Genetic Algorithms
Simple Examples

Cse352
Artificial Intelligence
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A program in C

- int foo (int time)

        {
            int temp1, temp2;
            if (time > 10)
                temp1 = 3;
            else
                temp1 = 4;
            temp2 = temp1 + 1 + 2;
            return (temp2);
        }

- Equivalent expression (similar to a classification rule in data mining):

(+ 1 2 (IF (> TIME 10) 3 4))
Program tree

(+ 1 2 (IF (> TIME 10) 3 4))

Citation: www.genetic-programming.com/c2003lecture1modified.ppt
Given data

<table>
<thead>
<tr>
<th>Input: Independent variable $X$</th>
<th>Output: Dependent variable $Y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>-0.80</td>
<td>0.84</td>
</tr>
<tr>
<td>-0.60</td>
<td>0.76</td>
</tr>
<tr>
<td>-0.40</td>
<td>0.76</td>
</tr>
<tr>
<td>-0.20</td>
<td>0.84</td>
</tr>
<tr>
<td>0.00</td>
<td>1.00</td>
</tr>
<tr>
<td>0.20</td>
<td>1.24</td>
</tr>
<tr>
<td>0.40</td>
<td>1.56</td>
</tr>
<tr>
<td>0.60</td>
<td>1.96</td>
</tr>
<tr>
<td>0.80</td>
<td>2.44</td>
</tr>
<tr>
<td>1.00</td>
<td>3.00</td>
</tr>
</tbody>
</table>
# Problem description

<table>
<thead>
<tr>
<th>Objective:</th>
<th>Find a computer program with one input (independent variable $x$) whose output $Y$ equals the given data</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Terminal set:</td>
<td>$T = {X, \text{Random-Constants}}$</td>
</tr>
<tr>
<td>2 Function set:</td>
<td>$F = {+,-,\times,\div}$</td>
</tr>
<tr>
<td>3 Initial population:</td>
<td>Randomly created individuals from elements in $T$ and $F$.</td>
</tr>
<tr>
<td>4 Fitness:</td>
<td>$</td>
</tr>
<tr>
<td>5 Termination:</td>
<td>An individual emerges whose sum of absolute errors (the value of its fitness function) is less than 0.1</td>
</tr>
</tbody>
</table>

Citation: [www.genetic-programming.com/c2003lecture1modified.ppt](http://www.genetic-programming.com/c2003lecture1modified.ppt)
Generation 0

Population of 4 randomly created individuals

(a) \( x + 1 \)  
(b) \( x^2 + 1 \)  
(c) 2  
(d) \( x \)

Citation: examples taken from: www.genetic-programming.com/c2003lecture1modified.ppt
Mutation

Mutation:
picking "2"
as mutation point

Citation: part of the pictures used as examples are taken from: [www.genetic-programming.com/c2003lecture1modified.ppt](http://www.genetic-programming.com/c2003lecture1modified.ppt)
Crossover

Crossover:

picking “+” subtree and leftmost “x” as crossover points

Citation: example taken from: www.genetic-programming.com/c2003lecture1modified.ppt
Generation 1

Copy of (a)

Mutant of (c)
picking “2” as mutation point

First offspring of crossover of (a) and (b)
picking “+” of parent (a) and left-most “x” of parent (b) as crossover points

Second offspring of crossover of (a) and (b)
picking “+” of parent (a) and left-most “x” of parent (b) as crossover points

Citation: part of the examples is taken from: [www.genetic-programming.com/c2003lecture1modified.ppt](http://www.genetic-programming.com/c2003lecture1modified.ppt)
| $X$ | $Y$ | $X+1$ | $|X+1-Y|$ | $1$ | $|1-Y|$ | $X$ | $|X-Y|$ | $X^2+X+1$ | $|X^2+X+1-Y|$ |
|-----|-----|-------|-----------|-----|--------|-----|--------|-------------|-----------------|
| -1.00 | 1.00 | 0 | 1 | 1 | 0 | -1.00 | 2 | 1 | 0 |
| -0.80 | 0.84 | 0.20 | 0.64 | 1 | 0.16 | -0.80 | 1.64 | 0.84 | 0 |
| -0.60 | 0.76 | 0.40 | 0.36 | 1 | 0.24 | -0.60 | 1.36 | 0.76 | 0 |
| -0.40 | 0.76 | 0.60 | 0.16 | 1 | 0.24 | -0.40 | 1.16 | 0.76 | 0 |
| -0.20 | 0.84 | 0.80 | 0.04 | 1 | 0.16 | -0.20 | 1.04 | 0.84 | 0 |
| 0.00 | 1.00 | 1.00 | 0 | 1 | 0 | 0.00 | 1 | 1 | 0 |
| 0.20 | 1.24 | 1.20 | 0.04 | 1 | 0.24 | 0.20 | 1.04 | 1.24 | 0 |
| 0.40 | 1.56 | 1.40 | 0.16 | 1 | 0.56 | 0.40 | 1.16 | 1.56 | 0 |
| 0.60 | 1.96 | 1.60 | 0.36 | 1 | 0.96 | 0.60 | 1.36 | 1.96 | 0 |
| 0.80 | 2.44 | 1.80 | 0.64 | 1 | 1.44 | 0.80 | 1.64 | 2.44 | 0 |
| 1.00 | 3.00 | 2.00 | 1 | 1 | 2 | 1.00 | 2 | 3 | 0 |

**Fitness**: 4.40 + 6.00 + 15.40 = 25.80

**Found!**
**GA and Classification**

**Classify** customers based on number of children and salary:

<table>
<thead>
<tr>
<th>Parameter</th>
<th># of children (NOC)</th>
<th>Salary (S)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>0…10</td>
<td>0…500000</td>
</tr>
<tr>
<td>Syntax of atomic expression</td>
<td>NOC = x</td>
<td></td>
</tr>
<tr>
<td></td>
<td>NOC &lt; x</td>
<td>S = x</td>
</tr>
<tr>
<td></td>
<td>NOC &lt;= x</td>
<td>S &lt; x</td>
</tr>
<tr>
<td></td>
<td>NOC &gt; x</td>
<td>S &gt; x</td>
</tr>
<tr>
<td></td>
<td>NOC &gt;= x</td>
<td></td>
</tr>
</tbody>
</table>
GA and Classification Rules

• A classification rule is of the form

$$\text{IF description THEN class} = c_i$$

Antecedent         Consequence
Formula representation

• Possible rule:
  – If (NOC = 2) AND ( S > 80000) then GOOD (customer)
# Initial data table

<table>
<thead>
<tr>
<th>Nr. Crt.</th>
<th>Number of children (NOC)</th>
<th>Salary (S)</th>
<th>Type of customer (C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>&gt; 80000</td>
<td>GOOD</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>&gt; 30000</td>
<td>GOOD</td>
</tr>
<tr>
<td>3</td>
<td>0</td>
<td>= 50000</td>
<td>GOOD</td>
</tr>
<tr>
<td>4</td>
<td>&gt; 2</td>
<td>&lt; 10000</td>
<td>BAD</td>
</tr>
<tr>
<td>5</td>
<td>= 10</td>
<td>= 30000</td>
<td>BAD</td>
</tr>
<tr>
<td>6</td>
<td>= 5</td>
<td>&lt; 30000</td>
<td>BAD</td>
</tr>
</tbody>
</table>
Initial data represented as rules

- Rule 1: If (NOC = 2) AND (S > 80000) then C = GOOD
- Rule 2: If (NOC = 1) AND (S > 30000) then C = GOOD
- Rule 3: If (NOC = 0) AND (S = 50000) then C = GOOD
- Rule 4: If (NOC > 2) AND (S < 10000) then C = BAD
- Rule 5: If (NOC = 10) AND (S = 30000) then C = BAD
- Rule 6: If (NOC = 5) AND (S < 30000) then C = BAD
Generation 0

• Population of 3 randomly created individuals:
  – If (NOC > 3) AND (S > 10000) then C = GOOD
  – If (NOC > 1) AND (S > 30000) then C = GOOD
  – If (NOC >= 0) AND (S < 40000) then C = GOOD

• We want to find a more general (if it is possible the most general) characteristic description for class GOOD

• We want to assign predicted class GOOD for all individuals
Generation 0

\[(\text{NOC} > 3) \land (S > 10000)\]

\[(\text{NOC} > 1) \land (S > 30000)\]

\[(\text{NOC} \geq 0) \land (S < 40000)\]
Fitness function

• For a rule IF A THEN C
  CF (Confidence factor) = \frac{|A \cup C|}{|A|}

  \(|A| = \text{number of records that satisfy } A\)
  \(|A \cup C| = \text{number of records that satisfy } A \text{ and are in predicted class } C\)

Citation: the confidence formula is taken from class slides: http://www.cs.sunysb.edu/~cse634/lecture_notes/07association.pdf
Fitness function – Generation 0

Rule 1: If (NOC = 2) AND (S > 80000) then GOOD
Rule 2: If (NOC = 1) AND (S > 30000) then GOOD
Rule 3: If (NOC = 0) AND (S = 50000) then GOOD
Rule 4: If (NOC > 2) AND (S < 10000) then BAD
Rule 5: If (NOC = 10) AND (S = 30000) then BAD
Rule 6: If (NOC = 5) AND (S < 30000) then BAD

Fitness of Individual 1: If (NOC > 3) AND (S > 10000) then GOOD
|A| = 2 (Rule 5 & 6), |AUC| = 0, CF = 0 / 2 = 0
Fitness of Individual 2: If (NOC > 1) AND (S > 30000) then GOOD
|A| = 1 (Rule 1), |AUC| = 1, CF = 1 / 1 = 1
Fitness of Individual 3: If (NOC >= 0) AND (S < 40000) then GOOD
|A| = 4 (Rule 2 & 4 & 5 & 6), |AUC| = 1, CF = 1 / 4 = 0.25

Best in Gen 0
\[(\text{NOC} \geq 0) \land (S < 40000)\]

\[(\text{NOC} > 0) \land (S < 90000)\]
(NOC > 1) AND (S > 30000)

(NOC >= 0) AND (S > 30000)

(NOC > 1) AND (S < 40000)

(NOC >= 0) AND (S < 40000)
Generation 1

Individual 1

\[(\text{NOC} > 1) \land (S < 40000)\]

Individual 2

\[(\text{NOC} \geq 0) \land (S > 30000)\]

Individual 3

\[(\text{NOC} > 0) \land (S < 90000)\]
Fitness function – Generation 1

Rule 1: If (NOC = 2) AND (S > 80000) then GOOD
Rule 2: If (NOC = 1) AND (S > 30000) then GOOD
Rule 3: If (NOC = 0) AND (S = 50000) then GOOD
Rule 4: If (NOC > 2) AND (S < 10000) then BAD
Rule 5: If (NOC = 10) AND (S = 30000) then BAD
Rule 6: If (NOC = 5) AND (S < 30000) then BAD

Individual 1: If (NOC > 1) AND (S < 40000) then GOOD
|A| = 2 (Rule 4 & 5 & 6), |A&C| = 0, CF = 0 / 2 = 0

Individual 2: If (NOC >= 0) AND (S > 30000) then GOOD
|A| = 3 (Rule 1 & 2 & 3), |A&C| = 3, CF = 3 / 3 = 1

Individual 3: If (NOC > 0) AND (S < 90000) then GOOD
|A| = 5 (Rule 1 & 2 & 4 & 5 & 6), |A&C| = 1, CF = 1 / 5 = 0.2

Best in Gen 1
GA Rules Problem

- When GAs are used for optimization, the goal is typically to return a single value - the best solution found to date.

- The entire population ultimately converges to the neighborhood of a single solution.

- Sometimes GAs employ a special method called a niching method that makes them capable of finding and maintaining multiple rules.
APPLICATION EXAMPLE

Technical Document of

LBS Capital Management, Inc., Clearwater, Florida

Link: http://nas.cl.uh.edu/boetticher/ML_DataMining/mahfoud96financial.pdf
Forecasting Individual Stock Performance

- **GOAL:** using historical data of a stock, predict relative return for a quarter

Example: If IBM stock is up 5% after one quarter and the S&P 500 index is up 3% over the same period, then IBM’s relative return is +2%

-The Implementation Example consists of 15 attributes of a stock at specific points in time and the relative return for the stock over the subsequent 12 week time period.

- **200 to 600 (records) examples** were utilized depending on the experiment and the data available for a particular stock

**GOAL:** Combination of rules is required to model relationships among financial variables

Example: **Rule-1:** IF [P/E > 30] THEN Sell

**Rule-2:** IF [P/E < 40 and Growth Rate > 40%] THEN Buy
Preliminary Experiments

• For **Preliminary set of experiments**, to predict the return, relative to the market, a Madcap stock was randomly selected from the S&P 400

• 331 examples (records) present in the database of examples of stock X

• 70% of examples (records) were used as a **training set** for the GA

• 20% of the examples (records) were used as a stopping set, to decide which population is best

• 10% of the examples (records) were used to measure performance

• **A sample rule** that the GA generated in one of the experiments:
  
  IF [Earning Surprise Expectation > 10% and Volatility > 7%] and […]

  THEN Prediction = Up

• Same set of experiments were used using **Neural Network** with one layer of hidden nodes using **Backpropagation algorithm** with the same training, stopping and test sets as that of **GA experiment**
Observations on the Results

- The **GA** correctly predicts the direction of stock relative to the market 47.6% of the time and incorrectly predicts the 6.6% of time and produces no prediction 45%.

- Over **half of the time** (47.6% + 6.6%), the **GA** makes a prediction.

- When it **does make a prediction**, **GA** is correct 87.8% of the time.

- The **Neural Network** **correctly predicts** the direction relative to the market 79.2% of the time and incorrectly predicts direction 15.8% of the time.

- When it **does make a prediction**, the **NN** is correct 83.4%
Comparison with Neural Networks

• **Advantage** of GA’s over NN’s:
  1. GA has ability to output comprehensible rules
  2. GA provides rough explanation of the concepts learned by black-box approaches such as NN’s
  3. GA learns rules that are subsequently used in a formal expert system
• 3. GA makes no prediction when data is uncertain as opposed to Neural Network