Type Analysis

Is an operator applied to an "incompatible" operand? Type checking:

- Static: Check for type compatibility at compile time
- **Dynamic:** Check for type compatibility at run time

Type analysis phase also used to <u>resolve</u> fields in a structure:

Example: list.element

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Type Checking vs. Type Inference

• A **Type Checker** only <u>verifies</u> that the given declarations are consistent with their use.

Examples: type checkers for Pascal, C.

• A **Type Inference** system <u>generates</u> consistent type declarations from information implicit in the program.

Examples: Type inference in SML, Scheme.

Given y = 3.1415 * x * x, we can **infer** that y is a float.

Why Static Type Checking?

- Catch errors at compile time instead of run time.
- Determine which operators to apply.
 Example: In x + y, "+" is integer addition if x and y are both integers.
- Recognize when to convert from one representation to another (Type Coercion).

Example: In x + y, if x is a float while y is an integer, convert y to a float value before adding.

Type Checking: An Example

```
\begin{array}{cccc} E & \longrightarrow & \texttt{int\_const} & \{ \textit{ E.type} = \textit{int; } \} \\ E & \longrightarrow & \texttt{float\_const} & \{ \textit{ E.type} = \textit{float; } \} \\ E & \longrightarrow & E_1 + E_2 & \{ \\ & & & \texttt{if } E_1.\textit{type} == E_2.\textit{type} == \textit{int } \\ & & & E.\textit{type} = \textit{int; } \\ & & & \texttt{else} \\ & & & & E.\textit{type} = \textit{float; } \\ \} \end{array}
```

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Type Checking: Another Example

Types

- Base types: atomic types with no internal structure. Examples: int, char.
- Structured types: Types that combine (collect together) elements of other types.
 - Arrays:
 Characterized by dimensions, index range in each dimension, and type of elements.
 - Records: (structs and unions)
 Characterized by fields in the record and their types.

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Type Expressions

```
Language to define types.

Type \to \text{ int | float | char ...}

void
error
name
array(size, Type)
record((name, Type)*)
pointer(Type)
tuple((Type)*)
arrow(Type, Type)
```

Examples of Type Expressions

```
float xform[3][3];
 xform ∈ array(3, array(3, float))
char *string;
 string ∈ pointer(char)
struct list { int element; struct list *next; } 1;
 list ≡ record((element, int), (next, pointer(list)))
 1 ∈ list
int max(int, int);
 max ∈ arrow(tuple(int, int), int)
```

Type Checking with Type Expressions

```
E \longrightarrow E_1 \ [E_2] \ \{ \ \text{if $E_1$.type} == rray(\mathbf{S}, \, \mathbf{T}) \ \mathsf{AND} \ E_2.type == int} \ E.type = \mathbf{T} \ else \ E.type = error \ \} \ \{ \ \text{if $E_1$.type} == pointer(\mathbf{T}) \ E.type = \mathbf{T} \ else \ E.type = error \ \} \ E \longrightarrow \& E_1 \ \{ \ E.type = pointer(E_1.type) \ \}
```

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Functions and Operators

Functions and Operators have Arrow types.

- $\bullet \ \text{max:} \ \textit{int} \ \times \ \textit{int} \ \longrightarrow \ \textit{int}$
- sort: numlist → numlist

Functions and operators are applied to operands.

• max(x,y):

Function Application

```
E \longrightarrow E_1 E_2 \qquad \{ 	ext{ if } E_1. type \equiv 	ext{arrow}(\textbf{S}, \, \textbf{T}) 	ext{ AND} \ E_2. type \equiv \textbf{S} \ E. type = \textbf{T} \ 	ext{else} \ E. type = 	ext{error} \} 
E \longrightarrow (E_1, E_2) \quad \{ E. type = 	ext{tuple}(E_1. type, E_2. type) \}
```

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Type Equivalence

```
When are two types "equal"?

    type Vector = array [1..10] of real;
    type Weights = array [1..10] of real;

    var x, y: Vector;
    z: Weight;
```

- Name Equivalence: When they have the same name. x and y have same type, but z has different type.
- **Structural Equivalence:** When they have the same structure. x, y and z have same type.

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Structural Equivalence

```
S \equiv T iff:
```

- S and T are the same basic type;
- ullet ${f S}={f array}(S_1)$, ${f T}={f array}(T_1)$, and $S_1\equiv T_1$.
- $S = pointer(S_1)$, $T = pointer(T_1)$, and $S_1 \equiv T_1$.
- ullet ${f S}={f tuple}(S_1,S_2)$, ${f T}={f tuple}(T_1,T_2)$, and $S_1\equiv T_1$ and $S_2\equiv T_2$.
- ullet ${f S}={f arrow}(S_1,S_2)$, ${f T}={f arrow}(T_1,\,T_2)$, and $S_1\equiv T_1$ and $S_2\equiv T_2$.

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Subtyping

Object-oriented languages permit subtyping.

```
class Rectangle {
   private int x,y;
   int area() { ... }
}
class Square extends Rectangle {
   ...
}
```

Square is a subclass of Rectangle.

Since all methods on Rectangle are inherited by Square (unless explicitly overridden)

Square is a subtype of Rectangle.

Inheritance

```
class Circle {
  float x, y; // center
  float r; // radius
  float area() {
    return 3.1415 * r * r;
 }
}
class ColoredCircle extends Circle {
  Color c;
}
class Test{
  static main() {
    ColoredCircle t;
      ... t.area() ...
  }
}
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                                     Types
```

Resolving Names

What entity is represented by t.area()? (assume no overloading)

- Determine the type of t.
 t has to be of type user(c).
- If c has a method of name area, we are done.

 Otherwise, if the superclass of c has a method of name area, we are done.

Otherwise, if the superclass of superclass of c...

⇒ Determine the nearest <u>superclass</u> of class c that has a method with name area.

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Overloading

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```
class Rectangle {
  int x,y; // top lh corner
  int l, w; // length and width

  Rectangle move() {
    x = x + 5;      y = y + 5;
    return this;
  }

  Rectangle move(int dx, int dy) {
    x = x + dx;      y = y + dy;
    return this;
  }
}
```

Resolving Overloaded Names

What entity is represented by move in r.move(3, 10)?

- Determine the type of r.
 r has to be of type user(c).
- Determine the nearest $\underline{superclass}$ of class c that has a method with name move

Types

such that move is a method that takes two int parameters.

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Structural Subtyping

$S \subset T$ iff:

- **S** and **T** are the same **basic type**.
- $S = user(type_1)$, $T = user(type_2)$ and $type_1 \subseteq type_2$.
- $S = \operatorname{array}(S_1)$, $T = \operatorname{array}(T_1)$, and $S_1 \subseteq T_1$;
- ullet ${f S}={ t pointer}(S_1)$, ${f T}={ t pointer}(T_1)$, and $S_1\subseteq T_1$;
- ullet ${f S}={f tuple}(S_1,S_2)$, ${f T}={f tuple}(T_1,T_2)$, and $S_1\subseteq T_1$ and $S_2\subseteq T_2$;
- ullet ${f S}={f arrow}(S_1,S_2)$, ${f T}={f arrow}(T_1,T_2)$, and $S_1\subseteq T_1$ and $T_2\equiv S_2$.

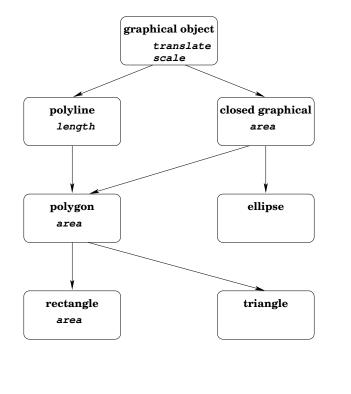
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Inheritance and Overloading

What entity is represented by f in $E.f(a_1, a_2, ..., a_n)$?

- Let the type of E be user(c).
- f is the method in the nearest superclass of class c such that type of f is a supertype of $type(a_1) \times \cdots type(a_1) \to \bot$.

Inheritance: Another Example



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Abstract objects and Concrete Representations

Abstract classes <u>declare</u> methods, but do not <u>define</u> them.

Example:

- closed_graphical declares "area" method, but cannot define the method.
- The different "area" methods are defined when the object's representations are concrete: in rectangle, ellipse, etc.

When "area" method is applied to an object of class closed_graphical, we method to be called is the one defined in rectangle, triangle, ellipse, etc.

... which can be resolved only at run-time!

Types in OO Languages: The Whole Story

Decaf implements a small part of the type system for an OO language.

• **Subtype rule:** Wherever an object of type *t* is required (as a parameter of a method, return value, or rhs of assignments), object of any subtype *s* of *t* can be used.

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Types in OO Languages: The Whole Story (contd.)

• **Method Selection rule:** If class B inherits from class tt A and overwrites method m, then for any B object b, method m of B must be used, even if b us used as an A object.

```
class A {
  int m() { ... }
  int m() { ... }
  }

class C{
  int f(B b) {
    A a;

  a = b;
    ... a.m() ...
}
```

Types in OO Languages: The Whole Story (contd.)

• **Dynamic Binding rule:** A method of object *obj*, which can be potentially overwritten in a subclass has to be bound **dynamically** if the compiler cannot determine the runtime type of *obj*.