C_i)$ is usually computed based on Gaussian distribution with a mean μ and standard deviation σ

$$g(x, \mu, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

and $P(x_k | C_i)$ is

$$P(\mathbf{X} | C_i) = g(x_k, \mu_{C_i}, \sigma_{C_i})$$

Naïve Bayesian Classifier: Training Dataset

age	income	student	credit_rating	compu
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
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>40	low	yes	excellent	no
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<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

Class:

C1:buys_computer = 'yes'

C2:buys_computer = 'no'

Data sample

X = (age <=30,

Income = medium,

Student = yes

Credit_rating = Fair)

Naïve Bayesian Classifier: An Example

- $P(C_i)$:
 $P(\text{buys_computer} = \text{"yes"}) = 9/14 = 0.643$
 $P(\text{buys_computer} = \text{"no"}) = 5/14 = 0.357$
- Compute $P(X|C_i)$ for each class
 $P(\text{age} = \text{"<=30"} | \text{buys_computer} = \text{"yes"}) = 2/9 = 0.222$
 $P(\text{age} = \text{"<= 30"} | \text{buys_computer} = \text{"no"}) = 3/5 = 0.6$
 $P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"yes"}) = 4/9 = 0.444$
 $P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$
 $P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$
 $P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"no"}) = 1/5 = 0.2$
 $P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$
 $P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$
- **$X = (\text{age} \leq 30, \text{income} = \text{medium}, \text{student} = \text{yes}, \text{credit_rating} = \text{fair})$**

$$P(X|C_i) : P(X|\text{buys_computer} = \text{"yes"}) = 0.222 \times 0.444 \times 0.667 \times 0.667 = 0.044$$

$$P(X|\text{buys_computer} = \text{"no"}) = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$$

$$P(X|C_i) * P(C_i) : P(X|\text{buys_computer} = \text{"yes"}) * P(\text{buys_computer} = \text{"yes"}) = 0.028$$

$$P(X|\text{buys_computer} = \text{"no"}) * P(\text{buys_computer} = \text{"no"}) = 0.007$$

Therefore, X belongs to class ("buys_computer = yes")

Avoiding the 0-Probability Problem

- Naïve Bayesian prediction requires each conditional prob. be non-zero. Otherwise, the predicted prob. will be zero

$$P(X | C_i) = \prod_{k=1}^n P(x_k | C_i)$$

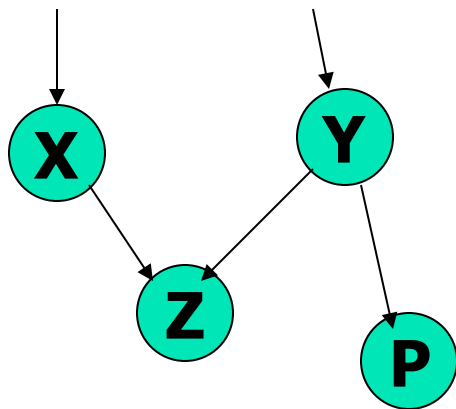
- Ex. Suppose a dataset with 1000 tuples, income=low (0), income=medium (990), and income = high (10),
- Use Laplacian correction (or Laplacian estimator)
 - Adding 1 to each case
 - Prob(income = low) = 1/1003
 - Prob(income = medium) = 991/1003
 - Prob(income = high) = 11/1003
 - The “corrected” prob. estimates are close to their “uncorrected” counterparts

Naïve Bayesian Classifier: Comments

- Advantages
 - Easy to implement
 - Good results obtained in most of the cases
- Disadvantages
 - Assumption: class conditional independence, therefore loss of accuracy
 - Practically, dependencies exist among variables
 - E.g., hospitals: patients: Profile: age, family history, etc.
Symptoms: fever, cough etc., Disease: lung cancer, diabetes, etc.
 - Dependencies among these cannot be modeled by Naïve Bayesian Classifier
- How to deal with these dependencies?
 - Bayesian Belief Networks

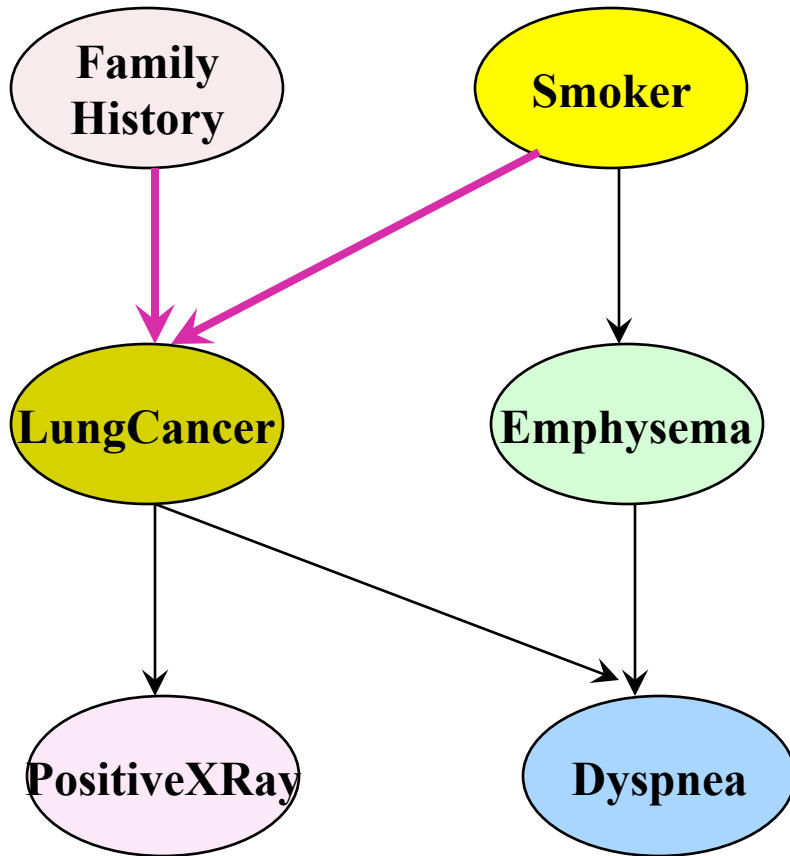
Bayesian Belief Networks

- Bayesian belief network allows a *subset* of the variables conditionally independent
- A graphical model of causal relationships
 - Represents dependency among the variables
 - Gives a specification of joint probability distribution



- Nodes: random variables
- Links: dependency
- X and Y are the parents of Z, and Y is the parent of P
- No dependency between Z and P
- Has no loops or cycles

Bayesian Belief Network: An Example



The **conditional probability table (CPT)** for variable LungCancer:

	(FH, S)	(FH, ~S)	(~FH, S)	(~FH, ~S)
LC	0.8	0.5	0.7	0.1
~LC	0.2	0.5	0.3	0.9

CPT shows the conditional probability for each possible combination of its parents

Derivation of the probability of a particular combination of values of \mathbf{X} , from CPT:


$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | Parents(Y_i))$$

Bayesian Belief Networks

Training Bayesian Networks

- Several scenarios:
 - Given both the network structure and all variables observable: *learn only the CPTs*
 - Network structure known, some hidden variables: *gradient descent* (greedy hill-climbing) method, analogous to neural network learning
 - Network structure unknown, all variables observable: search through the model space to *reconstruct network topology*
 - Unknown structure, all hidden variables: No good algorithms known for this purpose
- Ref. D. Heckerman: Bayesian networks for data mining

Chapter 6. Classification and Prediction

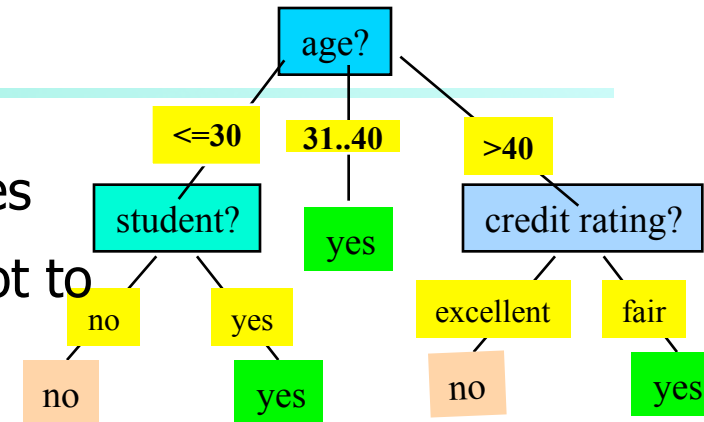
- What is classification? What is prediction?
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Using IF-THEN Rules for Classification

- Represent the knowledge in the form of **IF-THEN** rules
 - R: IF *age* = youth AND *student* = yes THEN *buys_computer* = yes
 - Rule antecedent/precondition vs. rule consequent
- Assessment of a rule: *coverage* and *accuracy*
 - n_{covers} = # of tuples covered by R
 - n_{correct} = # of tuples correctly classified by R
 - $\text{coverage}(R) = n_{\text{covers}} / |D|$ /* D: training data set */
 - $\text{accuracy}(R) = n_{\text{correct}} / n_{\text{covers}}$
- If more than one rule is triggered, need **conflict resolution**
 - Size ordering: assign the highest priority to the triggering rules that has the “toughest” requirement (i.e., with the *most attribute test*)
 - Class-based ordering: decreasing order of *prevalence or misclassification cost per class*
 - Rule-based ordering (**decision list**): rules are organized into one long priority list, according to some measure of rule quality or by experts

Rule Extraction from a Decision Tree

- Rules are easier to understand than large trees
- One rule is created for each path from the root to a leaf
- Each attribute-value pair along a path forms a conjunction: the leaf holds the class prediction
- Rules are mutually exclusive and exhaustive
- Example: Rule extraction from our *buys_computer* decision-tree



IF *age* = young AND *student* = no

THEN *buys_computer* = no

IF *age* = young AND *student* = yes

THEN *buys_computer* = yes

IF *age* = mid-age

THEN *buys_computer* = yes

IF *age* = old AND *credit_rating* = excellent

THEN *buys_computer* = yes

IF *age* = young AND *credit_rating* = fair

THEN *buys_computer* = no

Rule Extraction from the Training Data

- Sequential covering algorithm: Extracts rules directly from training data
- Typical sequential covering algorithms: FOIL, AQ, CN2, RIPPER
- Rules are learned *sequentially*, each for a given class C_i will cover many tuples of C_i but none (or few) of the tuples of other classes
- Steps:
 - Rules are learned one at a time
 - Each time a rule is learned, the tuples covered by the rules are removed
 - The process repeats on the remaining tuples unless *termination condition*, e.g., when no more training examples or when the quality of a rule returned is below a user-specified threshold
- Comp. w. decision-tree induction: learning a set of rules *simultaneously*

How to Learn-One-Rule?

- Star with the most general rule possible: condition = empty
- Adding new attributes by adopting a greedy depth-first strategy
 - Picks the one that most improves the rule quality
- Rule-Quality measures: consider both coverage and accuracy
 - Foil-gain (in FOIL & RIPPER): assesses info_gain by extending condition

$$FOIL_Gain = pos' \times \left(\log_2 \frac{pos'}{pos'+neg'} - \log_2 \frac{pos}{pos+neg} \right)$$

It favors rules that have high accuracy and cover many positive tuples


- Rule pruning based on an independent set of test tuples

$$FOIL_Prune(R) = \frac{pos - neg}{pos + neg}$$

Pos/neg are # of positive/negative tuples covered by R.

If $FOIL_Prune$ is higher for the pruned version of R, prune R

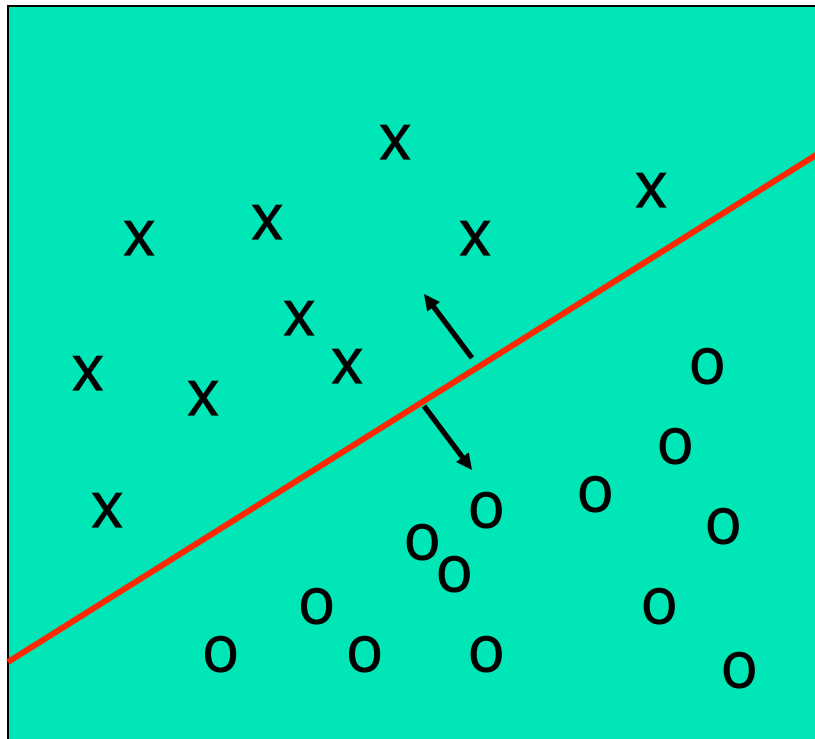
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Classification: A Mathematical Mapping

- **Classification:**
 - predicts categorical class labels
- E.g., Personal homepage classification
 - $x_i = (x_1, x_2, x_3, \dots)$, $y_i = +1$ or -1
 - x_1 : # of a word “homepage”
 - x_2 : # of a word “welcome”
- Mathematically
 - $x \in X = \mathfrak{R}^n$, $y \in Y = \{+1, -1\}$
 - We want a function $f: X \rightarrow Y$

Linear Classification

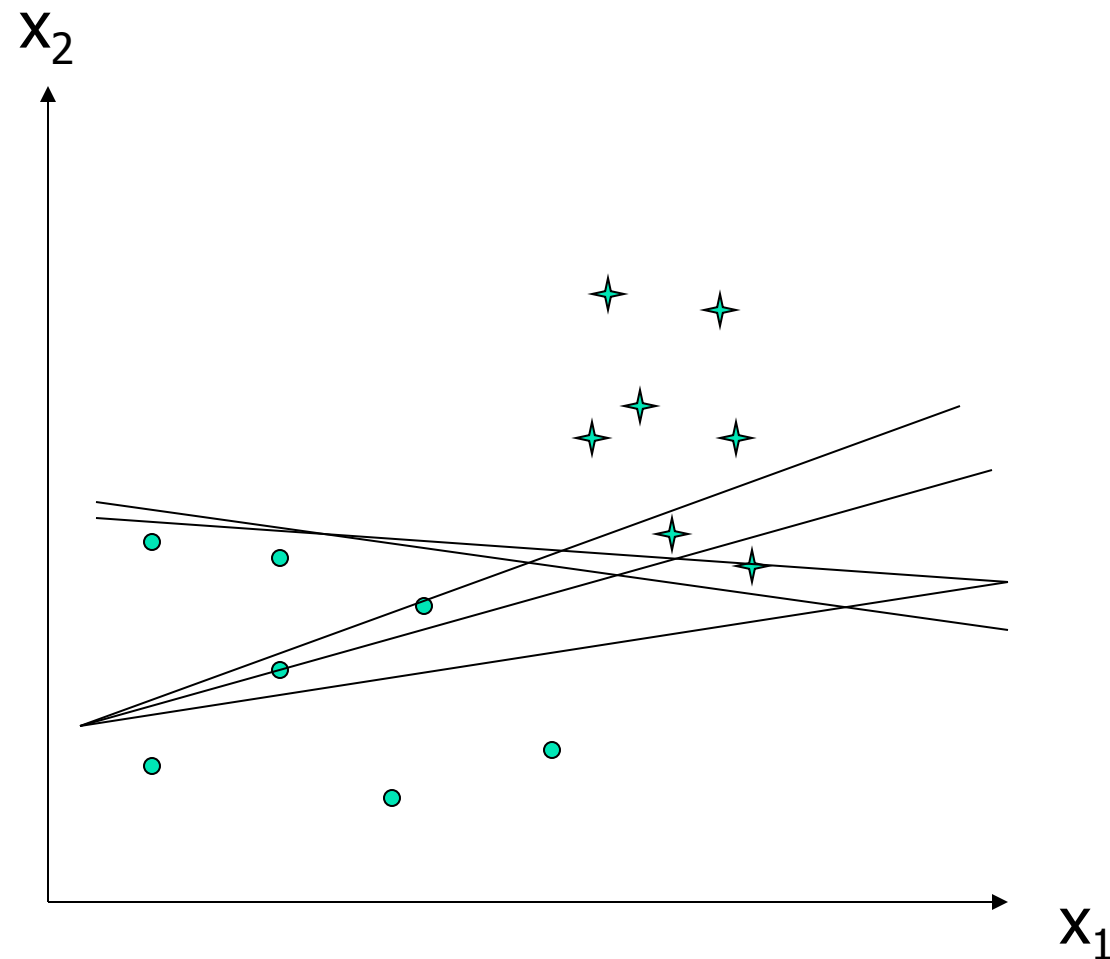


- Binary Classification problem
- The data above the red line belongs to class 'x'
- The data below red line belongs to class 'o'
- Examples: SVM, Perceptron, Probabilistic Classifiers

Discriminative Classifiers

- Advantages
 - prediction accuracy is generally high
 - As compared to Bayesian methods – in general
 - robust, works when training examples contain errors
 - fast evaluation of the learned target function
 - Bayesian networks are normally slow
- Criticism
 - long training time
 - difficult to understand the learned function (weights)
 - Bayesian networks can be used easily for pattern discovery
 - not easy to incorporate domain knowledge
 - Easy in the form of priors on the data or distributions

Perceptron & Winnow



- Vector: x, w

- Scalar: x, y, w

Input: $\{(x_1, y_1), \dots\}$

Output: classification function $f(x)$

$f(x_i) > 0$ for $y_i = +1$

$f(x_i) < 0$ for $y_i = -1$

$f(x) \Rightarrow wx + b = 0$

or $w_1x_1 + w_2x_2 + b = 0$

- Perceptron: update W additively

- Winnow: update W multiplicatively

Classification by Backpropagation

- Backpropagation: A **neural network** learning algorithm
- Started by psychologists and neurobiologists to develop and test computational analogues of neurons
- A neural network: A set of connected input/output units where each connection has a **weight** associated with it
- During the learning phase, the **network learns by adjusting the weights** so as to be able to predict the correct class label of the input tuples
- Also referred to as **connectionist learning** due to the connections between units

Neural Network as a Classifier

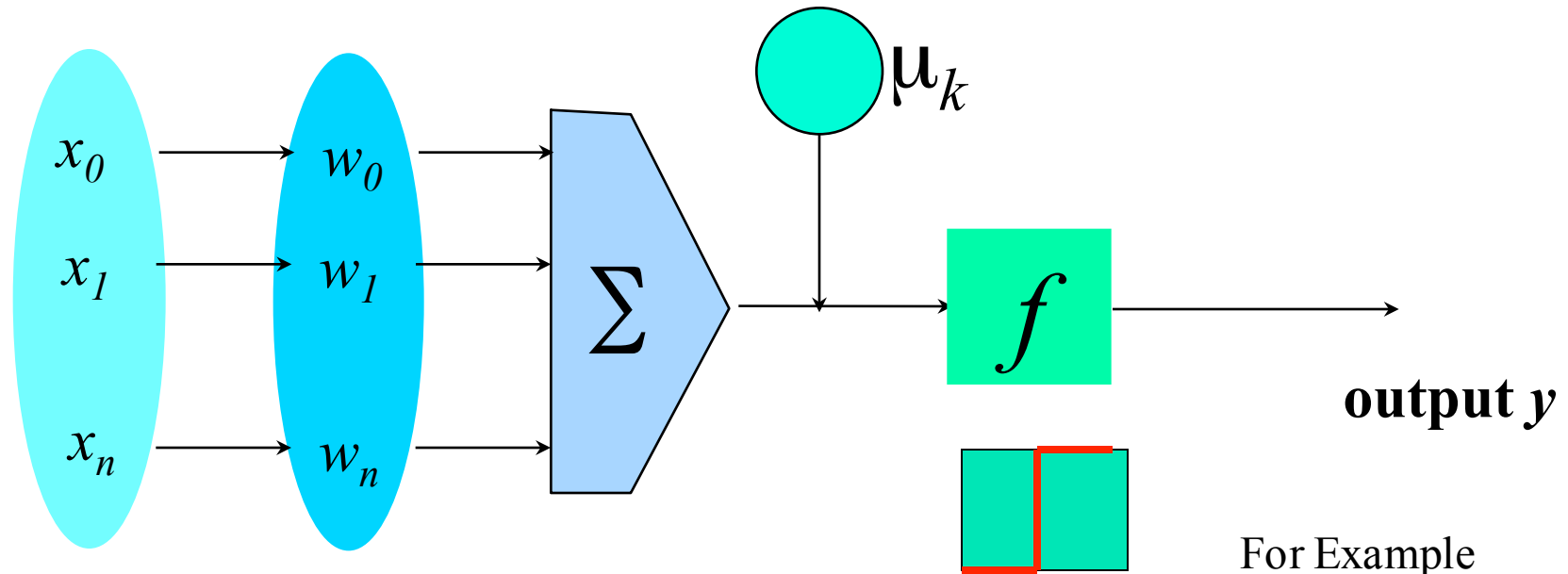
■ Weakness

- Long training time
- Require a number of parameters typically best determined empirically, e.g., the network topology or "structure."
- Poor interpretability: Difficult to interpret the symbolic meaning behind the learned weights and of "hidden units" in the network

■ Strength

- High tolerance to noisy data
- Ability to classify untrained patterns
- Well-suited for continuous-valued inputs and outputs
- Successful on a wide array of real-world data
- Algorithms are inherently parallel
- Techniques have recently been developed for the extraction of rules from trained neural networks

A Neuron (= a perceptron)



**Input
vector \mathbf{x}**

**weight
vector \mathbf{W}**

**weighted
sum**

**Activation
function**

For Example

$$y = \text{sign}\left(\sum_{i=0}^n w_i x_i + \mu_k\right)$$

- The n -dimensional input vector \mathbf{x} is mapped into variable y by means of the scalar product and a nonlinear function mapping

A Multi-Layer Feed-Forward Neural Network

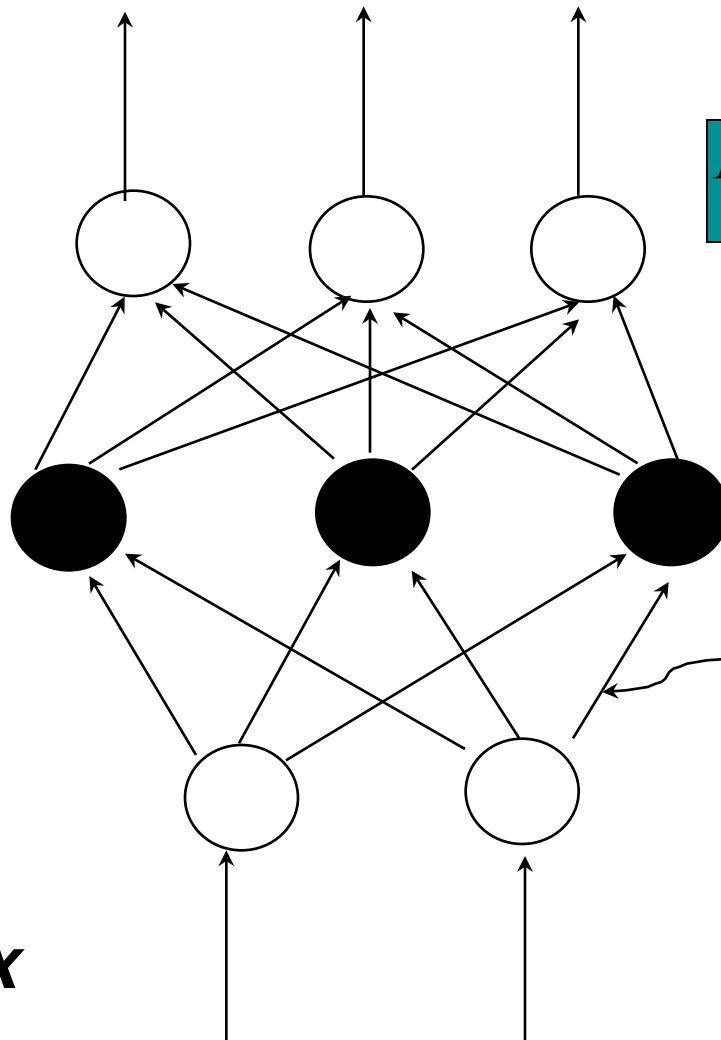
Output vector

Output layer

Hidden layer

Input layer

Input vector: X



$$Err_j = O_j(1 - O_j) \sum_k Err_k w_{jk}$$

$$\theta_j = \theta_j + (l)Err_j$$

$$w_{ij} = w_{ij} + (l)Err_j O_i$$

$$Err_j = O_j(1 - O_j)(T_j - O_j)$$

$$O_j = \frac{1}{1 + e^{-I_j}}$$

$$I_j = \sum_i w_{ij} O_i + \theta_j$$

How A Multi-Layer Neural Network Works?

- The **inputs** to the network correspond to the attributes measured for each training tuple
- Inputs are fed simultaneously into the units making up the **input layer**
- They are then weighted and fed simultaneously to a **hidden layer**
- The number of hidden layers is arbitrary, although usually only one
- The weighted outputs of the last hidden layer are input to units making up the **output layer**, which emits the network's prediction
- The network is **feed-forward** in that none of the weights cycles back to an input unit or to an output unit of a previous layer
- From a statistical point of view, networks perform **nonlinear regression**: Given enough hidden units and enough training samples, they can closely approximate any function

Defining a Network Topology

- First decide the **network topology**: # of units in the *input layer*, # of *hidden layers* (if > 1), # of units in *each hidden layer*, and # of units in the *output layer*
- Normalizing the input values for each attribute measured in the training tuples to [0.0—1.0]
- One **input** unit per domain value, each initialized to 0
- **Output**, if for classification and more than two classes, one output unit per class is used
- Once a network has been trained and its accuracy is **unacceptable**, repeat the training process with a *different network topology* or a *different set of initial weights*


Backpropagation

- Iteratively process a set of training tuples & compare the network's prediction with the actual known target value
- For each training tuple, the weights are modified to **minimize the mean squared error** between the network's prediction and the actual target value
- Modifications are made in the “**backwards**” direction: from the output layer, through each hidden layer down to the first hidden layer, hence “**backpropagation**”
- Steps
 - Initialize weights (to small random #s) and biases in the network
 - Propagate the inputs forward (by applying activation function)
 - Backpropagate the error (by updating weights and biases)
 - Terminating condition (when error is very small, etc.)

Backpropagation and Interpretability

- Efficiency of backpropagation: Each epoch (one iteration through the training set) takes $O(|D| * w)$, with $|D|$ tuples and w weights, but # of epochs can be exponential to n , the number of inputs, in the worst case
- Rule extraction from networks: network pruning
 - Simplify the network structure by removing weighted links that have the least effect on the trained network
 - Then perform link, unit, or activation value clustering
 - The set of input and activation values are studied to derive rules describing the relationship between the input and hidden unit layers
- Sensitivity analysis: assess the impact that a given input variable has on a network output. The knowledge gained from this analysis can be represented in rules

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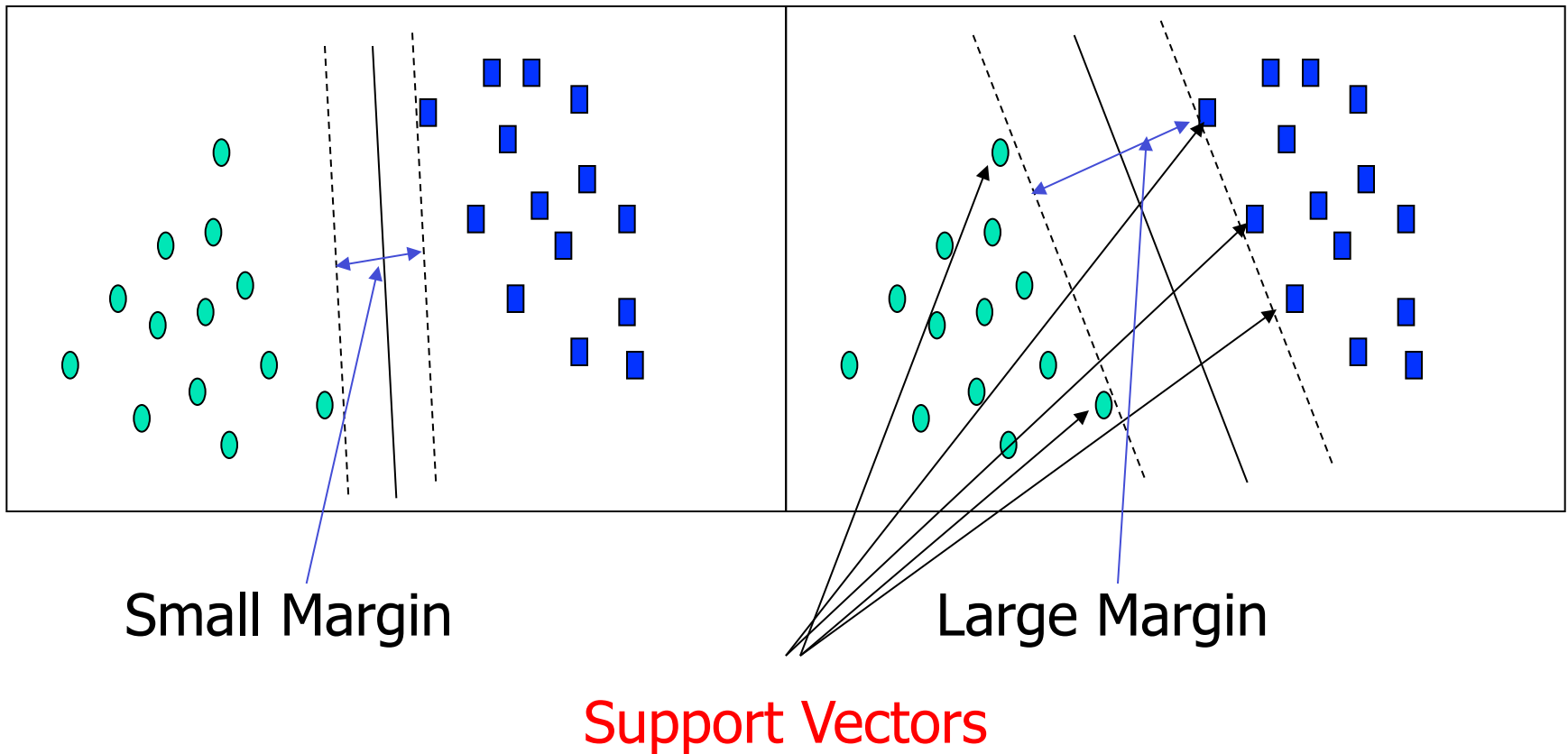
SVM—Support Vector Machines

- A new classification method for both linear and nonlinear data
- It uses a nonlinear mapping to transform the original training data into a higher dimension
- With the new dimension, it searches for the linear optimal separating hyperplane (i.e., “decision boundary”)
- With an appropriate nonlinear mapping to a sufficiently high dimension, data from two classes can always be separated by a hyperplane
- SVM finds this hyperplane using support vectors (“essential” training tuples) and margins (defined by the support vectors)

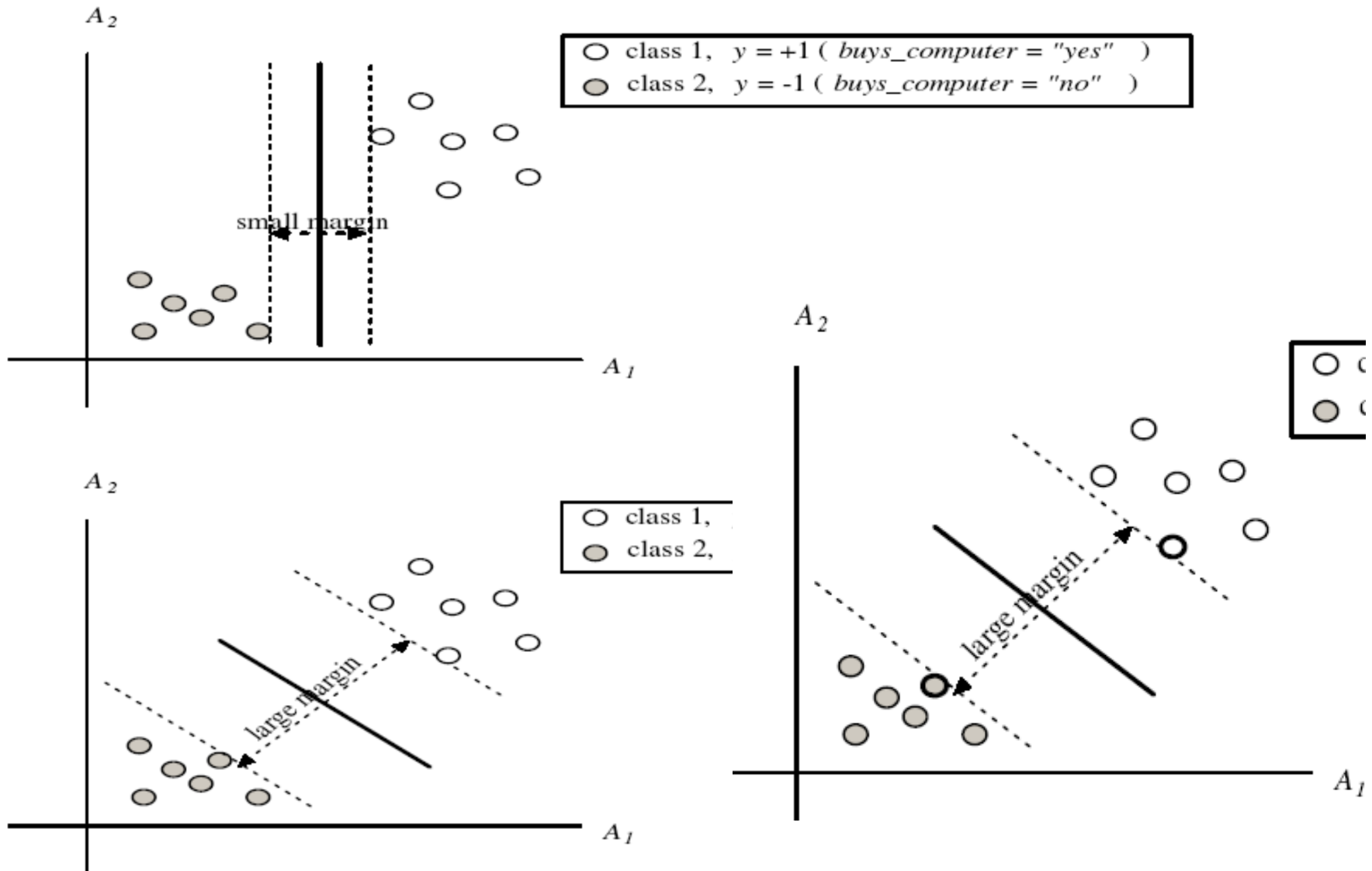
SVM—History and Applications

- Vapnik and colleagues (1992)—groundwork from Vapnik & Chervonenkis’ statistical learning theory in 1960s
- Features: training can be slow but accuracy is high owing to their ability to model complex nonlinear decision boundaries (margin maximization)
- Used both for classification and prediction
- Applications:
 - handwritten digit recognition, object recognition, speaker identification, benchmarking time-series prediction tests

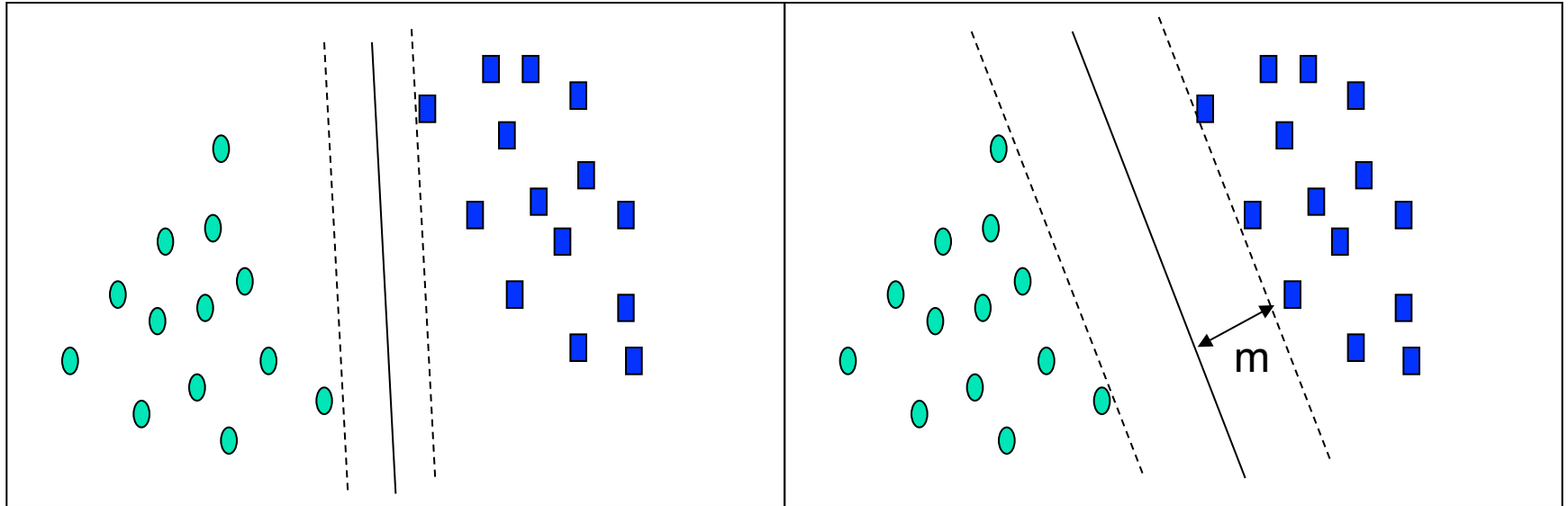
SVM—General Philosophy



SVM—Margins and Support Vectors



SVM—When Data Is Linearly Separable



Let data D be $(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_{|D|}, y_{|D|})$, where \mathbf{x}_i is the set of training tuples associated with the class labels y_i

There are infinite lines (hyperplanes) separating the two classes but we want to find the best one (the one that minimizes classification error on unseen data)

SVM searches for the hyperplane with the largest margin, i.e., **maximum marginal hyperplane** (MMH)

SVM—Linearly Separable

- A separating hyperplane can be written as

$$\mathbf{W} \bullet \mathbf{X} + b = 0$$

where $\mathbf{W} = \{w_1, w_2, \dots, w_n\}$ is a weight vector and b a scalar (bias)

- For 2-D it can be written as

$$w_0 + w_1 x_1 + w_2 x_2 = 0$$

- The hyperplane defining the sides of the margin:

$$H_1: w_0 + w_1 x_1 + w_2 x_2 \geq 1 \quad \text{for } y_i = +1, \text{ and}$$

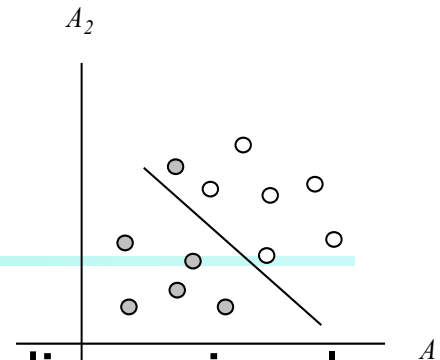
$$H_2: w_0 + w_1 x_1 + w_2 x_2 \leq -1 \quad \text{for } y_i = -1$$

- Any training tuples that fall on hyperplanes H_1 or H_2 (i.e., the sides defining the margin) are **support vectors**
- This becomes a **constrained (convex) quadratic optimization** problem: Quadratic objective function and linear constraints → *Quadratic Programming (QP)* → Lagrangian multipliers

Why Is SVM Effective on High Dimensional Data?

- The complexity of trained classifier is characterized by the # of support vectors rather than the dimensionality of the data
- The support vectors are the essential or critical training examples — they lie closest to the decision boundary (MMH)
- If all other training examples are removed and the training is repeated, the same separating hyperplane would be found
- The number of support vectors found can be used to compute an (upper) bound on the expected error rate of the SVM classifier, which is independent of the data dimensionality
- Thus, an SVM with a small number of support vectors can have good generalization, even when the dimensionality of the data is high

SVM—Linearly Inseparable



- Transform the original input data into a higher dimensional space

Example 6.8 Nonlinear transformation of original input data into a higher dimensional space. Consider the following example. A 3D input vector $\mathbf{X} = (x_1, x_2, x_3)$ is mapped into a 6D space Z using the mappings $\phi_1(\mathbf{X}) = x_1, \phi_2(\mathbf{X}) = x_2, \phi_3(\mathbf{X}) = x_3, \phi_4(\mathbf{X}) = (x_1)^2, \phi_5(\mathbf{X}) = x_1x_2$, and $\phi_6(\mathbf{X}) = x_1x_3$. A decision hyperplane in the new space is $d(\mathbf{Z}) = \mathbf{WZ} + b$, where \mathbf{W} and \mathbf{Z} are vectors. This is linear. We solve for \mathbf{W} and b and then substitute back so that we see that the linear decision hyperplane in the new (\mathbf{Z}) space corresponds to a nonlinear second order polynomial in the original 3-D input space,

$$\begin{aligned} d(\mathbf{Z}) &= w_1x_1 + w_2x_2 + w_3x_3 + w_4(x_1)^2 + w_5x_1x_2 + w_6x_1x_3 + b \\ &= w_1z_1 + w_2z_2 + w_3z_3 + w_4z_4 + w_5z_5 + w_6z_6 + b \quad \blacksquare \end{aligned}$$

- Search for a linear separating hyperplane in the new space

SVM—Kernel functions

- Instead of computing the dot product on the transformed data tuples, it is mathematically equivalent to instead applying a kernel function $K(\mathbf{X}_i, \mathbf{X}_j)$ to the original data, i.e., $K(\mathbf{X}_i, \mathbf{X}_j) = \Phi(\mathbf{X}_i) \cdot \Phi(\mathbf{X}_j)$
- Typical Kernel Functions

Polynomial kernel of degree h : $K(X_i, X_j) = (X_i \cdot X_j + 1)^h$

Gaussian radial basis function kernel : $K(X_i, X_j) = e^{-\|X_i - X_j\|^2 / 2\sigma^2}$

Sigmoid kernel : $K(X_i, X_j) = \tanh(\kappa X_i \cdot X_j - \delta)$

- SVM can also be used for classifying multiple (> 2) classes and for regression analysis (with additional user parameters)

Scaling SVM by Hierarchical Micro-Clustering

- SVM is not scalable to the number of data objects in terms of training time and memory usage
- “Classifying Large Datasets Using SVMs with Hierarchical Clusters Problem” by Hwanjo Yu, Jiong Yang, Jiawei Han, KDD’ 03
- CB-SVM (Clustering-Based SVM)
 - Given limited amount of system resources (e.g., memory), maximize the SVM performance in terms of accuracy and the training speed
 - Use micro-clustering to effectively reduce the number of points to be considered
 - At deriving support vectors, de-cluster micro-clusters near “candidate vector” to ensure high classification accuracy

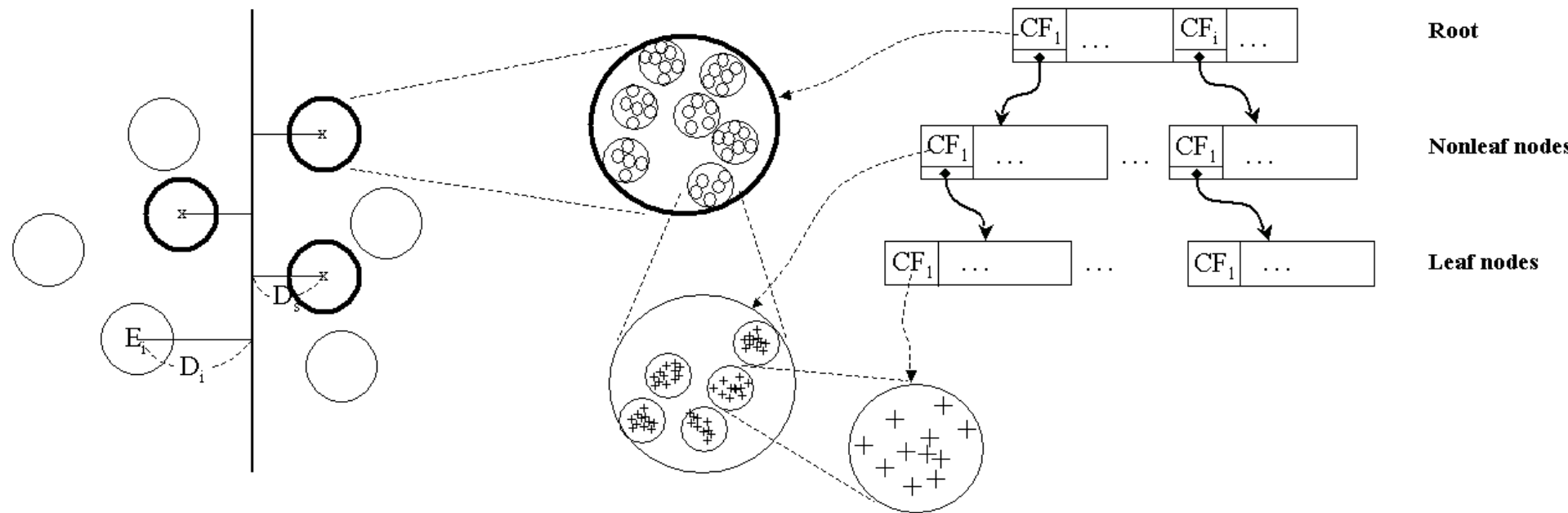
CB-SVM: Clustering-Based SVM

- Training data sets may not even fit in memory
- Read the data set once (minimizing disk access)
 - Construct a statistical summary of the data (i.e., hierarchical clusters) given a limited amount of memory
 - The statistical summary maximizes the benefit of learning SVM
- The summary plays a role in indexing SVMs
- Essence of Micro-clustering (Hierarchical indexing structure)
 - Use micro-cluster hierarchical indexing structure
 - provide finer samples closer to the boundary and coarser samples farther from the boundary
 - Selective de-clustering to ensure high accuracy

CF-Tree: Hierarchical Micro-cluster

Negative clusters

Positive clusters

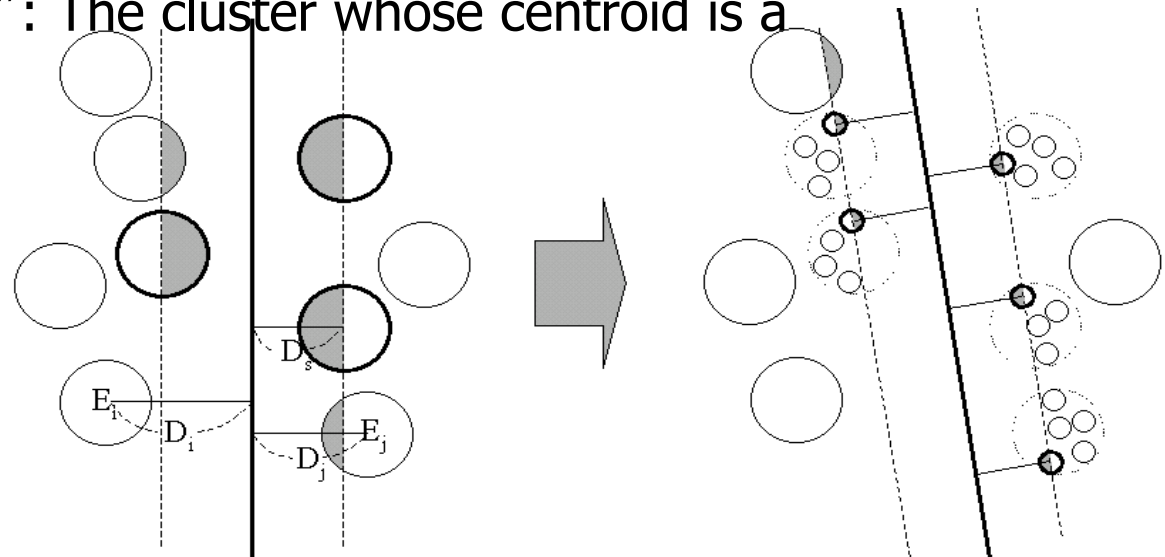


CB-SVM Algorithm: Outline

- Construct two CF-trees from positive and negative data sets independently
 - Need one scan of the data set
- Train an SVM from the centroids of the root entries
- De-cluster the entries near the boundary into the next level
 - The children entries de-clustered from the parent entries are accumulated into the training set with the non-declustered parent entries
- Train an SVM again from the centroids of the entries in the training set
- Repeat until nothing is accumulated

Selective Declustering

- CF tree is a suitable base structure for selective declustering
- De-cluster only the cluster E_i such that
 - $D_i - R_i < D_s$, where D_i is the distance from the boundary to the center point of E_i and R_i is the radius of E_i
 - Decluster only the cluster whose subclusters have possibilities to be the support cluster of the boundary
 - “Support cluster”: The cluster whose centroid is a support vector



Experiment on Synthetic Dataset

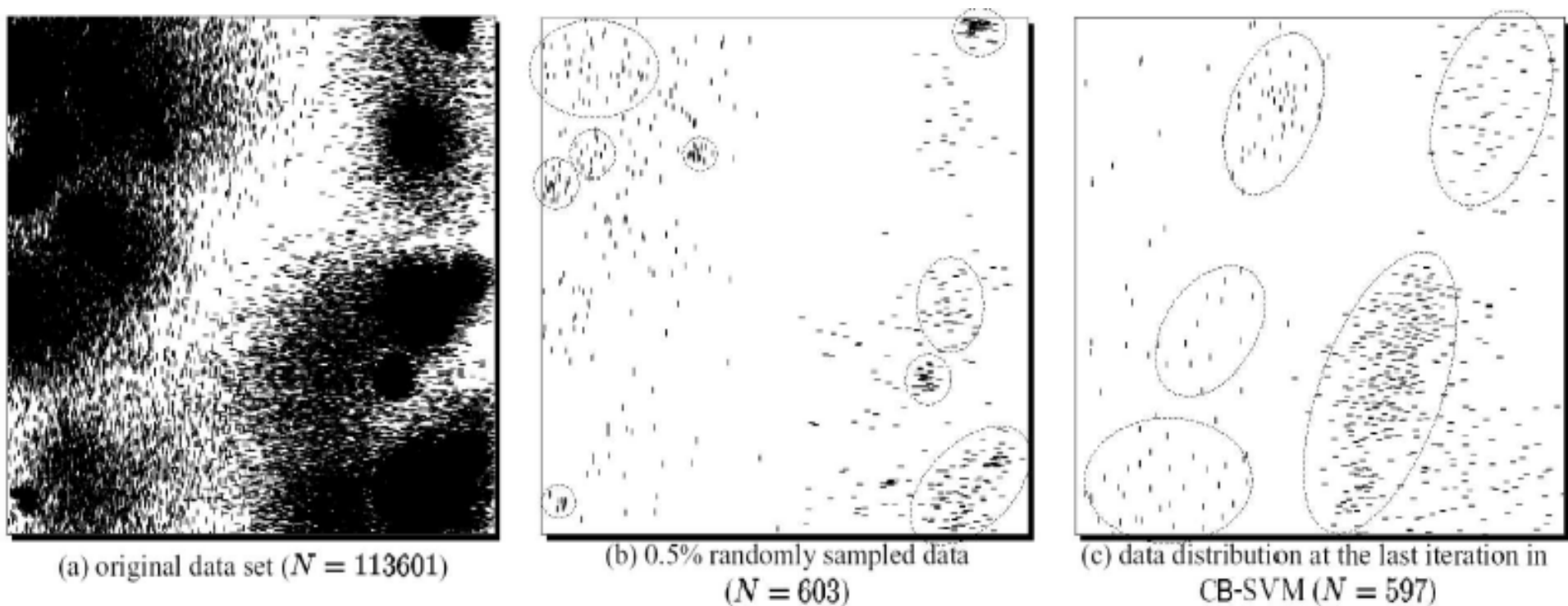


Figure 6: Synthetic data set in a two-dimensional space. ‘+’: positive data; ‘-’: negative data

Experiment on a Large Data Set

S-Rate	# of data	# of errors	T-Time	S-Time
0.0001%	23	6425	0.000114	822.97
0.001%	226	2413	0.000972	825.40
0.01%	2333	1132	0.03	828.61
0.1%	23273	1012	6.287	835.87
1%	230380	1015	1192.793	838.92
5%	1151714	1020	20705.4	842.92
ASVM	307	865	54872.213	
CB-SVM	2893	876	1.639	2528.213

Table 4: Performance results on the very large data set (# of training data = 23066169, # of testing data = 233890). S-Rate: sampling rate; T-Time: training time; S-Time: sampling time; ASVM: selective sampling

SVM vs. Neural Network

■ SVM

- Relatively new concept
- Deterministic algorithm
- Nice Generalization properties
- Hard to learn – learned in batch mode using quadratic programming techniques
- Using kernels can learn very complex functions

■ Neural Network

- Relatively old
- Nondeterministic algorithm
- Generalizes well but doesn't have strong mathematical foundation
- Can easily be learned in incremental fashion
- To learn complex functions—use multilayer perceptron (not that trivial)


SVM Related Links

- SVM Website
 - <http://www.kernel-machines.org/>
- Representative implementations
 - LIBSVM: an efficient implementation of SVM, multi-class classifications, nu-SVM, one-class SVM, including also various interfaces with java, python, etc.
 - SVM-light: simpler but performance is not better than LIBSVM, support only binary classification and only C language
 - SVM-torch: another recent implementation also written in C.

SVM—Introduction Literature

- “Statistical Learning Theory” by Vapnik: extremely hard to understand, containing many errors too.
- C. J. C. Burges.
[A Tutorial on Support Vector Machines for Pattern Recognition.](#)
Knowledge Discovery and Data Mining, 2(2), 1998.
 - Better than the Vapnik’s book, but still written too hard for introduction, and the examples are so not-intuitive
- The book “An Introduction to Support Vector Machines” by N. Cristianini and J. Shawe-Taylor
 - Also written hard for introduction, but the explanation about the mercer’s theorem is better than above literatures
- The neural network book by Haykins

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Associative Classification

- Associative classification
 - Association rules are generated and analyzed for use in classification
 - Search for strong associations between frequent patterns (conjunctions of attribute-value pairs) and class labels
 - Classification: Based on evaluating a set of rules in the form of
$$P_1 \wedge p_2 \dots \wedge p_l \rightarrow "A_{\text{class}} = C" \text{ (conf, sup)}$$
- Why effective?
 - It explores highly confident associations among multiple attributes and may overcome some constraints introduced by decision-tree induction, which considers only one attribute at a time
 - In many studies, associative classification has been found to be more accurate than some traditional classification methods, such as C4.5

Typical Associative Classification Methods

- CBA (Classification By Association: Liu, Hsu & Ma, KDD' 98)
 - Mine association possible rules in the form of
 - Cond-set (a set of attribute-value pairs) → class label
 - Build classifier: Organize rules according to decreasing precedence based on confidence and then support
- CMAR (Classification based on Multiple Association Rules: Li, Han, Pei, ICDM' 01)
 - Classification: Statistical analysis on multiple rules
- CPAR (Classification based on Predictive Association Rules: Yin & Han, SDM' 03)
 - Generation of predictive rules (FOIL-like analysis)
 - High efficiency, accuracy similar to CMAR
- RCBT (Mining top- k covering rule groups for gene expression data, Cong et al. SIGMOD' 05)
 - Explore high-dimensional classification, using top- k rule groups
 - Achieve high classification accuracy and high run-time efficiency

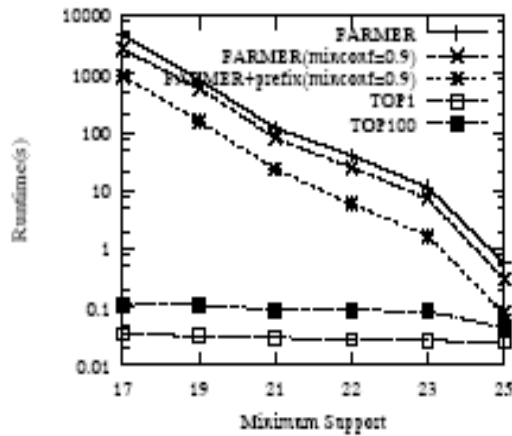
A Closer Look at CMAR

- CMAR (Classification based on Multiple Association Rules: Li, Han, Pei, ICDM' 01)
- Efficiency: Uses an enhanced FP-tree that maintains the distribution of class labels among tuples satisfying each frequent itemset
- Rule pruning whenever a rule is inserted into the tree
 - Given two rules, R_1 and R_2 , if the antecedent of R_1 is more general than that of R_2 and $\text{conf}(R_1) \geq \text{conf}(R_2)$, then R_2 is pruned
 - Prunes rules for which the rule antecedent and class are not positively correlated, based on a χ^2 test of statistical significance
- Classification based on generated/pruned rules
 - If only one rule satisfies tuple X , assign the class label of the rule
 - If a rule set S satisfies X , CMAR
 - divides S into groups according to class labels
 - uses a weighted χ^2 measure to find the strongest group of rules, based on the statistical correlation of rules within a group
 - assigns X the class label of the strongest group

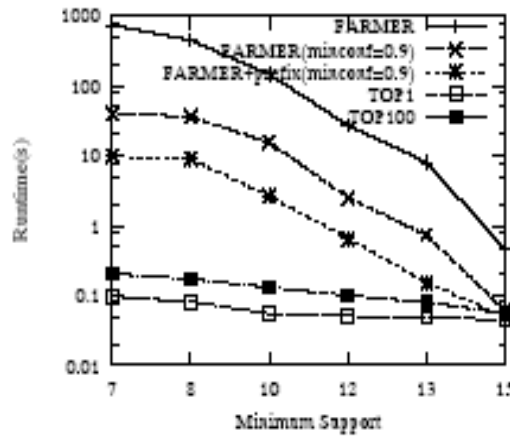
Associative Classification May Achieve High Accuracy and Efficiency (Cong et al. SIGMOD05)

Dataset	RCBT	CBA	IRG Classifier	C4.5 family			SVM
				single tree	bagging	boosting	
AML/ALL (ALL)	91.18%	91.18%	64.71%	91.18%	91.18%	91.18%	97.06%
Lung Cancer(LC)	97.99%	81.88%	89.93%	81.88%	96.64%	81.88%	96.64%
Ovarian Cancer(OC)	97.67%	93.02%	-	97.67%	97.67%	97.67%	97.67%
Prostate Cancer(PC)	97.06%	82.35%	88.24%	26.47%	26.47%	26.47%	79.41%
Average Accuracy	95.98%	87.11%	80.96%	74.3%	77.99%	74.3%	92.70%

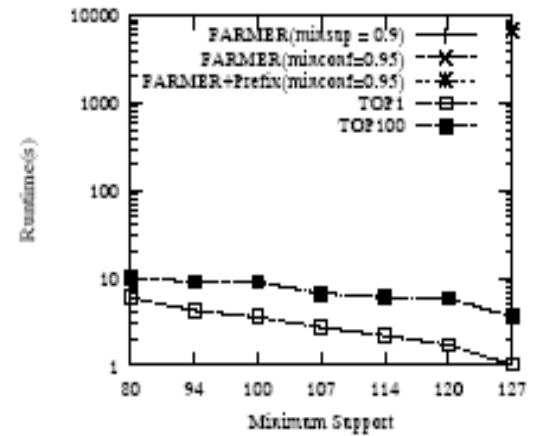
Table 2: Classification Results



(a) ALL-AML leukemia




(b) Lung Cancer



(c) Ovarian Cancer

Chapter 6. Classification and Prediction

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Lazy vs. Eager Learning

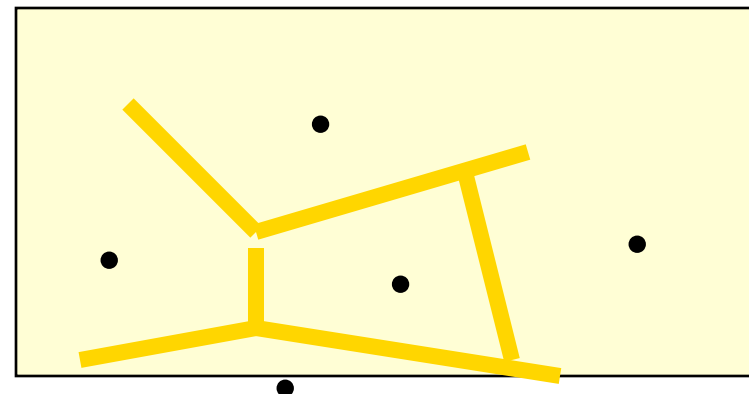
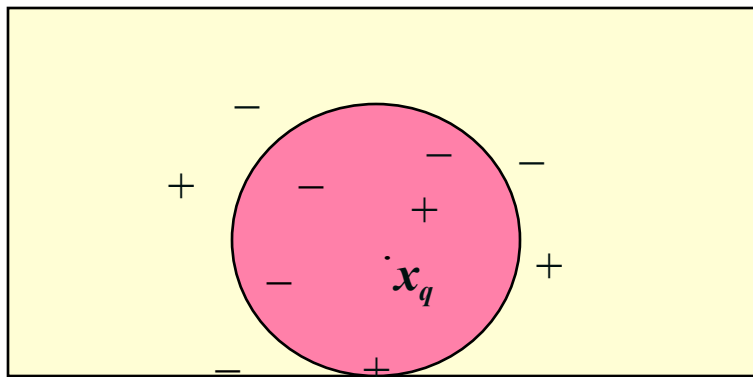
- Lazy vs. eager learning
 - Lazy learning (e.g., instance-based learning): Simply stores training data (or only minor processing) and waits until it is given a test tuple
 - Eager learning (the above discussed methods): Given a set of training set, constructs a classification model before receiving new (e.g., test) data to classify
- Lazy: less time in training but more time in predicting
- Accuracy
 - Lazy method effectively uses a richer hypothesis space since it uses many local linear functions to form its implicit global approximation to the target function
 - Eager: must commit to a single hypothesis that covers the entire instance space

Lazy Learner: Instance-Based Methods

- Instance-based learning:
 - Store training examples and delay the processing (“lazy evaluation”) until a new instance must be classified
- Typical approaches
 - *k*-nearest neighbor approach
 - Instances represented as points in a Euclidean space.
 - Locally weighted regression
 - Constructs local approximation
 - Case-based reasoning
 - Uses symbolic representations and knowledge-based inference

The k -Nearest Neighbor Algorithm

- All instances correspond to points in the n -D space
- The nearest neighbor are defined in terms of Euclidean distance, $\text{dist}(\mathbf{X}_1, \mathbf{X}_2)$
- Target function could be discrete- or real- valued
- For discrete-valued, k -NN returns the most common value among the k training examples nearest to x_q
- Voronoi diagram: the decision surface induced by 1-NN for a typical set of training examples




Discussion on the k -NN Algorithm

- k -NN for real-valued prediction for a given unknown tuple
 - Returns the mean values of the k nearest neighbors
- Distance-weighted nearest neighbor algorithm
 - Weight the contribution of each of the k neighbors according to their distance to the query x_q
 - Give greater weight to closer neighbors $w \equiv \frac{1}{d(x_q, x_i)^2}$
- Robust to noisy data by averaging k -nearest neighbors
- Curse of dimensionality: distance between neighbors could be dominated by irrelevant attributes
 - To overcome it, axes stretch or elimination of the least relevant attributes

Case-Based Reasoning (CBR)

- CBR: Uses a database of problem solutions to solve new problems
- Store symbolic description (tuples or cases)—not points in a Euclidean space
- Applications: Customer-service (product-related diagnosis), legal ruling
- Methodology
 - Instances represented by rich symbolic descriptions (e.g., function graphs)
 - Search for similar cases, multiple retrieved cases may be combined
 - Tight coupling between case retrieval, knowledge-based reasoning, and problem solving
- Challenges
 - Find a good similarity metric
 - Indexing based on syntactic similarity measure, and when failure, backtracking, and adapting to additional cases

Chapter 6. Classification and Prediction

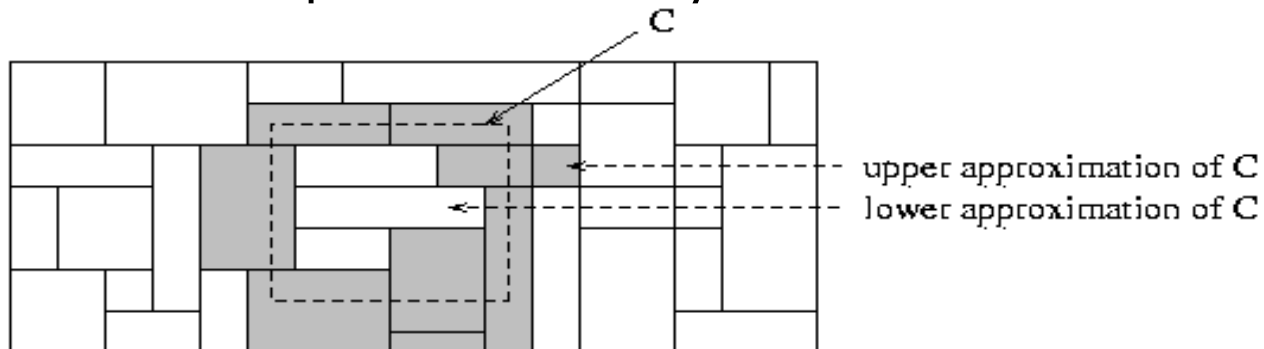
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Genetic Algorithms (GA)

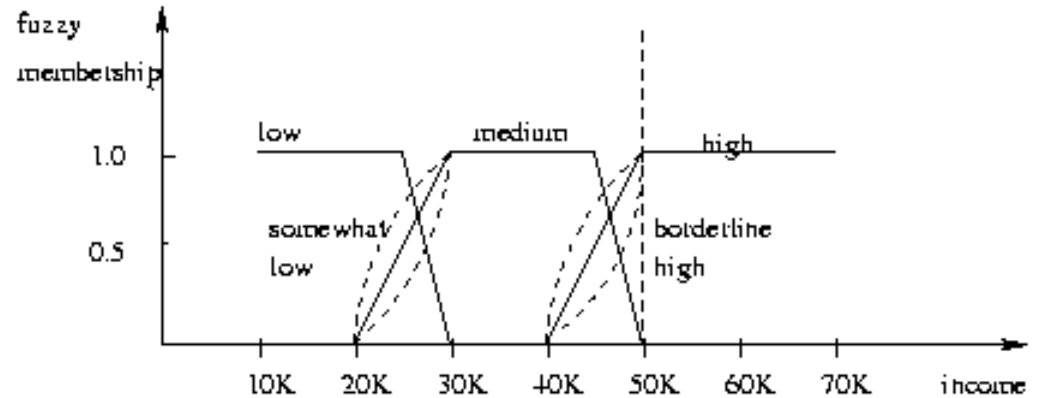
- Genetic Algorithm: based on an analogy to biological evolution
- An initial **population** is created consisting of randomly generated rules
 - Each rule is represented by a string of bits
 - E.g., if A_1 and $\neg A_2$ then C_2 can be encoded as 100
 - If an attribute has $k > 2$ values, k bits can be used
- Based on the notion of survival of the **fittest**, a new population is formed to consist of the fittest rules and their offsprings
- The fitness of a rule is represented by its *classification accuracy* on a set of training examples
- Offsprings are generated by *crossover* and *mutation*
- The process continues until a population P evolves *when each rule in P satisfies a prespecified threshold*
- Slow but easily parallelizable

Rough Set Approach

- Rough sets are used to **approximately** or “**roughly**” define **equivalent classes**
- A rough set for a given class C is approximated by two sets: a **lower approximation** (certain to be in C) and an **upper approximation** (cannot be described as not belonging to C)
- Finding the minimal subsets (**reducts**) of attributes for feature reduction is NP-hard but a **discernibility matrix** (which stores the differences between attribute values for each pair of data tuples) is used to reduce the computation intensity




Fuzzy Set Approaches



- Fuzzy logic uses truth values between 0.0 and 1.0 to represent the degree of membership (such as using **fuzzy membership graph**)
- Attribute values are converted to fuzzy values
 - e.g., income is mapped into the discrete categories {low, medium, high} with fuzzy values calculated
- For a given new sample, more than one fuzzy value may apply
- Each applicable rule contributes a vote for membership in the categories
- Typically, the truth values for each predicted category are summed, and these sums are combined

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What Is Prediction?

- (Numerical) prediction is similar to classification
 - construct a model
 - use model to predict continuous or ordered value for a given input
- Prediction is different from classification
 - Classification refers to predict categorical class label
 - Prediction models continuous-valued functions
- Major method for prediction: regression
 - model the relationship between one or more *independent* or **predictor** variables and a *dependent* or **response** variable
- Regression analysis
 - Linear and multiple regression
 - Non-linear regression
 - Other regression methods: generalized linear model, Poisson regression, log-linear models, regression trees

Linear Regression

- Linear regression: involves a response variable y and a single predictor variable x

$$y = w_0 + w_1 x$$

where w_0 (y-intercept) and w_1 (slope) are regression coefficients

- Method of least squares: estimates the best-fitting straight line

$$w_1 = \frac{\sum_{i=1}^{|D|} (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^{|D|} (x_i - \bar{x})^2} \quad w_0 = \bar{y} - w_1 \bar{x}$$

- Multiple linear regression: involves more than one predictor variable
 - Training data is of the form $(\mathbf{X}_1, y_1), (\mathbf{X}_2, y_2), \dots, (\mathbf{X}_{|D|}, y_{|D|})$
 - Ex. For 2-D data, we may have: $y = w_0 + w_1 x_1 + w_2 x_2$
 - Solvable by extension of least square method or using SAS, S-Plus
 - Many nonlinear functions can be transformed into the above

Nonlinear Regression

- Some nonlinear models can be modeled by a polynomial function
- A polynomial regression model can be transformed into linear regression model. For example,

$$y = w_0 + w_1 x + w_2 x^2 + w_3 x^3$$

convertible to linear with new variables: $x_2 = x^2$, $x_3 = x^3$

$$y = w_0 + w_1 x + w_2 x_2 + w_3 x_3$$

- Other functions, such as power function, can also be transformed to linear model
- Some models are intractable nonlinear (e.g., sum of exponential terms)
 - possible to obtain least square estimates through extensive calculation on more complex formulae

Other Regression-Based Models

- Generalized linear model:
 - Foundation on which linear regression can be applied to modeling categorical response variables
 - Variance of y is a function of the mean value of y , not a constant
 - Logistic regression: models the prob. of some event occurring as a linear function of a set of predictor variables
 - Poisson regression: models the data that exhibit a Poisson distribution
- Log-linear models: (for categorical data)
 - Approximate discrete multidimensional prob. distributions
 - Also useful for data compression and smoothing
- Regression trees and model trees
 - Trees to predict continuous values rather than class labels

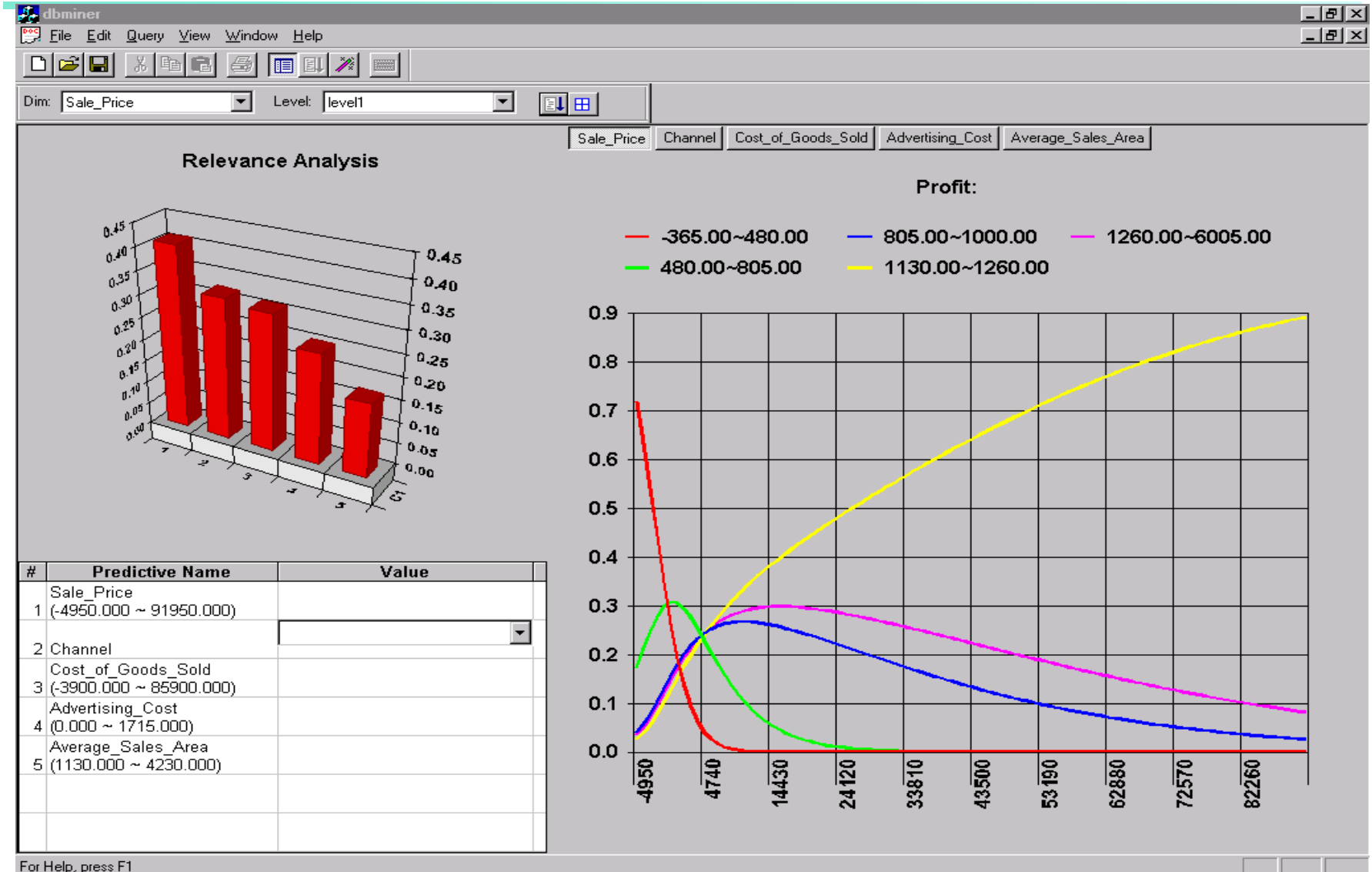
Regression Trees and Model Trees

- Regression tree: proposed in CART system (Breiman et al. 1984)
 - CART: Classification And Regression Trees
 - Each leaf stores a *continuous-valued prediction*
 - It is the *average value of the predicted attribute* for the training tuples that reach the leaf
- Model tree: proposed by Quinlan (1992)
 - Each leaf holds a regression model—a multivariate linear equation for the predicted attribute
 - A more general case than regression tree
- Regression and model trees tend to be more accurate than linear regression when the data are not represented well by a simple linear model

Predictive Modeling in Multidimensional Databases

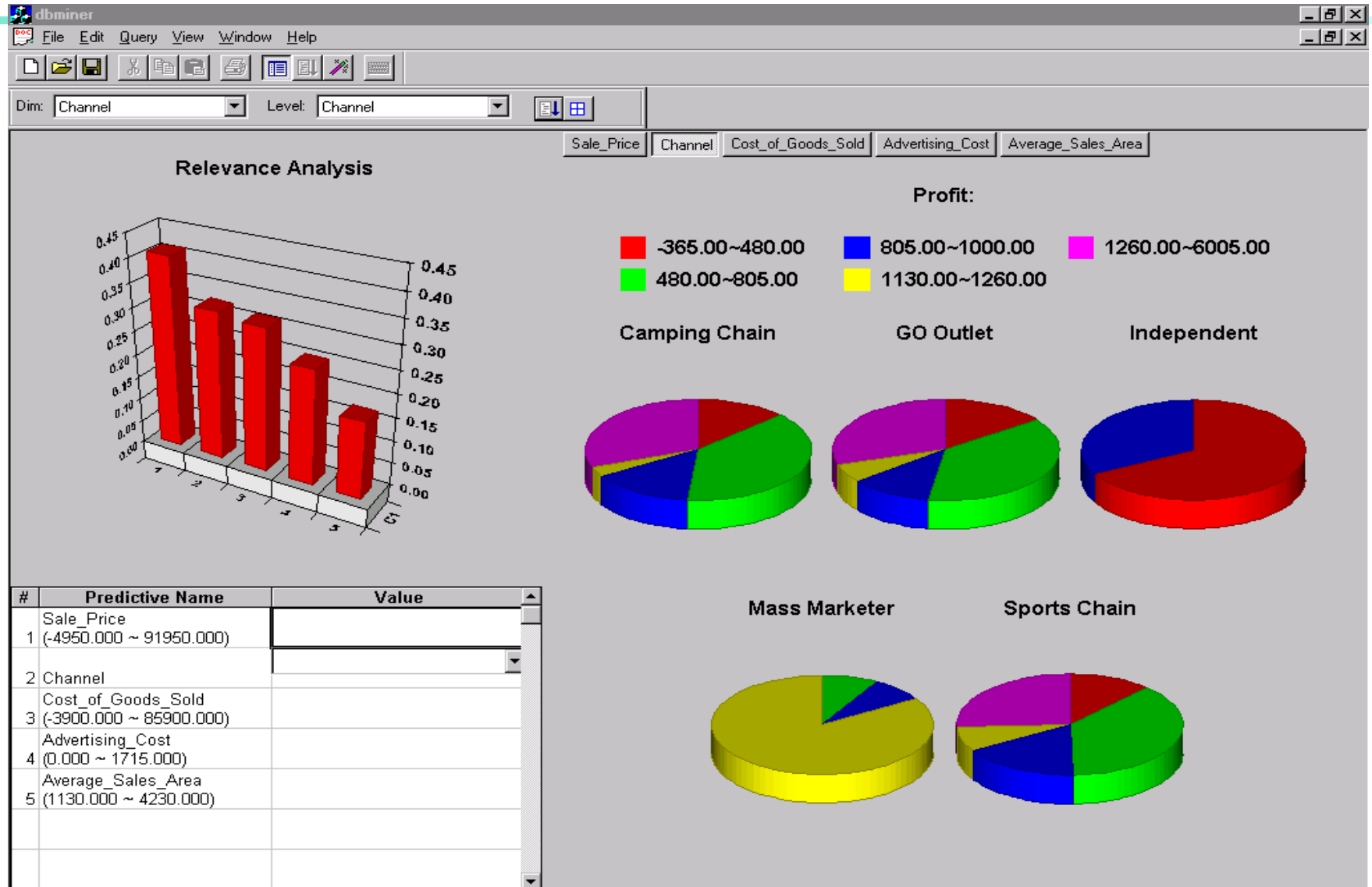
- Predictive modeling: Predict data values or construct generalized linear models based on the database data
- One can only predict value ranges or category distributions
- Method outline:
 - Minimal generalization
 - Attribute relevance analysis
 - Generalized linear model construction
 - Prediction
- Determine the major factors which influence the prediction
 - Data relevance analysis: uncertainty measurement, entropy analysis, expert judgement, etc.
- Multi-level prediction: drill-down and roll-up analysis

Prediction: Numerical Data




For Help, press F1

Prediction: Categorical Data



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Classifier Accuracy Measures

	C_1	C_2
C_1	True positive	False negative
C_2	False positive	True negative

classes	buy_computer = yes	buy_computer = no	total	recognition(%)
buy_computer = yes	6954	46	7000	99.34
buy_computer = no	412	2588	3000	86.27
total	7366	2634	10000	95.52

- Accuracy of a classifier M , $\text{acc}(M)$: percentage of test set tuples that are correctly classified by the model M
 - Error rate (misclassification rate) of $M = 1 - \text{acc}(M)$
 - Given m classes, $CM_{i,j}$ an entry in a **confusion matrix**, indicates # of tuples in class i that are labeled by the classifier as class j
- Alternative accuracy measures (e.g., for cancer diagnosis)
 - sensitivity = t-pos/pos /* true positive recognition rate */
 - specificity = t-neg/neg /* true negative recognition rate */
 - precision = t-pos/(t-pos + f-pos)
 - accuracy = sensitivity * pos/(pos + neg) + specificity * neg/(pos + neg)
 - This model can also be used for cost-benefit analysis

Predictor Error Measures

- Measure predictor accuracy: measure how far off the predicted value is from the actual known value
- **Loss function:** measures the error betw. y_i and the predicted value y_i'
 - Absolute error: $|y_i - y_i'|$
 - Squared error: $(y_i - y_i')^2$
- Test error (generalization error): the average loss over the test set
 - Mean absolute error: $\frac{\sum_{i=1}^d |y_i - y_i'|}{d}$ Mean squared error: $\frac{\sum_{i=1}^d (y_i - y_i')^2}{d}$
 - Relative absolute error: $\frac{\sum_{i=1}^d |y_i - y_i'|}{\sum_{i=1}^d |y_i - \bar{y}|}$ Relative squared error: $\frac{\sum_{i=1}^d (y_i - y_i')^2}{\sum_{i=1}^d (y_i - \bar{y})^2}$

The mean squared-error exaggerates the presence of outliers

Popularly use (square) root mean-square error, similarly, root relative squared error

Evaluating the Accuracy of a Classifier or Predictor (I)


- Holdout method
 - Given data is randomly partitioned into two independent sets
 - Training set (e.g., 2/3) for model construction
 - Test set (e.g., 1/3) for accuracy estimation
 - Random sampling: a variation of holdout
 - Repeat holdout k times, accuracy = avg. of the accuracies obtained
- Cross-validation (k -fold, where $k = 10$ is most popular)
 - Randomly partition the data into k *mutually exclusive* subsets, each approximately equal size
 - At i -th iteration, use D_i as test set and others as training set
 - Leave-one-out: k folds where $k = \#$ of tuples, for small sized data
 - Stratified cross-validation: folds are stratified so that class dist. in each fold is approx. the same as that in the initial data

Evaluating the Accuracy of a Classifier or Predictor (II)

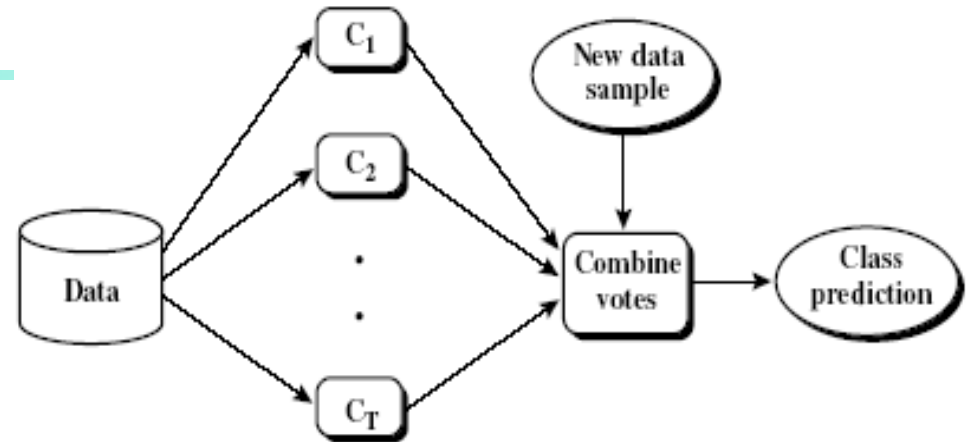
- Bootstrap
 - Works well with small data sets
 - Samples the given training tuples uniformly *with replacement*
 - i.e., each time a tuple is selected, it is equally likely to be selected again and re-added to the training set
- Several bootstrap methods, and a common one is **.632 bootstrap**
 - Suppose we are given a data set of d tuples. The data set is sampled d times, with replacement, resulting in a training set of d samples. The data tuples that did not make it into the training set end up forming the test set. About 63.2% of the original data will end up in the bootstrap, and the remaining 36.8% will form the test set (since $(1 - 1/d)^d \approx e^{-1} = 0.368$)
 - Repeat the sampling procedure k times, overall accuracy of the model:

$$acc(M) = \sum_{i=1}^k (0.632 \times acc(M_i)_{test_set} + 0.368 \times acc(M_i)_{train_set})$$

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Ensemble Methods: Increasing the Accuracy



- Ensemble methods
 - Use a combination of models to increase accuracy
 - Combine a series of k learned models, M_1, M_2, \dots, M_k , with the aim of creating an improved model M^*
- Popular ensemble methods
 - Bagging: averaging the prediction over a collection of classifiers
 - Boosting: weighted vote with a collection of classifiers
 - Ensemble: combining a set of heterogeneous classifiers

Bagging: Bootstrap Aggregation

- Analogy: Diagnosis based on multiple doctors' majority vote
- Training
 - Given a set D of d tuples, at each iteration i , a training set D_i of d tuples is sampled with replacement from D (i.e., bootstrap)
 - A classifier model M_i is learned for each training set D_i
- Classification: classify an unknown sample \mathbf{X}
 - Each classifier M_i returns its class prediction
 - The bagged classifier M^* counts the votes and assigns the class with the most votes to \mathbf{X}
- Prediction: can be applied to the prediction of continuous values by taking the average value of each prediction for a given test tuple
- Accuracy
 - Often significant better than a single classifier derived from D
 - For noise data: not considerably worse, more robust
 - Proved improved accuracy in prediction

Boosting

- Analogy: Consult several doctors, based on a combination of weighted diagnoses—weight assigned based on the previous diagnosis accuracy
- How boosting works?
 - Weights are assigned to each training tuple
 - A series of k classifiers is iteratively learned
 - After a classifier M_i is learned, the weights are updated to allow the subsequent classifier, M_{i+1} , to pay more attention to the training tuples that were misclassified by M_i
 - The final M^* combines the votes of each individual classifier, where the weight of each classifier's vote is a function of its accuracy
- The boosting algorithm can be extended for the prediction of continuous values
- Comparing with bagging: boosting tends to achieve greater accuracy, but it also risks overfitting the model to misclassified data


Adaboost (Freund and Schapire, 1997)

- Given a set of d class-labeled tuples, $(\mathbf{X}_1, y_1), \dots, (\mathbf{X}_d, y_d)$
- Initially, all the weights of tuples are set the same ($1/d$)
- Generate k classifiers in k rounds. At round i ,
 - Tuples from D are sampled (with replacement) to form a training set D_i of the same size
 - Each tuple's chance of being selected is based on its weight
 - A classification model M_i is derived from D_i
 - Its error rate is calculated using D_i as a test set
 - If a tuple is misclassified, its weight is increased, o.w. it is decreased
- Error rate: $err(\mathbf{X}_j)$ is the misclassification error of tuple \mathbf{X}_j . Classifier M_i error rate is the sum of the weights of the misclassified tuples:

$$error(M_i) = \sum_j^d w_j \times err(\mathbf{X}_j)$$

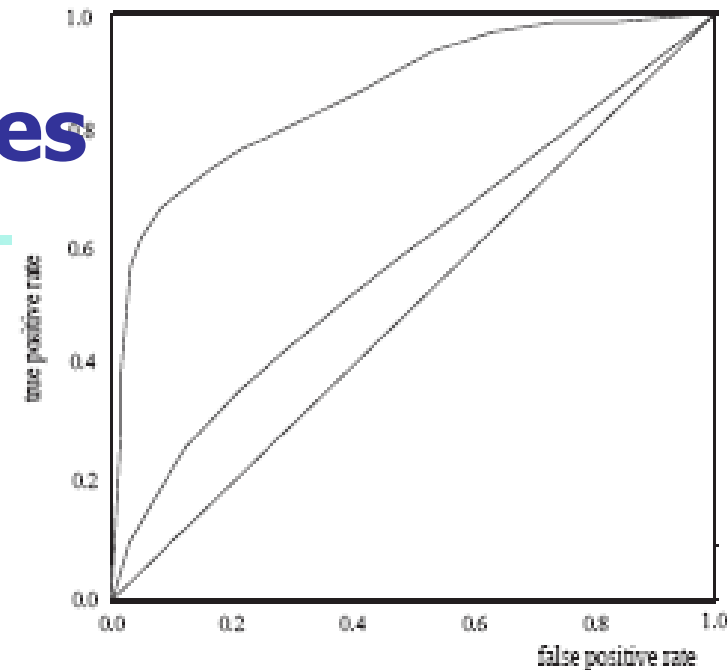
- The weight of classifier M_i 's vote is $\log \frac{1 - error(M_i)}{error(M_i)}$

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Model Selection: ROC Curves

- ROC (Receiver Operating Characteristics) curves: for visual comparison of classification models
- Originated from signal detection theory
- Shows the trade-off between the true positive rate and the false positive rate
- The area under the ROC curve is a measure of the accuracy of the model
- Rank the test tuples in decreasing order: the one that is most likely to belong to the positive class appears at the top of the list
- The closer to the diagonal line (i.e., the closer the area is to 0.5), the less accurate is the model



- Vertical axis represents the true positive rate
- Horizontal axis rep. the false positive rate
- The plot also shows a diagonal line
- A model with perfect accuracy will have an area of 1.0

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Summary (I)

- **Classification** and **prediction** are two forms of data analysis that can be used to extract **models** describing important data classes or to predict future data trends.
- Effective and scalable methods have been developed for **decision trees induction, Naive Bayesian classification, Bayesian belief network, rule-based classifier, Backpropagation, Support Vector Machine (SVM), associative classification, nearest neighbor classifiers, and case-based reasoning**, and other classification methods such as **genetic algorithms, rough set and fuzzy set** approaches.
- **Linear, nonlinear, and generalized linear models of regression** can be used for **prediction**. Many nonlinear problems can be converted to linear problems by performing transformations on the predictor variables. **Regression trees** and **model trees** are also used for prediction.

Summary (II)

- **Stratified k-fold cross-validation** is a recommended method for accuracy estimation. **Bagging** and **boosting** can be used to increase overall accuracy by learning and combining a series of individual models.
- **Significance tests** and **ROC curves** are useful for model selection
- There have been numerous **comparisons of the different classification and prediction methods**, and the matter remains a research topic
- No single method has been found to be superior over all others for all data sets
- Issues such as accuracy, training time, robustness, interpretability, and scalability must be considered and can involve trade-offs, further complicating the quest for an overall superior method

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