

# Modular Neural Networks

**CSE 537 DATA MINING**

**Professor Anita Wasilewska**

# References

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- [http://www.kovan.ceng.metu.edu.tr/~emre/literature/LOMNN/Modular\\_Neural\\_Networks\\_A\\_Survey.pdf](http://www.kovan.ceng.metu.edu.tr/~emre/literature/LOMNN/Modular_Neural_Networks_A_Survey.pdf)
- <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.7.6594&rep=rep1&type=pdf>
- <http://www.teco.edu/~albrecht/neuro/report.pdf>
- [https://en.wikipedia.org/wiki/Modular\\_neural\\_network](https://en.wikipedia.org/wiki/Modular_neural_network)
- A Parallel and Modular Multi-Sieving Neural Network Architecture for Constructive Learning, by Lu et al.
- A modular neural network architecture with concept, by Yi Dinga, Qi Fenga, Tianjiang Wanga, Xian Fub
- <https://www3.cs.stonybrook.edu/~cse634/>

# Overview

- **History** of Neural networks
- **Motivation** behind Neural networks
- **Biological** neural networks
- **Modular** neural networks
- Motivation behind **Modular** Neural Networks
- A paper study on a parallel and fault tolerant **MNN**
- **Benefits**

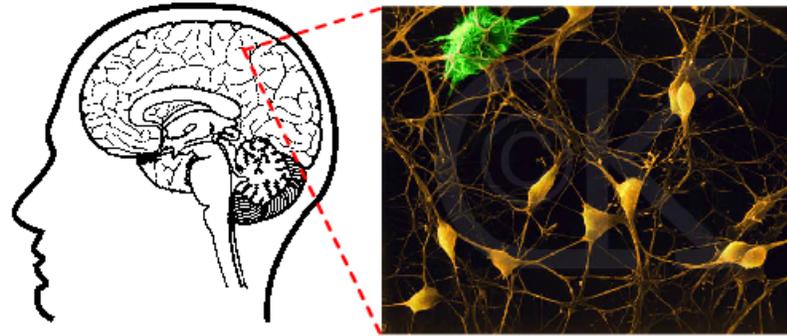
# History of Neural Networks

- In 1943, neurophysiologist Warren McCulloch and mathematician Walter Pitts modelled a simple neural network using electrical circuits
- Nathaniel Rochester from the IBM research laboratories simulated a hypothetical network and failed in his first attempt.

# History of Neural Networks

- In 1959, Bernard Widrow and Marcian Hoff of Stanford developed models called "ADALINE" and "MADALINE."
- ADALINE was developed to recognize binary patterns so that if it was reading streaming bits from a phone line, it could predict the next bit
- MADALINE was the first neural network applied to a real world problem, using an adaptive filter that eliminates echoes on phone lines.
- While the system is as ancient as air traffic control systems, like air traffic control systems, it is still in commercial use !!

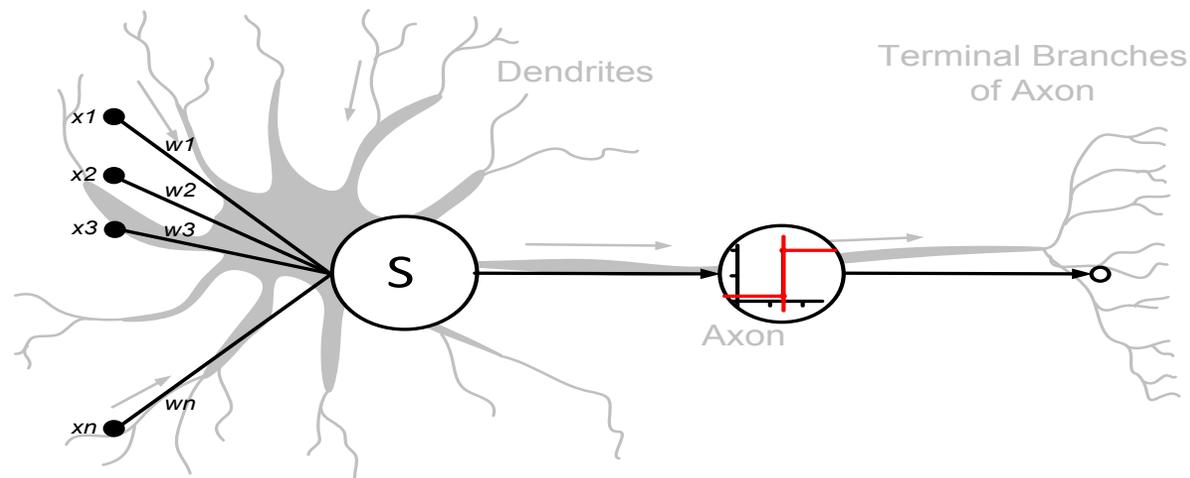
# Biological Neural Network



- Each of the yellow blobs in the picture above are **neuronal cell** bodies: **Soma**
- The lines are the input and output channels: **dendrites** and **axons** which connect them
- Each **neuron** receives **electrochemical inputs** from other **neurons** at the **dendrites**

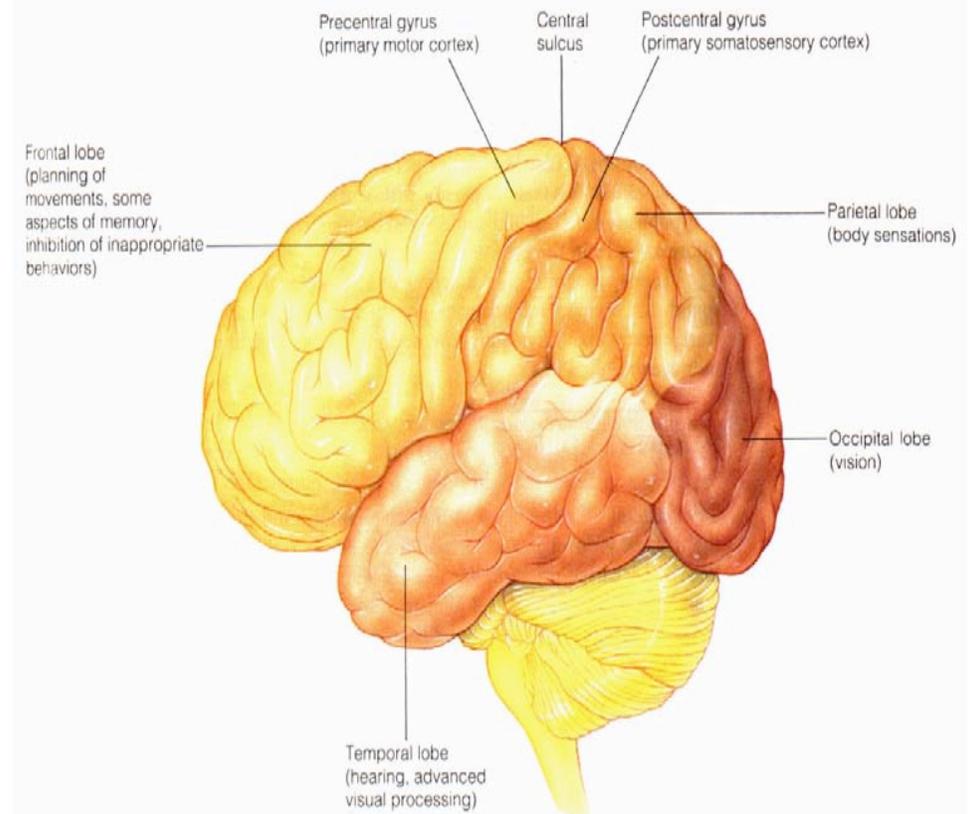
# Biological Neural Network

- If the **sum** of these electrical inputs is sufficiently powerful to **activate** the **neuron**, it **fires** or transmits these signals to other **neurons**
- It is important to note that a **neuron fires only** if the total signal received at the cell body **exceeds** a certain level
- Each **neuron** performs a **weighted sum** of its inputs, and **fires** a binary signal if the **total input** exceeds a certain level
- **This is the model on which artificial neural networks are based**



# Modularity

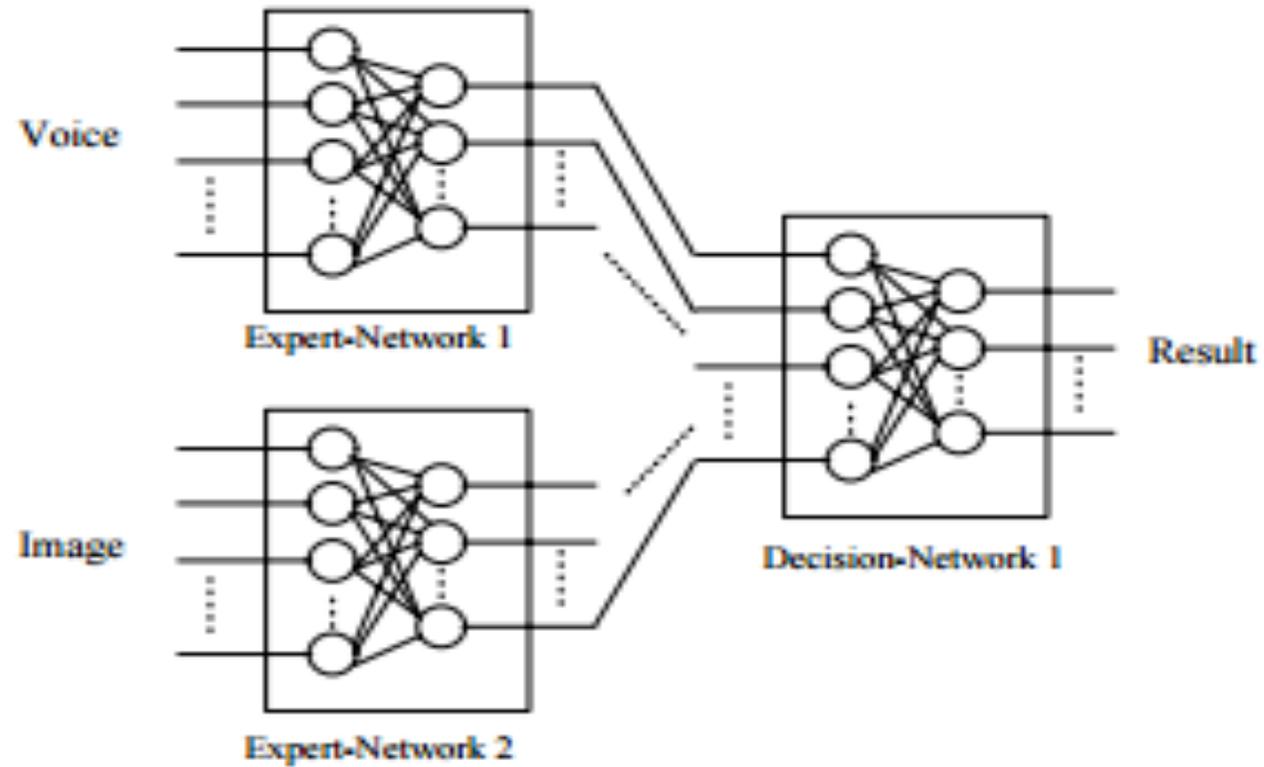
- Biological **modularity** is the first idea which **motivated** many **Modular NN** designs
- **Brain** is **modular** on different spatial scales
- On the **smallest** scale, **synapses** are clustered on **dendrites**
- On the **largest** scale, the **brain** is **composed** of several anatomically and functionally **distinct** areas



# Modularity in Neural Networks

- The most used artificial **neural networks** have a **monolithic** structure and **perform well** on a small input space
- The **complexity increases** and the performance decreases rapidly with a growing **input dimension**
- **Different** models of **NN** combined into a **single system** form **modular neural networks**
- Each **single network** is made into a **module** that can be freely **intermixed** with modules of other types in that system.

# Modular Neural Networks



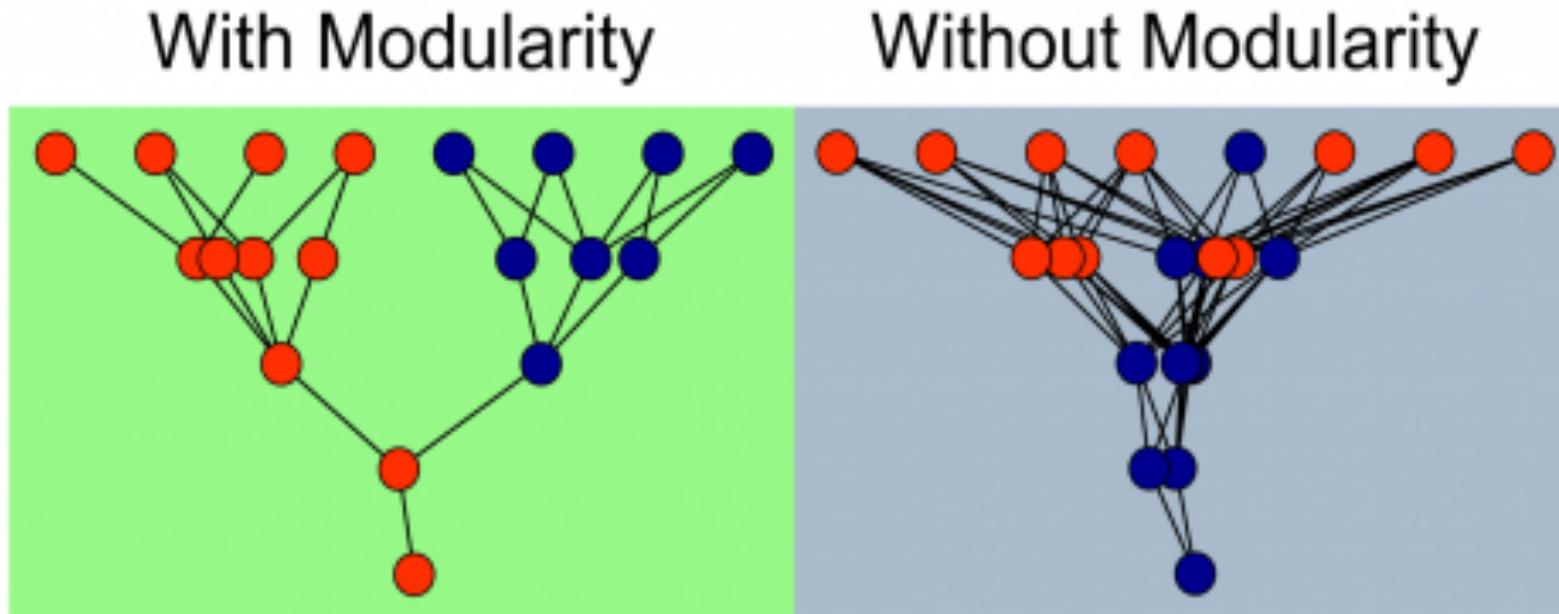
# Modular Neural Networks

- **Modular** (multiple) NN are used for strongly separated architecture
- **Each** of the networks works independently on its own domain
- The single networks are built and trained for its domain and for their specific task
- The final decision is made on the results of the individual networks

# Modular Neural Networks

- The **decision system** can be implemented by a logical **majority vote** function, another **neural network** or a rule based **expert system** may be employed
- The **individual network** is trained on its **domain** only
- The **output** by a **single network** is according to its **specific input**
-

# Modular Neural Networks



One of the networks is trained to **identify a person by voice** while the other network is trained to **identify the person by vision**

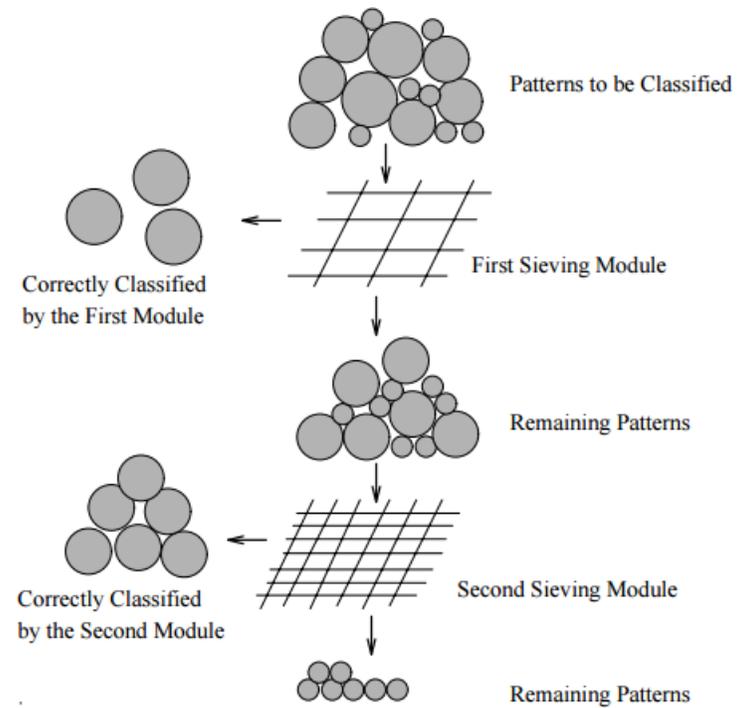
# Modular Neural Networks

- **Modular** neural network **architecture** builds a **bigger network** by using **modules** as **building blocks**
- The **architecture** of a **single** module is simpler and the **sub-networks** are **smaller** than a **monolithic** network.
- Due to the **structural modifications** the **task** the **module** has to learn is in general **easier** than the **whole task** of the network

# Modular Neural Networks

- The modules are **independent** to a certain level which **allows** the system to work in **parallel**
- For this **modular approach** it is always necessary to have a **control system** to **enable** the modules to work **together** in a useful way

# Modular Multi-Sieving Neural Network Architecture



# Modular Multi-Sieving Neural Network Architecture

- The **patterns** are **classified** by this **algorithm** on different **levels**
- 
- In the **first level** , a very **rough sieve**, some patterns may be
- recognized correctly while others will not
- The **correctly classified** samples are **taken out** of the **training set**
  
- The **next level** , a **less rough sieve**, is only **trained** on the
- remaining ones
- **After** the **training** of this level the **correctly recognized** patterns
- are **removed** from the **training set**.

# Modular Multi-Sieving Neural Network Architecture

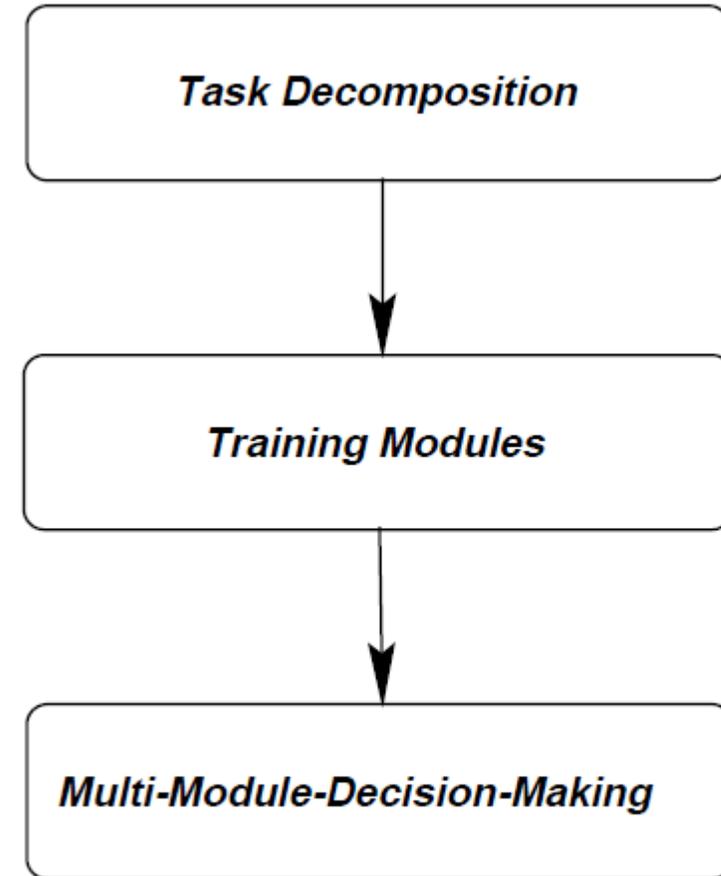
- The remaining **patterns** form the **training set** for the **next level**
- This **process** is **repeated until** all patterns are **classified correctly**
- 
- **Each level** of learning , **each sieve generates** a neural network
- with the **ability** to **recognize a subset** of the original **training set**
- 
- These **networks** called **sieving modules** face a **simpler recognition** task than the **whole problem**

# Motivations for Modular Neural Network

- **Biological motivations :**
  - **Modularity, Functional specialization concept, Fault tolerance, scalability**
- **Psychological motivations**
  - **Learning in stages,**
  - **Decomposing tasks**
    - A way to cope NP-completeness, some papers used MNN to solve travelling salesman problem
- **Hardware motivations**
  - Hardware reaching theoretical limits, need for speed and less memory structures
- **Computational motivations**
  - improves the speed of learning by reducing the effect of conflicting training information (or crosstalk). Crosstalk degrades the ability of the network to perform correctly for a group of patterns.

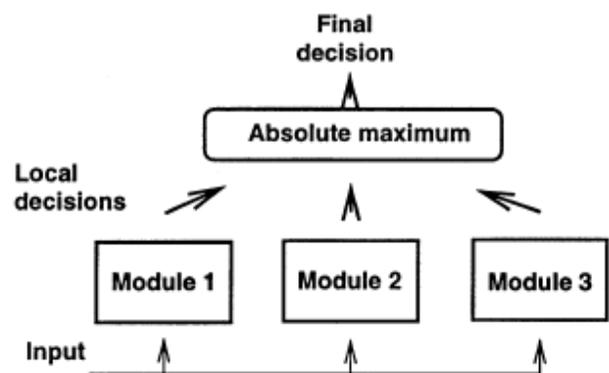
# MNN Design stages

- **Efficiency**
  - **multimodule decision-making** strategy has to take part in order to **integrate** the different **local decisions** (at the modular level) into a **global one**
- **Reasonable balance**
- between **sub-tasks simplification** and decision-making **efficiency**
  - **sub-tasks** as simple as possible
  - give the **multimodule decision-making strategy** enough information

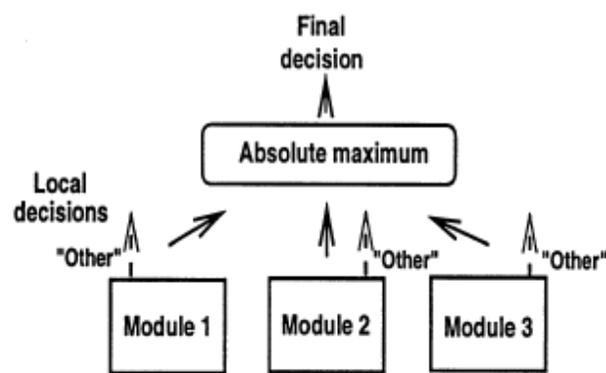


The general three main stages for designing MNN.

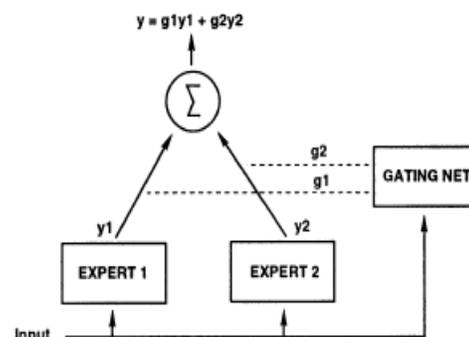
# MNN Architectures



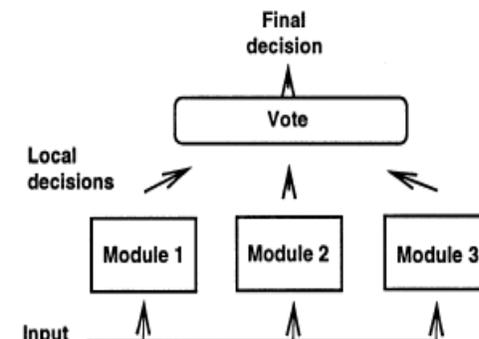
Decoupled modules



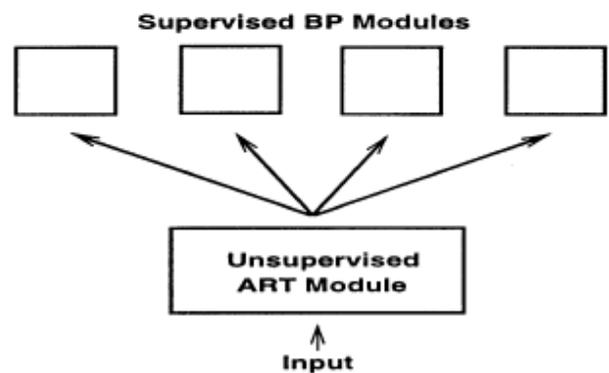
Other-o/p model



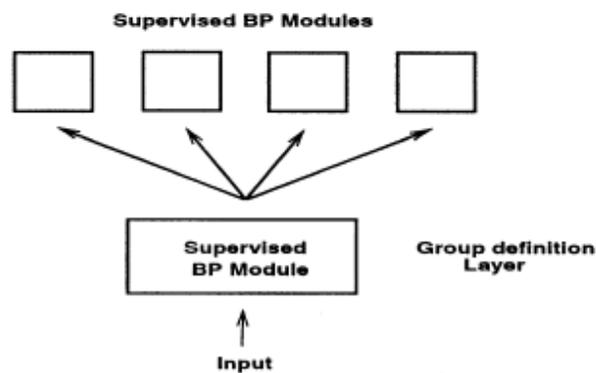
Multiple experts



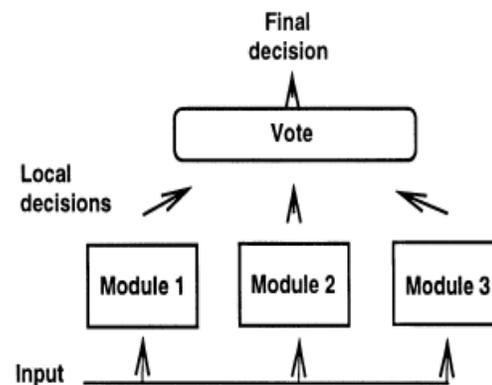
Ensemble (majority vote)



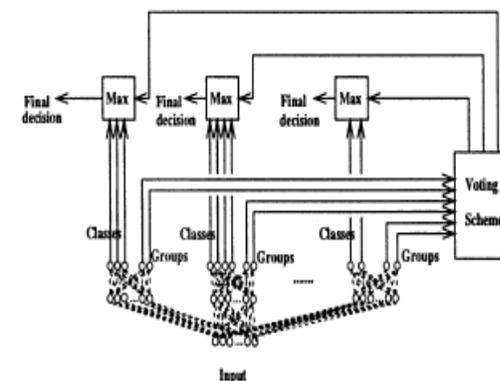
ART-BP model



Hierarchical modules



Ensemble (average vote)



Cooperative MNN

Eight of the most common MNN architectures.

# Research Paper

## **A modular neural network architecture with concept**

Yi Ding, Qi Feng, Tianjiang Wang, Xian Fu

**Journal of Neurocomputing**

Volume 125, February, 2014

Pages 3-6

Elsevier Science Publishers B. V. Amsterdam, The Netherlands

- **Aim:** Develop a parallel and fault tolerant MNN.
- **Motivation:** Human Nervous system.

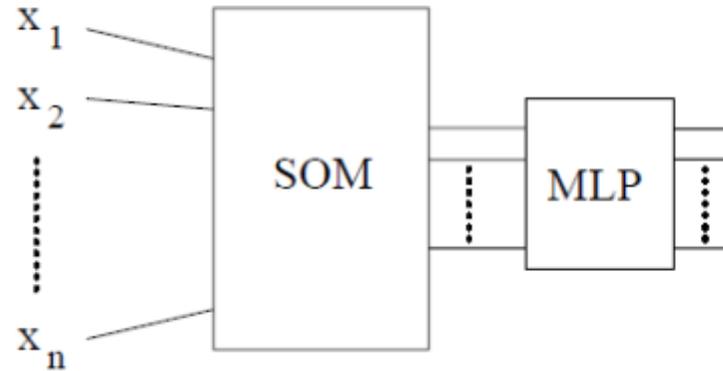
# Evolution of the Model

- Is the network **homogenous** or **heterogeneous**:  
Are all modules of **one type** or are there **different types** of modules used
- What **type of architecture** is used for the modules:  
**MLP, LNN, SOM, ART**
- How are the modules **interconnected**:  
Are only **feedforward connections** used, are **recurrent connections** allowed, are connections only made from **one layer to next**
- What is the **general network structure**:  
has the network a **single** layer or **n layers**

# Evolution of the Model

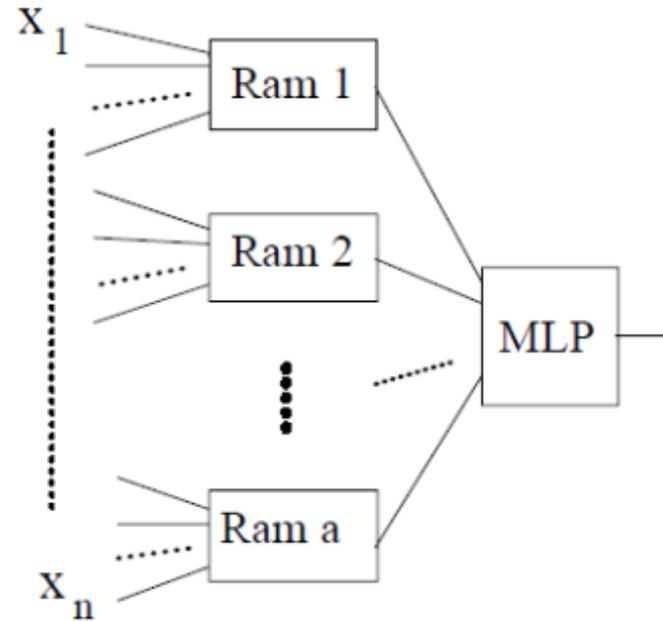
- How are the **inputs connected** to the network:  
Are the inputs connected to **all** modules **overlapping** or **only to one** module non-overlapping
- What **training algorithm** is used for the modules  
Is a **supervised** or **unsupervised** learning method used
- How is **learning organized** for the whole network:
  - Does the **network learn** in **stages**?
  - Is **noise** used during the training?

# Evolution of the Model



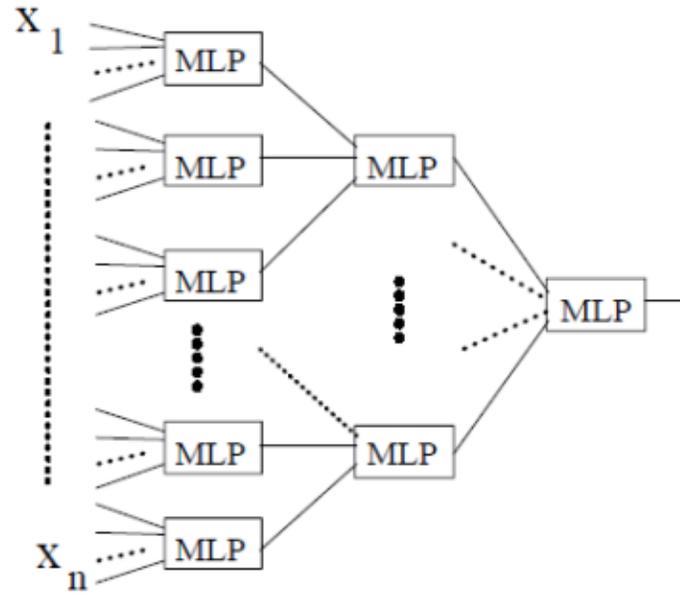
- A **heterogeneous architecture** consisting of **two modules**
- One is a self-organizing map SOM and is used to reduce the input dimension the other one is a multilayer Perceptron that works on the reduced input space

# Evolution of the Model



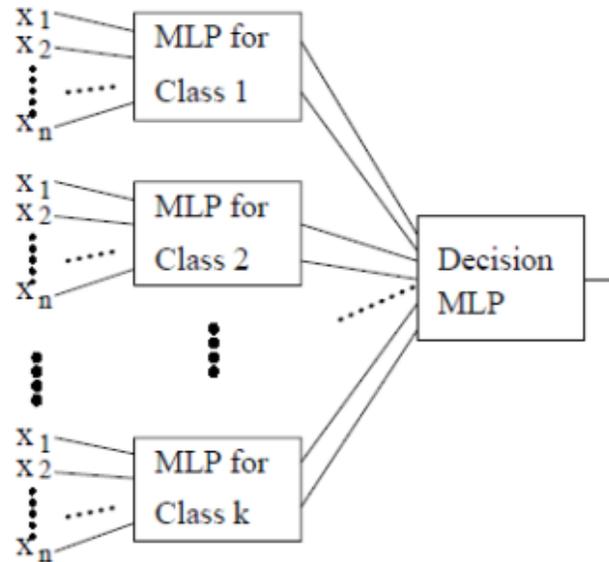
- MLP on the output of logical adaptive nodes is one idea for
- another **heterogeneous structure**

# Evolution of the Model



- A **homogeneous pyramidal** structure
- uses small **MLPs** instead of logical nodes
- This should provide **fast training** of the network as well as improved **generalization** ability

# Evolution of the Model



- The **input** and **output** dimensions of the problem remain
- **the same**
- Each **subnetwork** is only **concerned** with **a single class**

# The Final Architecture:

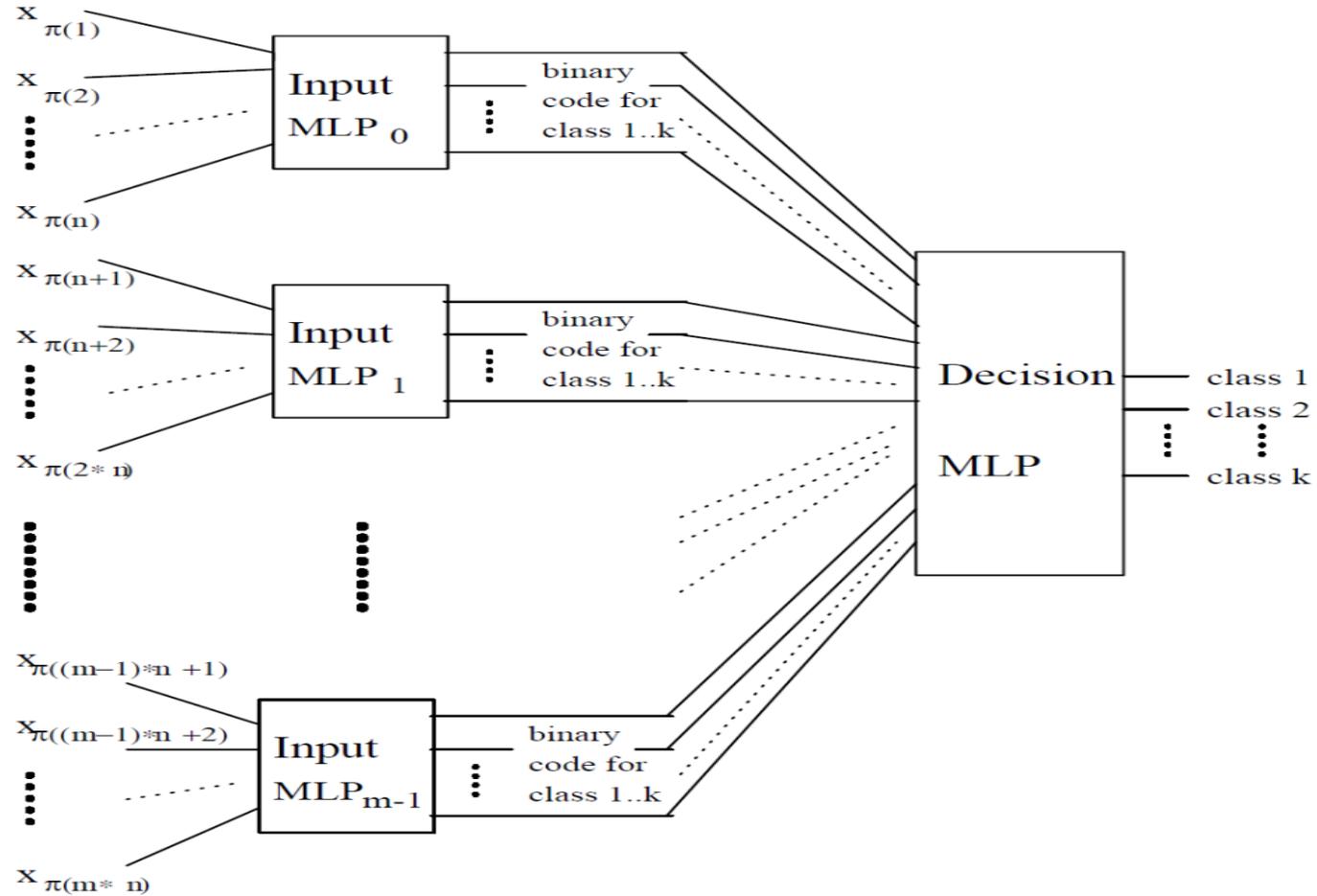


Figure 5.2: The Proposed Modular Neural Network Architecture.

# Characteristics

- All sub-networks are MLPs
- the number of inputs and the number of outputs of the module is determined by the system
- The internal structure such as the number of hidden layers and the number of neurons in each hidden layer can be chosen independent of the overall architecture

# Definition: A Module

A module is a multilayer feedforward neural network defined by a 3-tuple:

$$\mathcal{M} = (a, b, \mathcal{H})$$

Where  $a$  is the number of inputs of the module,  $b$  is the number of output nodes, and  $\mathcal{H}$  is a list containing the numbers of neurons in each of the hidden layers.

## **Example:**

A multilayer Perceptron module  $\mathcal{M}$  with eight inputs, twelve neurons in the first hidden layers, ten neurons in the second hidden layer, and four outputs is described as:  $\mathcal{M} = (8, 4, [12, 10])$ .

# Definition: A Modular Neural Network

A modular neural network is a set of interconnected modules defined by a 7-tuple.

$$N = (l, k, m, r, \pi, \mathcal{I}, \mathcal{D})$$

Where  $l$  is the number of inputs,  $k$  the number of classes,  $m$  the number of modules in the input layer,  $r$  is the type of the intermediate representation ( $r \in \{small, large\}$ ),  $\pi$  is the permutation function,  $\mathcal{I}$  is the input layer module, and  $\mathcal{D}$  is the decision module.

# Algorithm for MNN

## The Training Algorithm:

- Stage 1 – Training the Input Layer:
  1. Select the training sets  $TS_i$  from the original training set  $TS$ , for all  $i = 0 \dots m - 1$ .
  2. Train all modules  $MLP_i$  on  $TS_i$  using the BP algorithm.
- Stage 2 – Training the Decision Network
  1. Calculate the response  $r$  of the first layer for each input vector  $j$ .
$$r^j = \Phi((x_1^j, x_2^j, \dots, x_l^j)).$$
  2. Build the training set for the decision network
$$TS_d = \{(r^j; d_{BIT}^j) | j = 1, \dots, t\}$$
  3. Train the decision network on the set  $TS_d$  using the BP algorithm

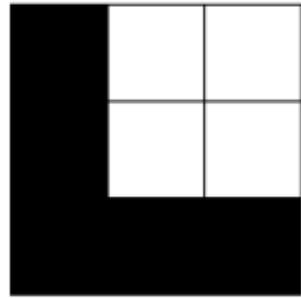
# Generalization

- The proposed architecture combines **two methods** of **generalization**:
- **One method** is built in to the **MLP**
- **Each** of the networks has the **ability to generalize** on its input space
- This type of **generalization** is common to **connectionist** systems.
- The **second method** of generalization **is due** to the architecture of the **proposed network**  
It is a way of **generalizing** according to the **similarity** of **input patterns**

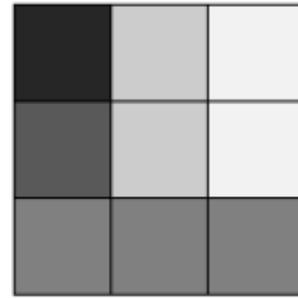
# Training



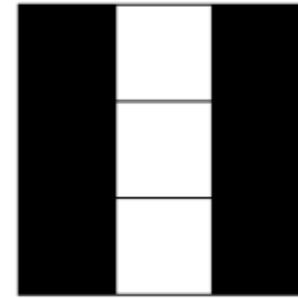
Simplified 'H'



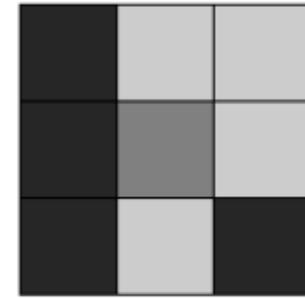
Simplified 'L'



Distorted 'L'  
Pattern 1



Distorted 'H'  
Pattern 2



Distorted 'L'  
Pattern 3

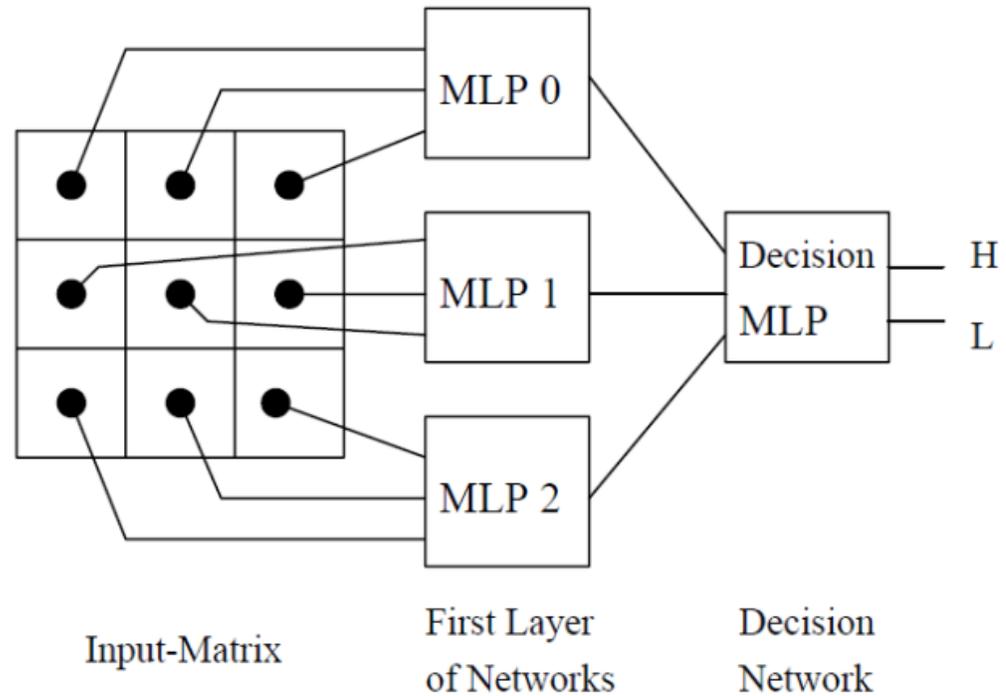
(a)

(b)

Figure 5.5: (a) The Training Set.

(b) The Test Set.

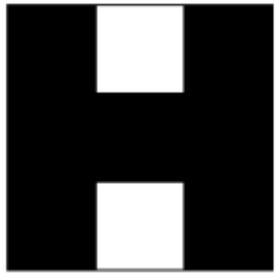
# Example Architecture



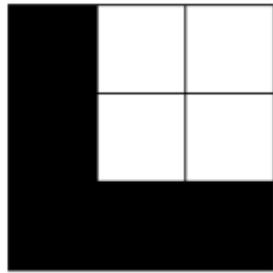
# Training

- **Input :**
- 9 values between 0 and 1 (black = 1, white = 0)
- The **network** needs to be **trained** to recognize the simplified letters 'H' and 'L'
- **Output:**            'H' = 0 ;            'L' = 1

# Training Subsets



Simplified 'H'



Simplified 'L'

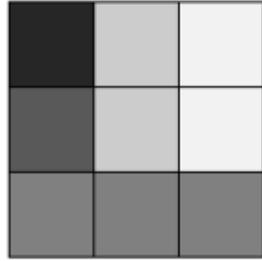
MLP <sub>0</sub>	MLP <sub>1</sub>	MLP <sub>2</sub>
(1,0,1;0)	(1,1,1;0)	(1,0,1;0)
(1,0,0;1)	(1,0,0;1)	(1,1,1;1)

# Training Set for decision Network

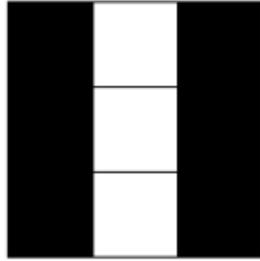
$$(\Phi(1, 0, 1, 1, 1, 1, 1, 0, 1); 1, 0) = (0, 0, 0; 1, 0)$$

$$(\Phi(1, 0, 0, 1, 0, 0, 1, 1, 1); 0, 1) = (1, 1, 1; 0, 1)$$

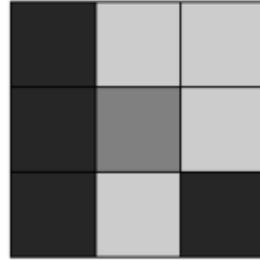
# Use Test Set



Distorted 'L'  
Pattern 1



Distorted 'H'  
Pattern 2



Distorted 'L'  
Pattern 3

- The 1st character tests generalization within the input modules
- Second tests the generalization on the number of correct sub-patterns
- Third character is a combination of both

# Global Decision Making (Classification)

$$\begin{aligned} r_1 &= \Psi(\Phi(0.9, 0.2, 0.1, 0.7, 0.2, 0.1, 0.5, 0.5, 0.5)) \\ &= \Psi(0.95, 0.86, 0.70) = (0.04, 0.96) \Rightarrow 'L' \end{aligned}$$

$$\begin{aligned} r_2 &= \Psi(\Phi(1.0, 0.0, 1.0, 1.0, 0.0, 1.0, 1.0, 0.0, 1.0)) \\ &= \Psi(0, 0.49, 0) = (0.91, 0.09) \Rightarrow 'H' \end{aligned}$$

$$\begin{aligned} r_3 &= \Psi(\Phi(0.9, 0.2, 0.2, 0.9, 0.5, 0.2, 0.9, 0.2, 0.9)) \\ &= \Psi(0.92, 0.65, 0.09) = (0.15, 0.89) \Rightarrow 'L' \end{aligned}$$

# Benefits of Modular Neural Network

- **Efficiency**

The possible **connections increases** at a daunting rate as **nodes** are **added** to the network

Since **computation time** depends on the **number** of nodes and their **connections**, any **increase** here will have drastic consequences in the **processing time**

**Speedup** of **10 times** achieved

# Benefits of Modular Neural Network

- **Training**

- A large **neural network** attempting to **model** multiple parameters can suffer from **interference** as new data can dramatically alter **existing** connections or just serve to **confuse**.
- With some **foresight** into the **subtasks** to be solved, **each** neural network can be **tailored** for **its task**
- Provide **unique** training **algorithm** and training **data** for each **sub-network**

**Implemented** much more **quickly**

# Benefits of Modular Neural Network

- **Robustness**

- Regardless of whether a large **neural network** is **biological** or **artificial**, it remains largely susceptible to **interference** at and **failure** in any one of its **nodes**
- By **compartmentalizing subtasks**, **failure** and **interference** are much more readily **diagnosed** and their **effects** on other **sub-networks** are **eliminated** as each one is **independent** of the other.

# Benefits of Modular Neural Network

Reference :

A modular neural network architecture with concept, by Yi Dinga, Qi Fenga, Tianjiang Wang, Xian Fu

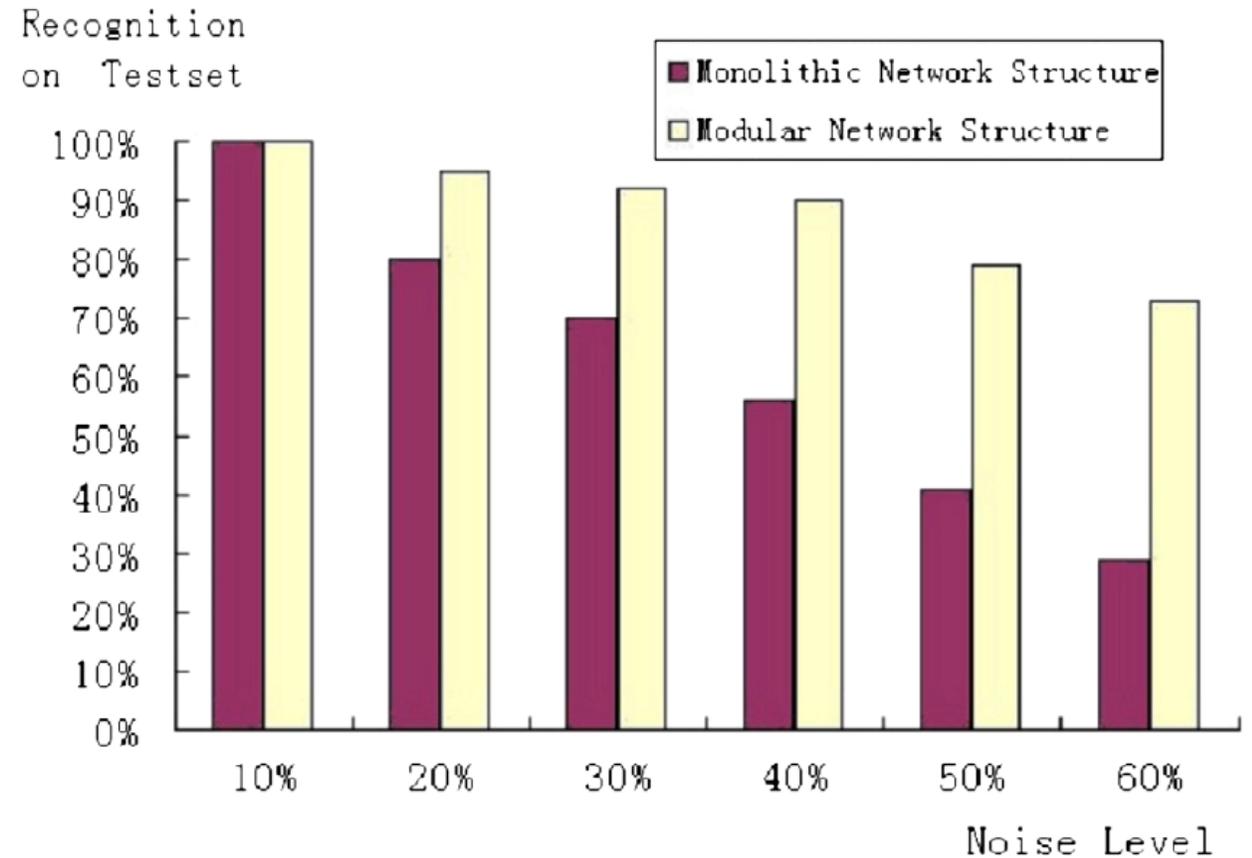


Fig. 3. The performance on noisy inputs.

# Summary

- **Modular Neural Networks**, its connection to **NN**
- Motivations
- Benefits of **MNN**
- **MNN** Architecture
- Example of developing a **MNN**