# CSE528 Computer Graphics: Theory, Algorithms, and Applications

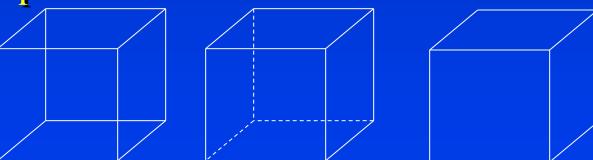
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#### Hidden Surface Removal

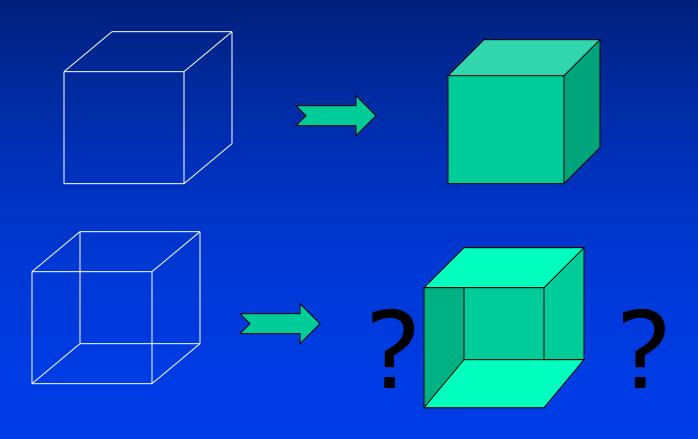
#### Hidden Surface Removal

- In 3D we must be concerned with whether or not objects are obscured by other objects
- Most objects are opaque so they should obscure/block things behind them
- Also known as: visible surface detection methods or hidden surface elimination methods

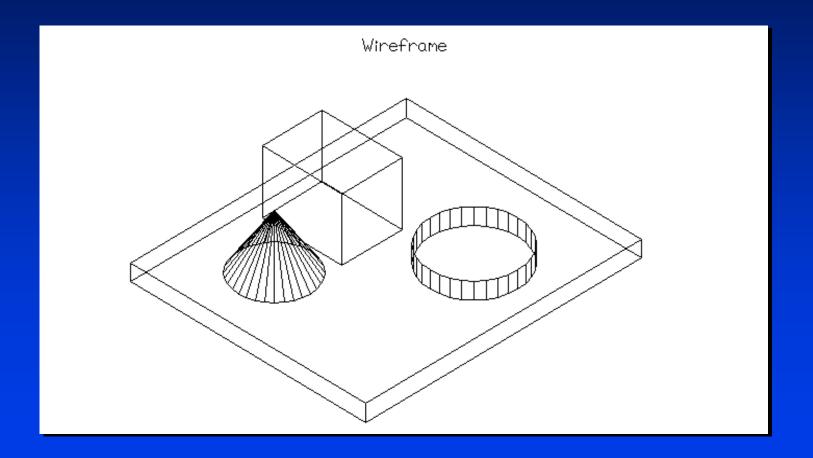
Related problem: Hidden line removal



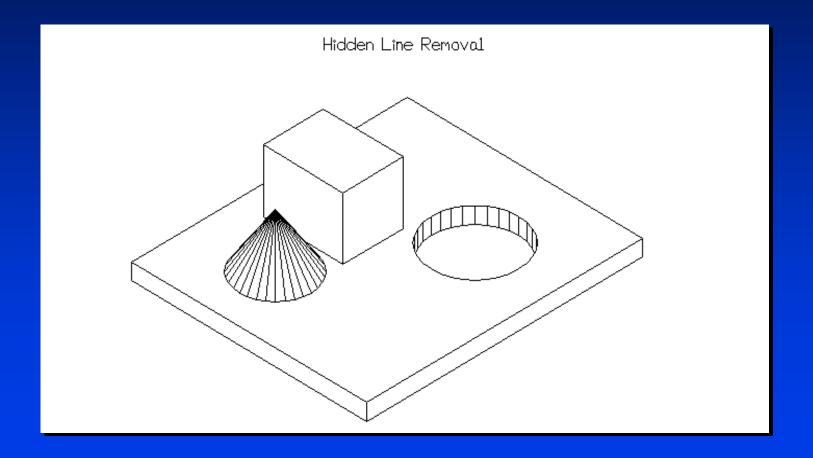
# Hidden Surface Removal (Example)



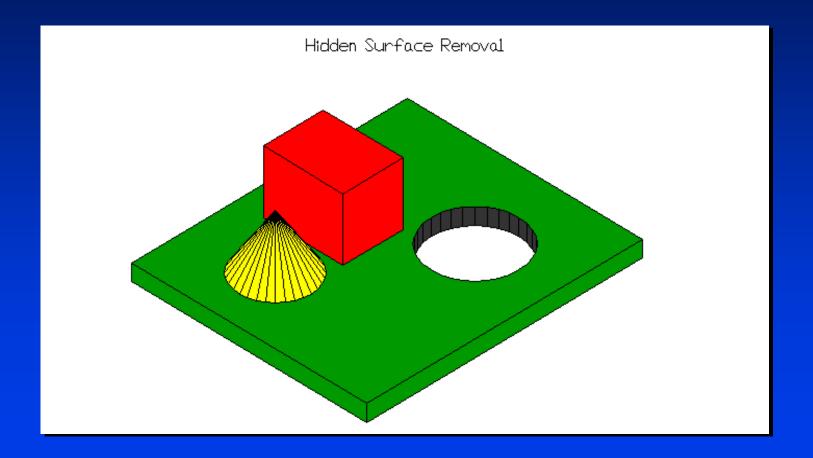
## No Lines Removed



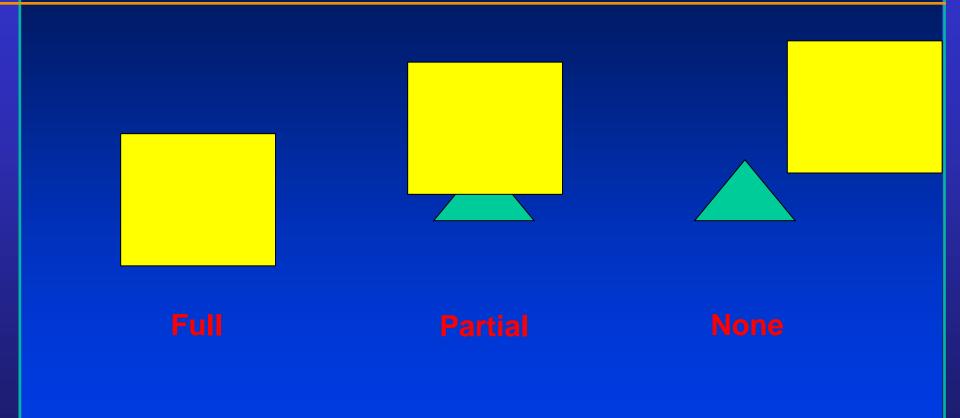
## Hidden Lines Removed



## Hidden Surfaces Removed



# Occlusion: Full, Partial, None



- The rectangle is closer than the triangle
- Should appear in front of the triangle



#### Hidden Surface Removal

- Motivation
- Algorithms for hidden surface removal
  - Back-face detection
  - Painter's algorithm
  - Ray casting
  - Scan-line
  - Z-buffer
  - Area subdivision
- Tradeoffs when comparing different techniques

#### **Motivation**

 Suppose that we have the polyhedron which has 3 totally visible surfaces, 4 totally invisible/hidden surfaces, and 1 partially visible/hidden surface.

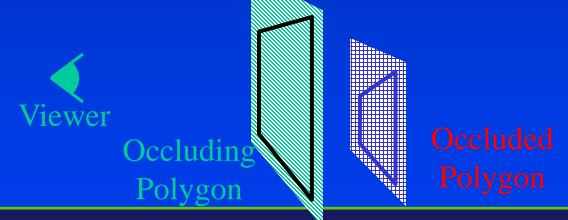
- Obviously, invisible/hidden surfaces do not contribute to the final image during graphics image synthesis.
- The procedure that distinguishes between visible surfaces from invisible/hidden surfaces is called visible-surface determination, which is often called hidden-surface removal.

#### **Motivation**

Surfaces may be back-facing:



Surfaces may be occluding:

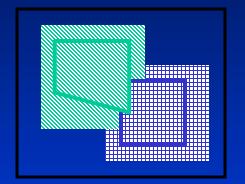




#### **Motivation**

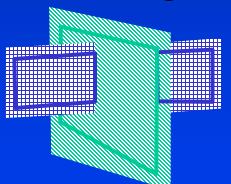
• Surfaces may be overlapping:

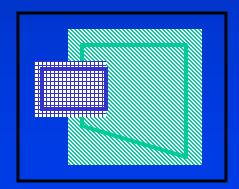




Surfaces may be intersecting:







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# Image or Object Space Algorithms

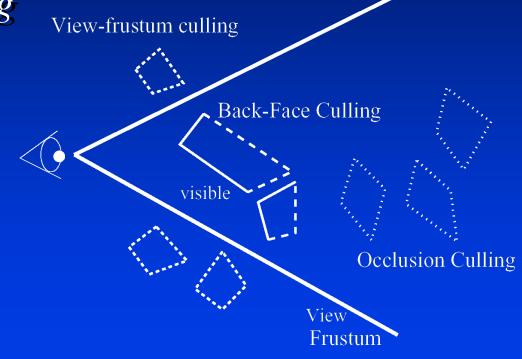
- Ideally an object space method converts the 3D scene into a list of 2D areas to be painted
- Image space decides for each pixel which surface to paint

# Visibility

- Basic assumption: All polygons are opaque
- What polygons are visible with respect to your view frustum?
  - Outside: View frustum clipping
    - > Remove polygons outside of the view volume
    - For example, Liang-Barsky 3D clipping (see our textbook for details)
  - Inside: Hidden surface removal
    - **Backface culling** 
      - Polygons facing away from the viewer
    - **Occlusion** 
      - > Polygons farther away are obscured by closer polygons
      - > Full or partially occluded portions
- Why should we remove these polygons?
  - Avoid unnecessary expensive operations on these polygons later

# Visibility Culling

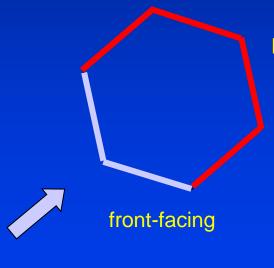
- Culling techniques
  - View-frustum culling
    - Reject geometry outside the viewing volume
  - Back-face culling
    - Reject geometry facing away from the observer
  - Occlusion culling
    - Reject objects occluded by others



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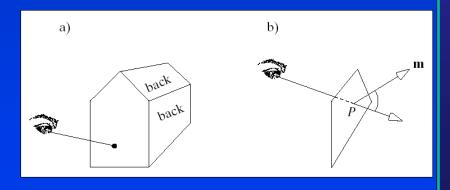
# **Backface Culling**

- Avoid drawing polygons facing away from the viewer
  - Front-facing polygons occlude these polygons in a closed polyhedron
- Test if a polygon is front- or back-facing?



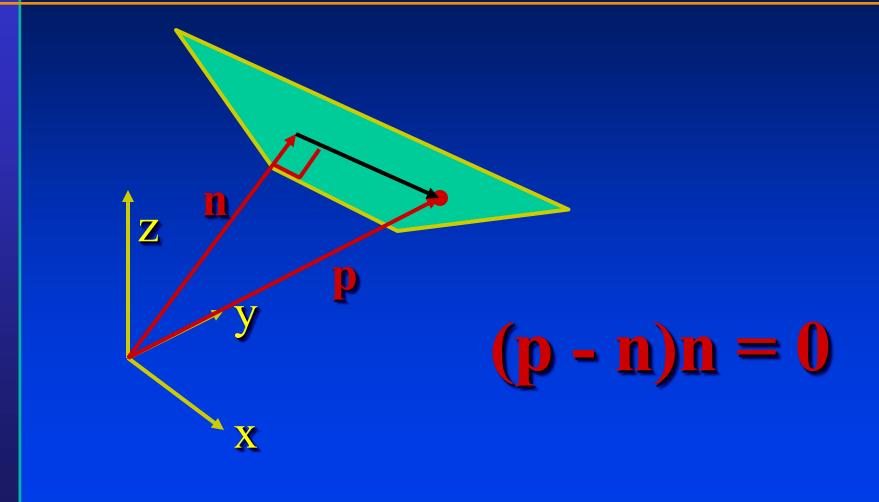
back-facing

#### Ideas?





## Which Side of a Plane?



# **Back Face Culling**

- Performance goals in real-time rendering
  - frame rate: 60-72 frames/sec?
  - resolution: 1600x1200?
  - photorealism (if necessary): undistinguishable from real scene!
- Unfortunately, there is no real upper limit on the scene complexity.
- We should *cull* those portions of the scene that are not considered to contribute to the final image as early as possible, and process only the rest of the scene.
- The simplest is *back-face culling*, which distinguishes between front faces (faces towards the viewer) and back faces (faces away from the viewer).

# **Detecting Back-face Polygons**

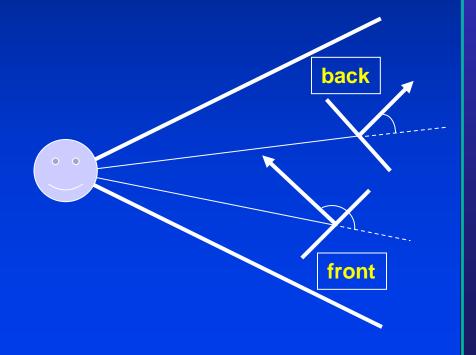
- The polygon normal of a ....
  - Front-facing polygon points towards the viewer
  - back-facing polygon points away from the viewer

If 
$$(\mathbf{n} \cdot \mathbf{v}) > 0 \Rightarrow$$
 "back-face"  
If  $(\mathbf{n} \cdot \mathbf{v}) \leq 0 \Rightarrow$  "front-face"  
 $\mathbf{v} = \text{view vector}$ 

• Eye-space test .... EASY!

➤ "back-face" if n<sub>x</sub> < 0

glCullFace(GL\_BACK)

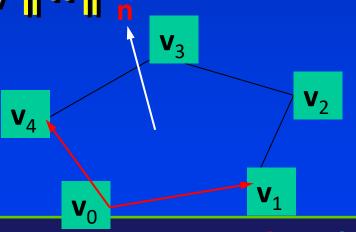


# Polygon Normals

- Let polygon vertices  $V_0$ ,  $V_1$ ,  $V_2$ ,...,  $V_{n-1}$  be in counterclockwise order and co-planar
- Calculate normal with cross product:

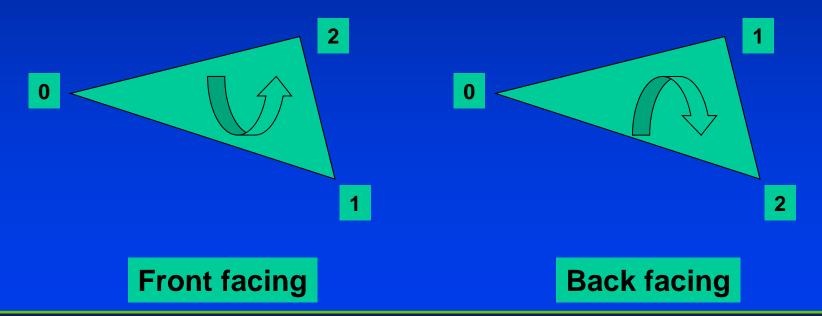
$$\mathbf{n} = (\mathbf{v}_1 - \mathbf{v}_0) \times (\mathbf{v}_{n-1} - \mathbf{v}_0)$$

• Normalize to unit vector with n/ n



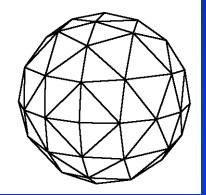
#### **Normal Direction**

- Vertices counterclockwise ⇒ Front-facing
- Vertices clockwise ⇒ Back-facing

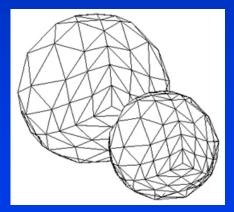


# **Back Face Culling**

- Back-face culling works as a preprocessing step for hidden surface removal, and is very powerful in that almost half of polygons of an object are discarded as back faces.
- Especially, for a single convex polyhedron, the back-face culling does the entire job of hidden-surface removal.
- Hidden-surface removal is applied to only the remaining front faces.



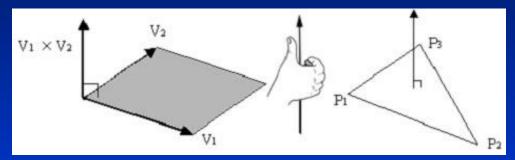
single convex polyhedron



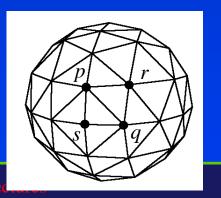
convex, but not a single polyhedron

#### **Face Normal**

The normal of a triangle  $\langle p_1, p_2, p_3 \rangle$  is computed as  $v_1 X v_2$  where  $v_1$  is the vector connecting  $p_1$  and  $p_2$ , and  $v_2$  connects  $p_1$  and  $p_3$ .



If the vertices of every polygon are ordered consistently (CCW or CW), we can make every polygon's normal point out of the polyhedron. All mesh data used in this class have triangles of CCW vertex ordering.



$$t_{1} = (p, q, r)$$

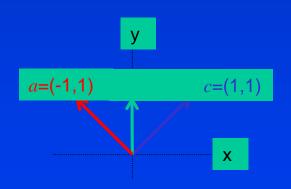
$$t_{2} = (s, q, p)$$

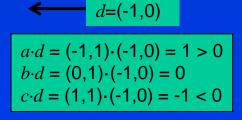
$$t_{1}'s \text{ normal} = (q-p)X(r-p)$$

$$t_{2}'s \text{ normal} = (q-s)X(p-s)$$

# Dot Product (revisited)

- Recall the dot product of two vectors  $v_i \& v_i$ .
  - If  $v_i \cdot v_i = 0$ ,  $v_i \cdot v_j$  are orthogonal/perpendicular.
  - If  $v_i \cdot v_i > 0$ , angle < 90
  - If  $v_i \cdot v_i < 0$ , angle > 90
- The same applies to 3D.

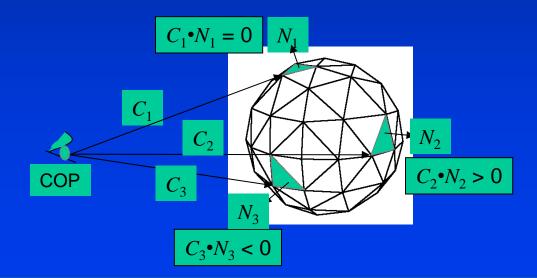






# Dot Product for Back Face Culling

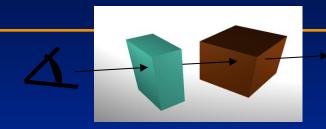
- Determining if a polygon is a front face or a back face
  - Generate a vector C connecting COP and a vertex of the polygon.
  - Take the dot product  $C \cdot N$  of the vector C and the polygon's normal N.
  - If  $C \cdot N > 0$ , it's a back face.
  - If  $C \cdot N < 0$ , it's a front face.
  - If  $C \cdot N = 0$ , it's a face that is projected as an edge/silhouette on the screen.

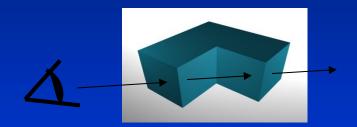




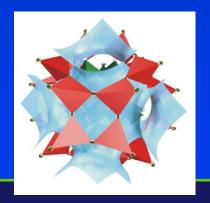
# **Backface Culling**

- For all polygons P<sub>i</sub>
  - Find Polygon Normal n
  - Find Viewer Direction v
  - $-\mathbf{IF} \quad (\mathbf{n} \bullet \mathbf{v} \le 0)$ 
    - Then CULL P<sub>i</sub>





- Does not work well for:
  - Overlapping front faces due to
    - Multiple objects
    - Concave objects
  - Non-polygonal models

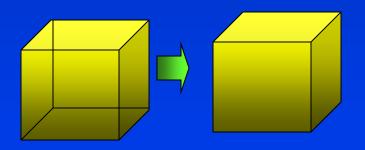


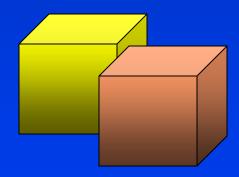




# Back Face Removal (Culling)

- Used to remove unseen polygons from convex, closed polyhedron (cube, sphere)
- Does not completely solve hidden surface problem since one polyhedron may obscure another



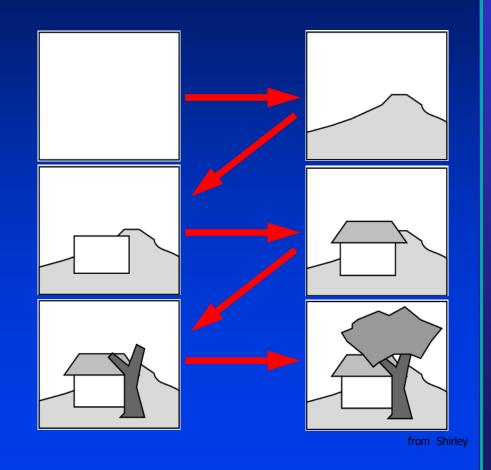


#### • Basic Idea

A painter creates a picture by drawing background scene elements before foreground ones:

#### Requirements

- Draw polygons in back-tofront order
- Need to <u>sort</u> the polygons by depth order to get a correct image



1. Sort all objects'  $z_{min}$  and  $z_{max}$ 

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- 2. If an object is uninterrupted (its  $z_{min}$  and  $z_{max}$  are adjacent in the sorted list), it is fine
- 3. If 2 objects DO overlap
  - 3.1 Check if they overlap along x-axis
    - If not, they are fine
  - 3.2 Check if they overlap along y-axis
    - If not, they are fine
    - If yes, need to split one

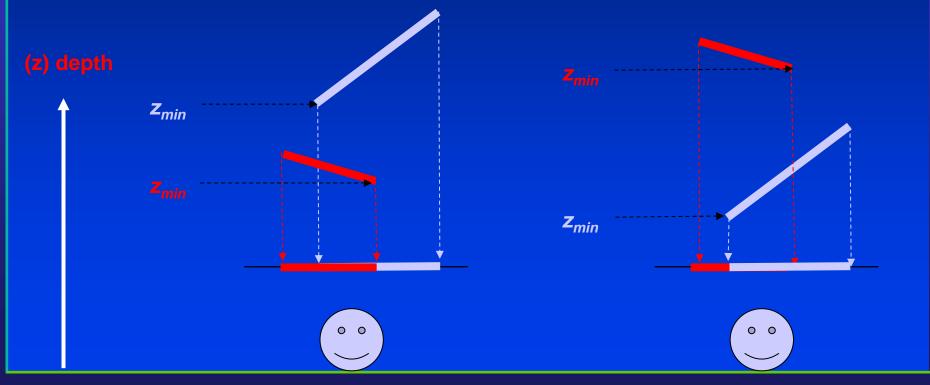
- The splitting step is the tough one
  - Need to find a plane to split one polygon so that each new polygon is entirely in front of or entirely behind the other
  - Polygons may actually intersect, so need to split each polygon by the other

- The splitting step is the tough one
  - Need to find a plane to split one polygon so that each new polygon is entirely in front of or entirely behind the other
  - Polygons may actually intersect, so then need to split each polygon by the other
- After splitting, you can resort the list and should be fine

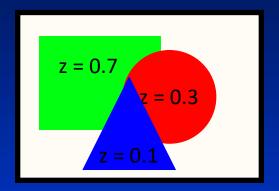
# Painter's Algorithm - Summary

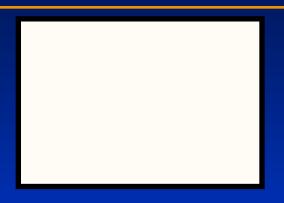
- Advantages
  - Simple algorithm for ordering polygons
- Disadvantages
  - Sorting criteria difficult to produce
  - Redraws same pixel many times
  - Sorting can also be expensive

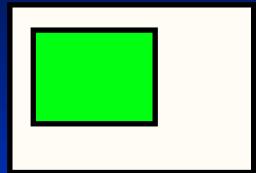
- Compute  $z_{min}$  ranges for each polygon
- Project polygons with furthest  $z_{min}$  first



# Painter's Example

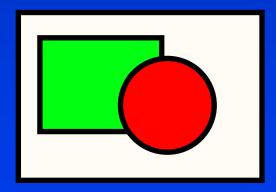


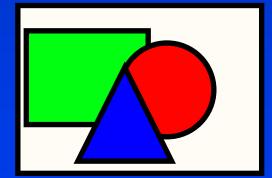




#### Sort by depth:

Green rect Red circle Blue tri







# **Depth Sorting**

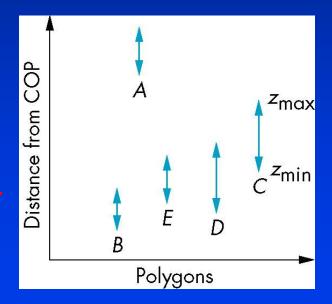
- Requires ordering of polygons first
  - -O(n log n) calculation for ordering

—Not every polygon is either in front or behind all other

polygons

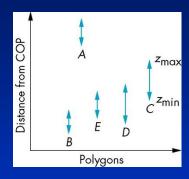
 Order polygons and deal with easy cases first, harder later

> Polygons sorted by distance from COP

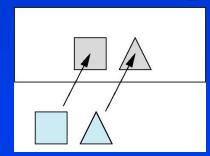


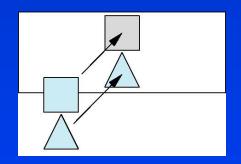
## Easy Cases

- A lies behind all other polygons
  - Can render



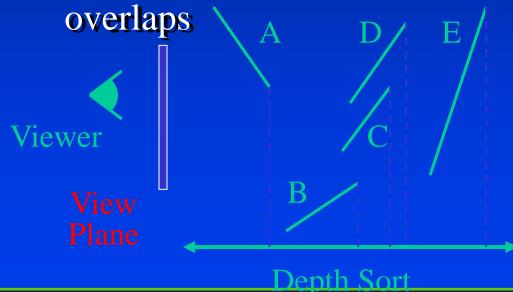
- Polygons overlap in z but not in either x or y
  - Can render independently





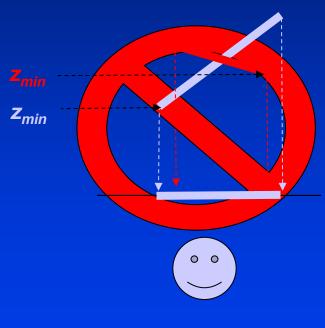
# Depth Sorting Example

- Painter's Algorithm:
  - Sort surfaces in order of decreasing maximum depth
  - Scan convert surfaces in order starting with ones of greatest depth, reordering as necessary based on

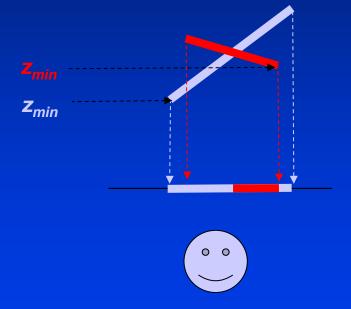


# Painter's Algorithm

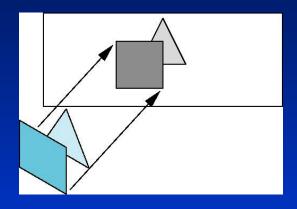
• Problem: Can you get a total sorting?



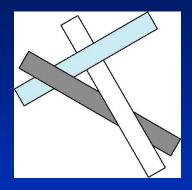




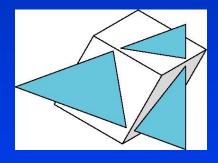
## **Hard Cases**



Overlap in all directions but can one is fully on one side of the other



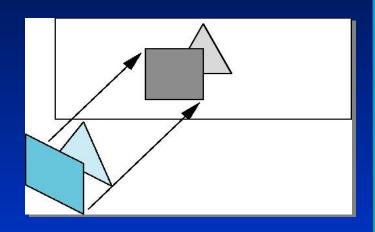
cyclic overlap

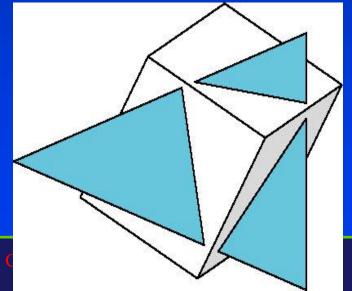


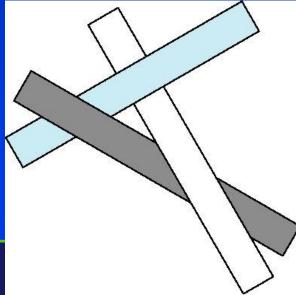
penetration

# Depth-sort Difficulties

- Polygons with overlapping projections
- Cyclic overlap
- Interpenetrating polygons
- What to do?

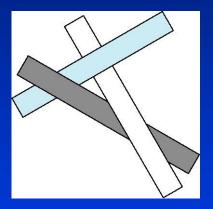






# Painter's Algorithm

- Cyclic Overlap
  - ► How do we sort these three polygons?



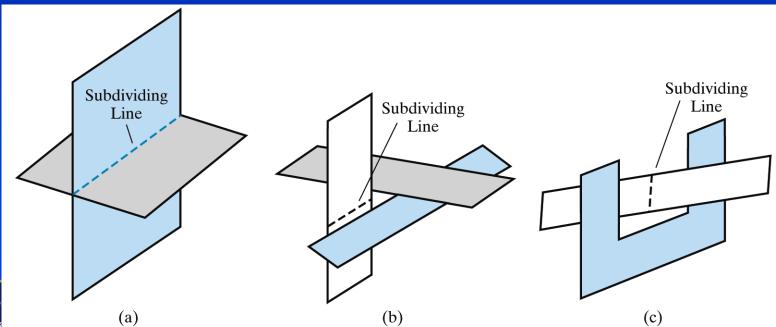
- Sorting is nontrivial
  - > Split polygons in order to get a total ordering
  - Not easy to do in general

# **Depth Sorting**

- Completely in front put in front
- Not overlapping in x, y either
- Intersecting divide along intersection
- overlapping divide along plane of one polygon.

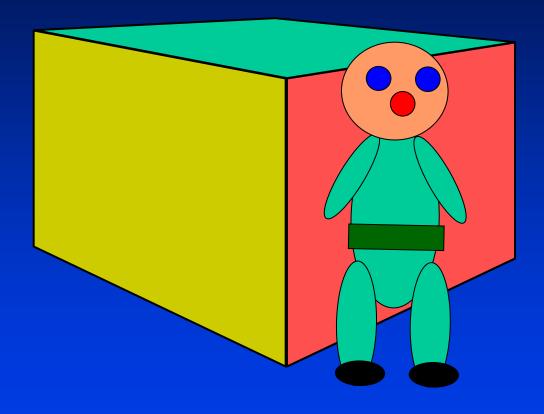
# Depth Sorting

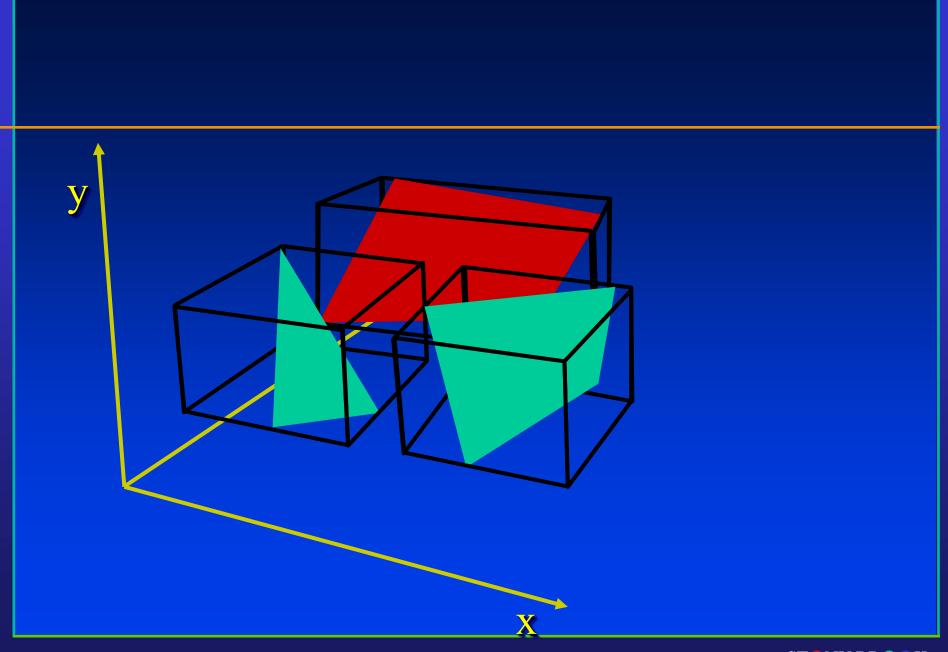
- Cyclically overlapping surfaces that alternately obscure one another
- We can divide the surfaces to eliminate the cyclic overlaps

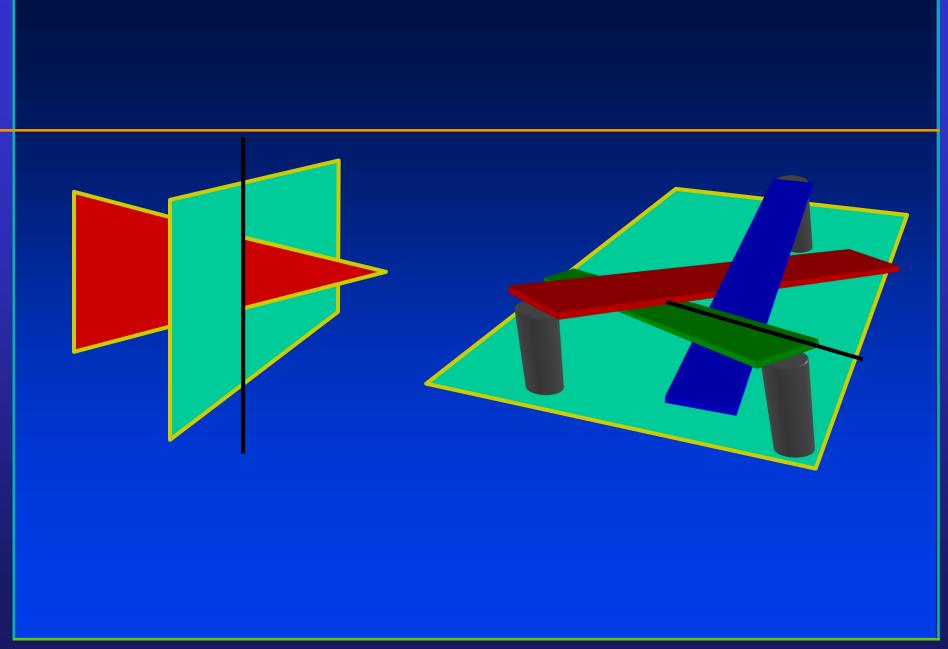




# Painter's Algorithm





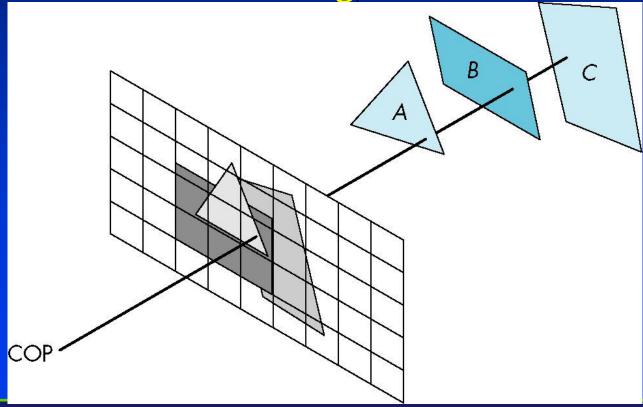


# The Painters Algorithm

- Sort polygons according to their z values and render from back to front
- Ends up drawing over the polygons in the back (more or less)
- Problems arise when polygons overlap or are allowed to pierce one another
- Heedless Painter's Algorithm: sort by "farthest" point and draw in order
- Depth sort improves on this by splitting up overlapping polygons into less ambiguous pieces

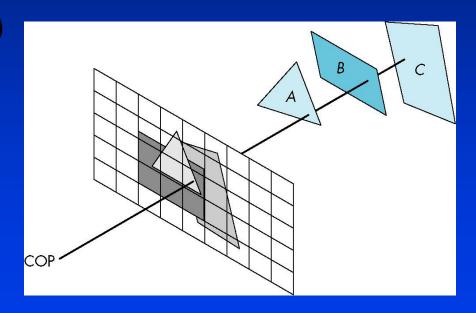
# Visibility

• How do we ensure that closer polygons overwrite further ones in general?



# Image Space Approach

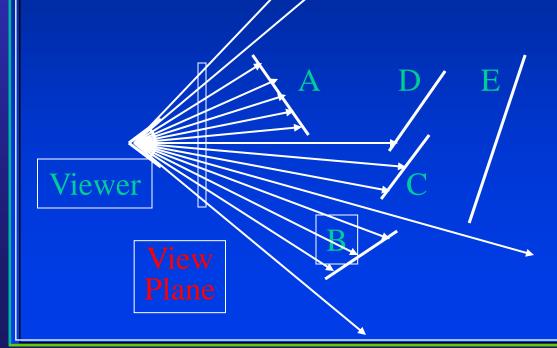
- Look at each projection (nm for an n x m frame buffer) and find closest of k polygons
- Complexity O(nmk)
- Ray tracing
- ·z-buffer



# Ray Casting

#### Algorithm:

 Cast ray from viewpoint through each pixel to find front-most surface



# The Z-buffer Algorithm

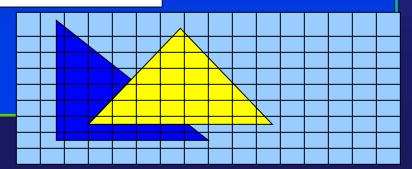
- The most widely-used hidden surface removal algorithm
- Relatively easy to implement in hardware (or software)
- An object-space algorithm which traverses scene and operates per polygon rather than per pixels
- We rasterize polygon by polygon and determine which (parts of) polygons get drawn on the screen
- Relies on a Secondary Buffer called the z-buffer or depth buffer
- Depth buffer has same width and height as the frame-buffer
- Each cell contains the z-value (distance from viewer) of the object at that pixel position

### **Z-Buffer**

- Depth buffer (Z-Buffer)
  - > A secondary image buffer that holds depth values
  - Same pixel resolution as the color buffer
  - > Why is it called a **Z-Buffer**?
    - $\triangleright$  After eye space, depth is simply the z-coordinate
- Sorting is done at the pixel level
  - ➤ Rule: Only draw a polygon at a pixel if it is closer than a polygon that has already been drawn to this pixel

# **Z-Buffer Algorithm**

Visibility testing is done during <u>rasterization</u>



# The Z-buffer Algorithm

1. Initialize all depth(x,y) to 0 and refresh(x,y) to background color

#### 2. For each pixel

1. Get current value depth(x,y)

2. Evaluate depth value z

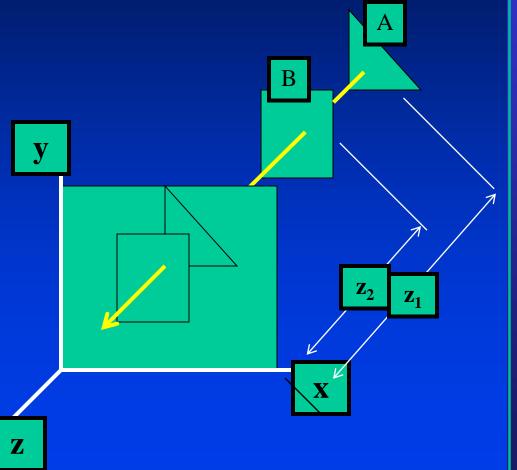
```
if z > depth(x,y)
then
```

**{**[

depth
$$(x,y) = z$$
  
refresh $(x,y) = I_s(x,y)$ 

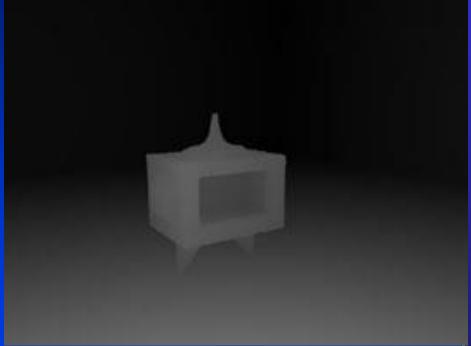
Calculate this using shading algorithm/illumination/fil





# Z-buffer: A Secondary Buffer

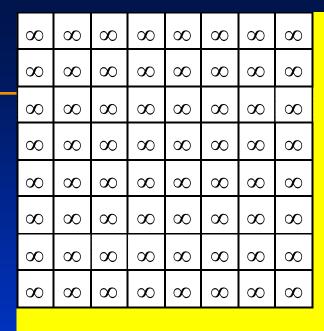




Color buffer

Depth buffer

# Example



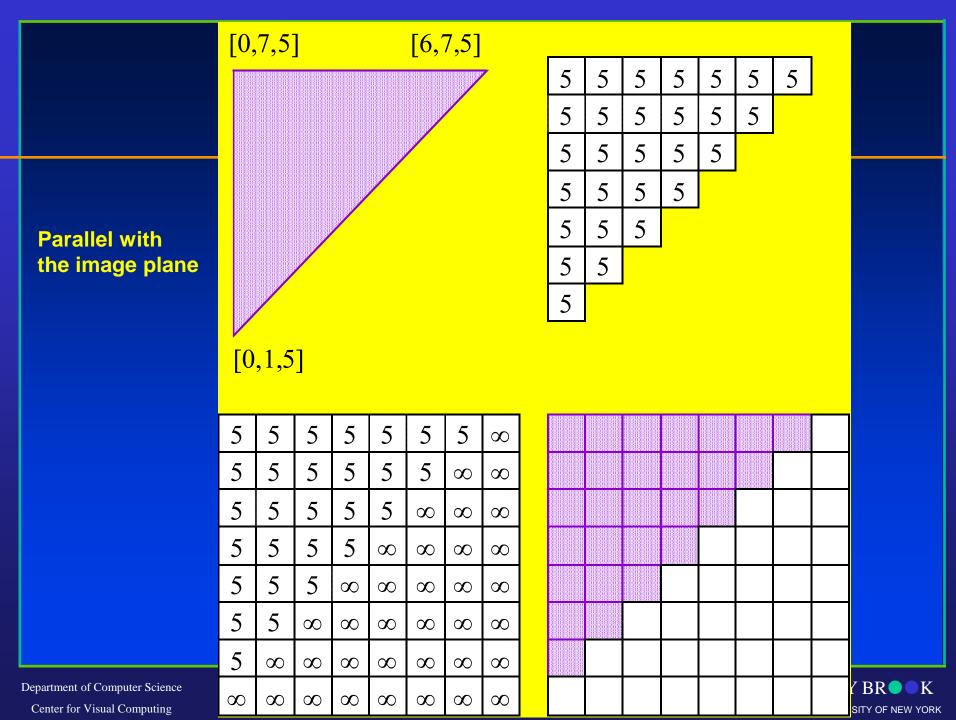
Z-buffer

Screen

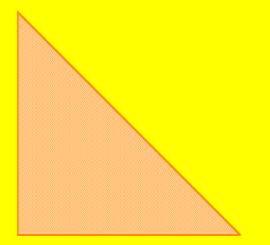
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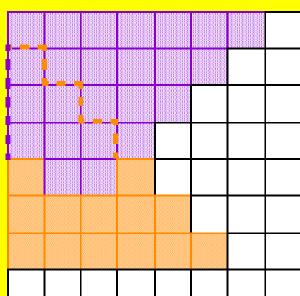




I	7					
	6	7				
	5	6	7			
	4	5	6	7		
	3	4	5	6	7	
	2	3	4	5	6	7

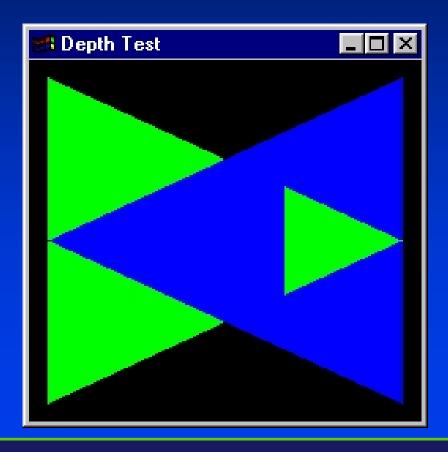
[0,1,2] [5,1,7]

5	5	5	5	5	5	5	$\infty$
5	5	5	5	5	5	8	8
5	5	5	5	5	8	8	8
5	5	5	5	8	8	8	8
4	5	5	7	8	8	8	$\infty$
3	5 4	5 5	<ul><li>7</li><li>6</li></ul>	∞ 7	8 8	8 8	8 8
	5 4 3						



## **Z-Buffer Algorithm**

Algorithm easily handles this case



# Z-buffering in OpenGL

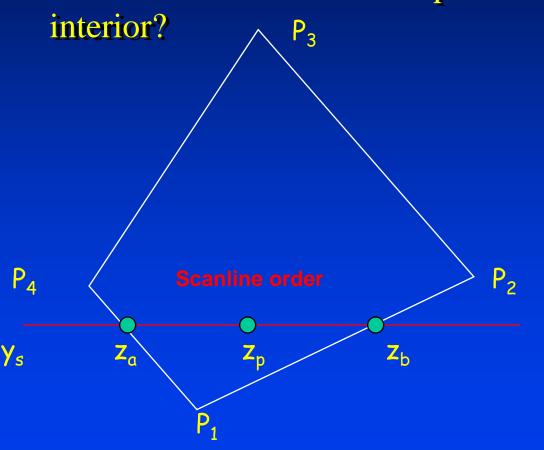
• Create depth buffer by setting GLUT\_DEPTH flag in glutInitDisplayMode() or the appropriate flag in the PIXELFORMATDESCRIPTOR.

- Enable per-pixel depth testing with glenable (GL DEPTH TEST)
- Clear depth buffer by setting

  GL DEPTH BUFFER BIT in glClear()

### **Z-Buffer**

How do we calculate the depth values on the polygon



$$Z_{a} = Z_{1} + (Z_{4} - Z_{1}) \frac{(y_{1} - y_{s})}{(y_{1} - y_{4})}$$

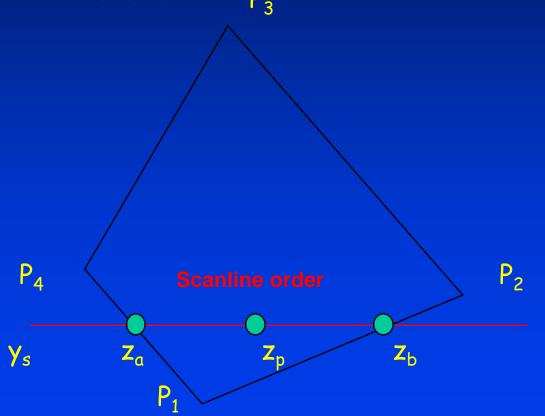
$$Z_{b} = Z_{1} + (Z_{2} - Z_{1}) \frac{(y_{1} - y_{s})}{(y_{1} - y_{2})}$$

$$Z_{p} = Z_{a} + (Z_{b} - Z_{a}) \frac{(x_{a} - x_{p})}{(x_{a} - x_{b})}$$

**Bilinear Interpolation** 

### **Z-Buffer**

How do we calculate the depth values on the polygon interior?



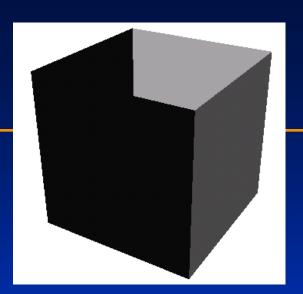
$$Z_{a} = Z_{1} + (Z_{4} - Z_{1}) \frac{(y_{1} - y_{s})}{(y_{1} - y_{4})}$$

$$Z_{b} = Z_{1} + (Z_{2} - Z_{1}) \frac{(y_{1} - y_{s})}{(y_{1} - y_{2})}$$

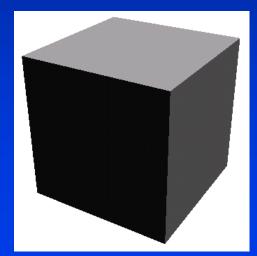
$$Z_{p} = Z_{a} + (Z_{b} - Z_{a}) \frac{(X_{a} - X_{p})}{(X_{a} - X_{b})}$$

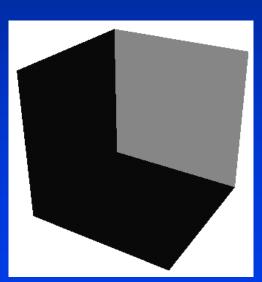
**Bilinear Interpolation** 

Without Hidden surface removal the wrong polygons can be drawn over



With Backface culling





Alternatively we could cull the front faces to see inside the solid

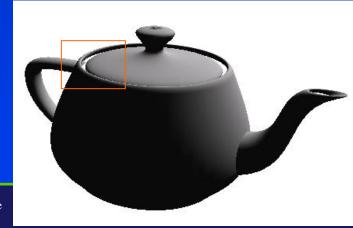


#### No hidden surface removal

Culling can reduce workload for depth testing but we need to ensure that objects are proper **solids**. This teapot is not quite a proper solid and as a result the image is incorrect. However, combining backface culling with more expensive depth-testing is usually a good practice.



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Backface Culling only: correct in some places but not adequate for objects which have holes, are non convex or multiple objects



Depth Testing Only



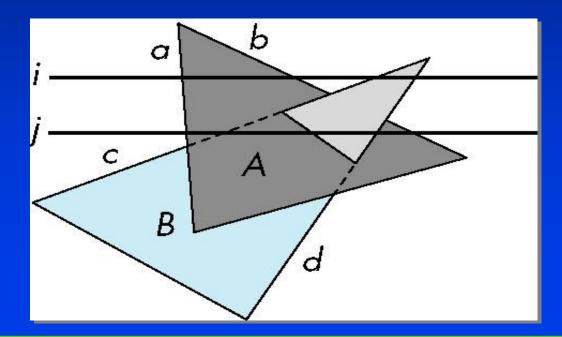
# Scan Line Algorithm

- Similar in some respects to the z-buffer method but handles the image scan-line by scan-line
- Due to coherency in data, this can be relatively efficient
- 1. Rasterize all polygon boundaries (edges)
- 2. Scanning across each scan line we determine the color of each pixel
  - a. By default color everything as background
  - b. If we encounter the edge of one polygon, start evaluating polygon color at each point and shade the scanline accordingly
  - c. For multiple edges do depth evaluation to see which polygon "wins"



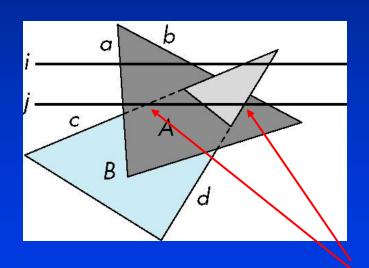
# Scan Line Algorithm

- Work one scan line at a time
- Compute intersections of faces along scanline
- Keep track of all "open segments" and draw the closest



# Scan Line Algorithm

• Can combine shading and hsr through scan line algorithm



scan line i: no need for depth information, can only be in no or one polygon

scan line j: need depth information only when in more than one polygon

#### Scan Conversion

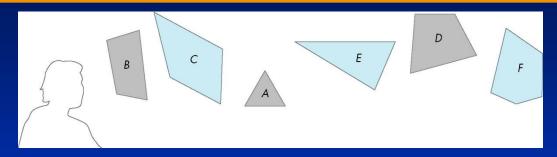
- At this point in the pipeline, we have only polygons and line segments. Render!
- To render, convert to pixels ("fragments") with integer screen coordinates (ix, iy), depth, and color
- Send fragments into fragment-processing pipeline

## Hidden Surface Removal

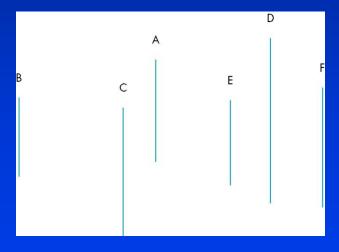
- Object space vs. Image space
- The main image-space algorithm: z-buffer
- Drawbacks
  - Aliasing
  - Rendering invisible objects

• How would object-space hidden surface removal work?

# Simple Example



#### consider 6 parallel polygons

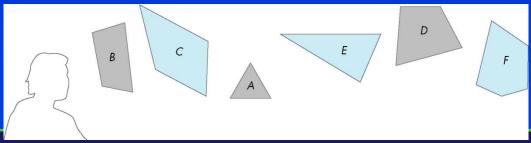


top view

The plane of A separates B and C from D, E and F

# Visibility Testing

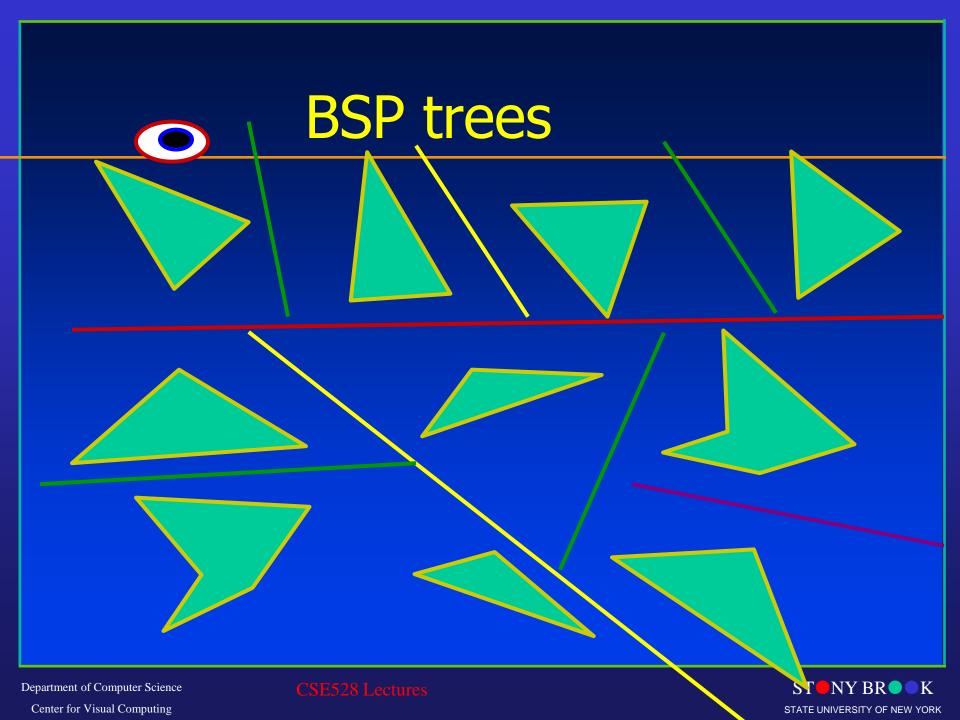
- In many real-time applications, such as games, we want to eliminate as many objects as possible within the application
  - -Reduce burden on pipeline
  - -Reduce traffic on bus
- Partition space with Binary Spatial Partition (BSP) Tree



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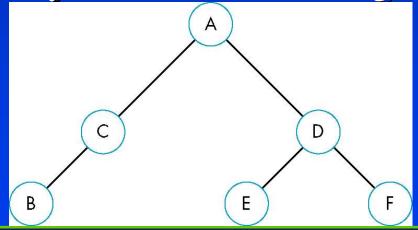
#### Divide Scene with a Plane

- Everything on the same side of that plane as the eye is in front of everything else.
- Divide front and back with more planes.
- If necessary split polygons by planes.



#### **BSP Tree**

- Can continue recursively
  - -Plane of C separates B from A
  - —Plane of D separates E and F
- Can put this information in a BSP tree
  - —Use for visibility and occlusion testing



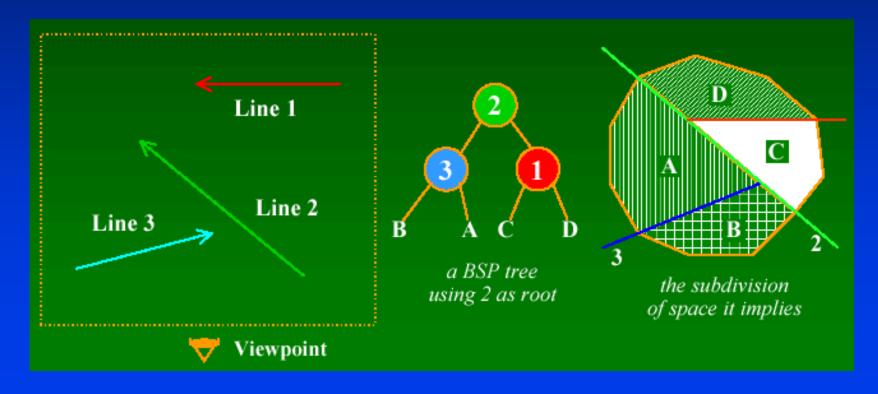
#### **BSP** Tree

- Split space with any line (2D) or plane (3D)
- Applications
  - Painters algorithm for hidden surface removal
  - Ray casting
  - Solid modeling
- Inherent spatial ordering given viewpoint
  - Left subtree: in front
  - right subtree: behind
- Problem: finding good space partitions
  - Proper ordering for the tree
  - Balance tree



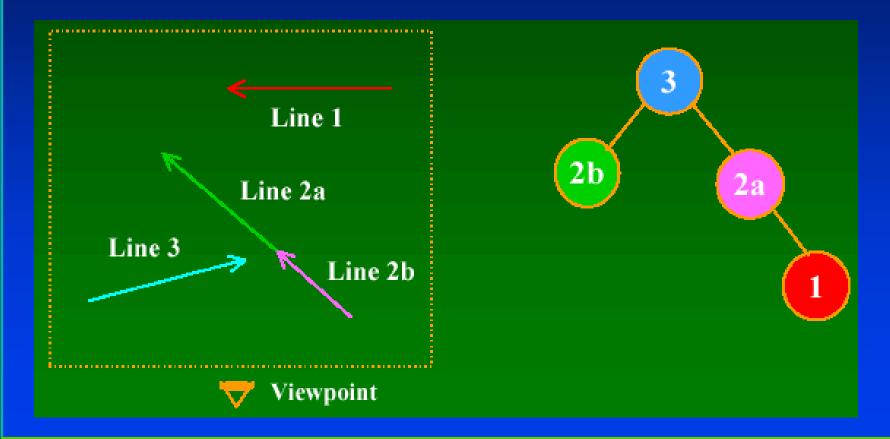
# **Building BSP Trees**

- Use hidden surface removal as intuition
- Using line 1 or line 2 as root is easy



# **Building BSP Trees**

• Using line 3 as root requires splitting



## Building a Good Tree

- Naive partitioning of n polygons yields O(n<sup>3</sup>) polygons (in 3D)
- Algorithms with O(n 2) increase exist
  - Try all, use polygon with fewest splits
  - Do not need to split exactly along polygon planes
- Should balance tree
  - More splits allow easier balancing
  - Rebalancing?

#### Painter's Algorithm with BSP Trees

- Building the tree
  - May need to split some polygons
  - Slow, but done only once
- Traverse back-to-front or front-to-back
  - Order is viewer-direction dependent
  - However, the tree is viewer-independent
  - What is front and what is back of each line changes
  - Determine order on the fly

# Finding the Depth

- Plane equation is Ax + By + Cz + D = 0
- z = -(Ax + By + D)/C
- replace x by x+1
- z' = -(A(x+1) + By + D)/C
- $\square \Delta z = z' z = -A/C'$
- New z is found by adding a constant.

# Details of Painter's Algorithm

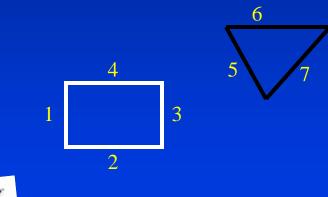
- Each face has form Ax + By + Cz + D
- Plug in coordinates and determine
  - Positive: front side
  - Zero: on plane
  - Negative: back side
- Back-to-front: in-order traversal, farther child first
- Front-to-back: in-order traversal, near child first
- Do backface culling with same sign test
- Clip against visible portion of space (portals)

# Binary Space Partition Trees (1979)

- BSP tree: organize all of space (hence *partition*) into a binary tree
  - Preprocess: overlay a binary tree on objects in the scene
  - Runtime: correctly traversing this tree enumerates objects from back to front
  - Idea: divide space recursively into half-spaces by choosing splitting planes
    - Splitting planes can be arbitrarily oriented

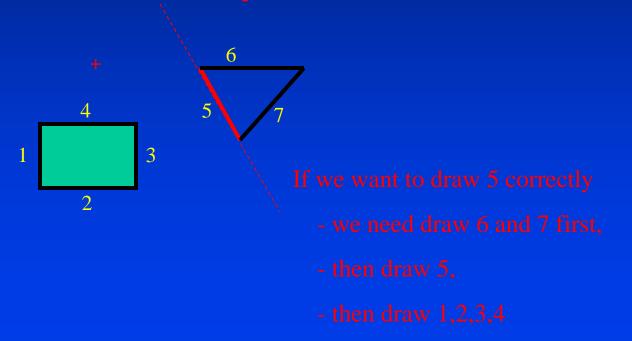
- BSP tree: organize all of space (hence *partition*) into a binary tree
  - Preprocess: overlay a binary tree on objects in the scene
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  - Idea: divide space recursively into half-spaces by choosing splitting planes
    - Splitting planes can be arbitrarily oriented

 Basic idea: Objects in the half space opposite of the viewpoint do not obscure objects in the half space containing the viewpoint; thus, one can safely render them without covering foreground objects

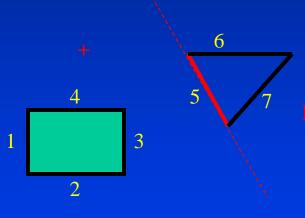


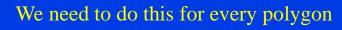


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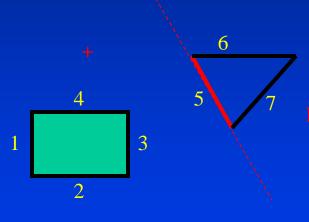


Can we do this efficiently?



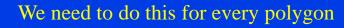
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 Basic idea: Objects in the half space opposite of the viewpoint do not obscure objects in the half space containing the viewpoint; thus, one can safely render them without covering foreground objects



If we want to draw 5 correctly

- we need draw 6 and 7 first,
- then draw 5,
- then draw 1,2,3,4

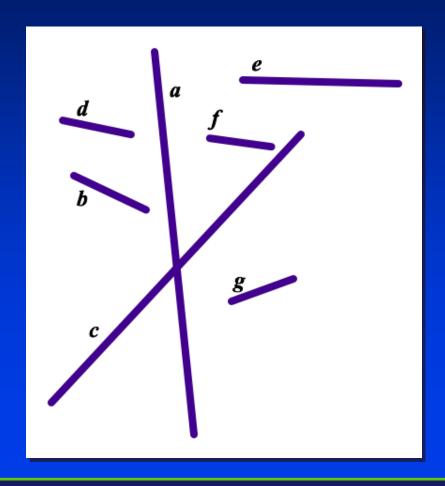


Can we do this efficiently? BSP tree

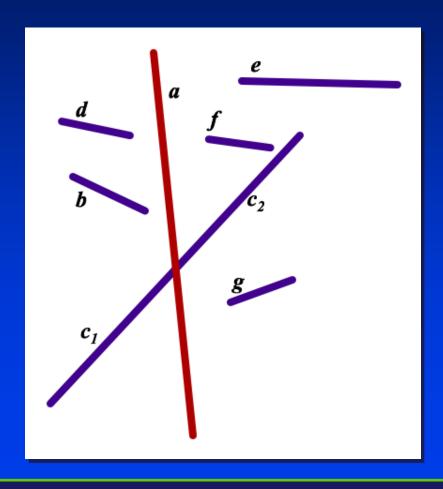


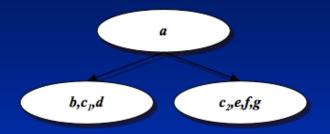
- Binary Space Partition (BSP) Trees
- Split space along planes
- Allows fast queries of some spatial relations
- Simple construction algorithm
- Select a plane as sub-tree root
- Everything on one side to one child
- Everything on the other side to other child
- Use random polygon for splitting plane

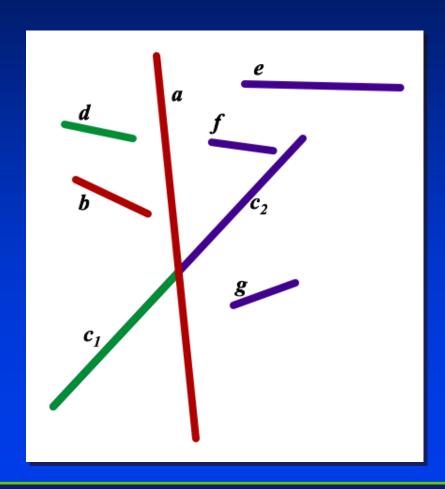
# BSP-Trees (One Example)

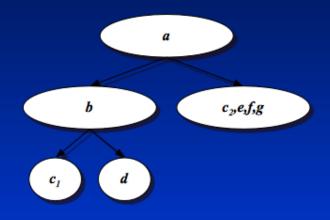


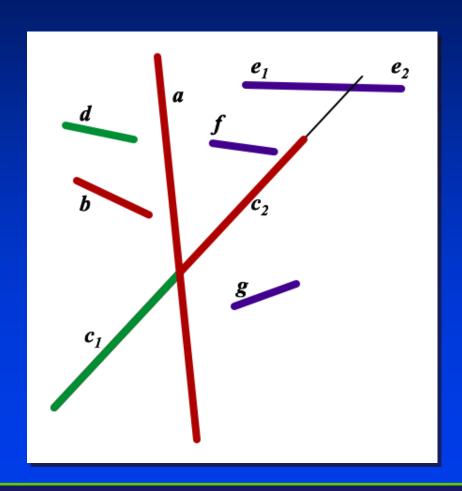
a,b,c,d,e,f,g

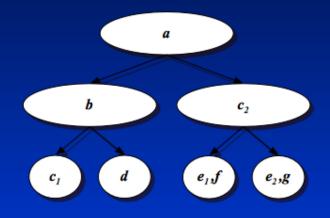


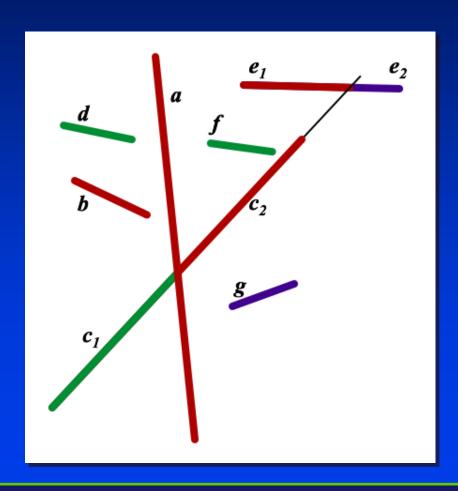


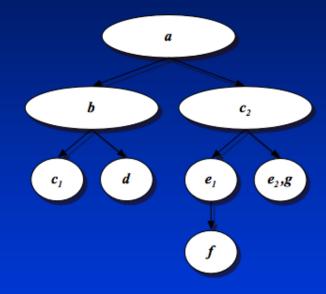


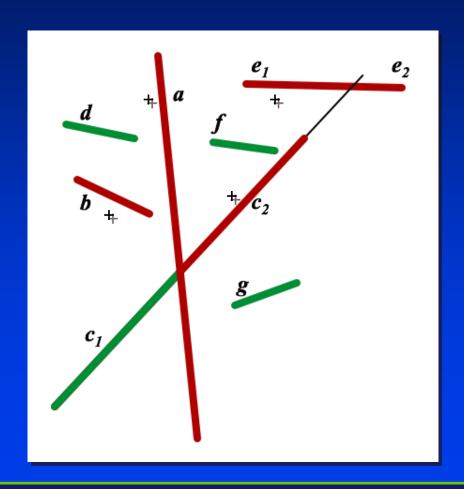


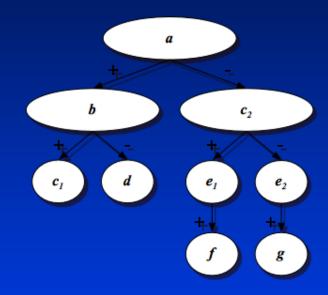






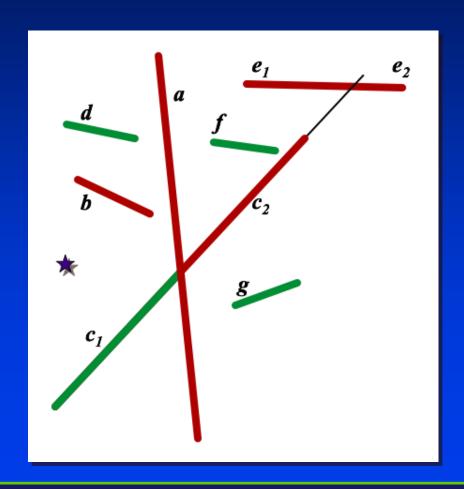


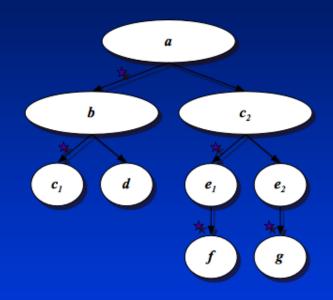




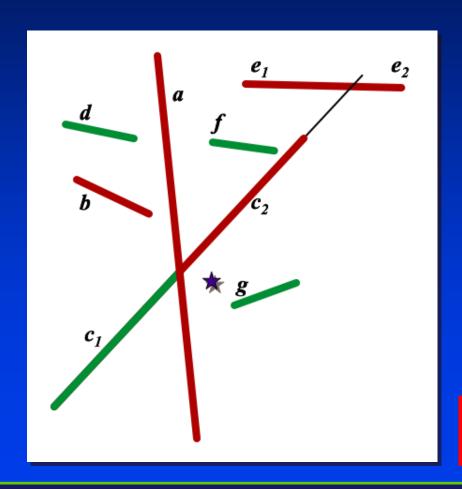
#### How Do We Traverse BSP Tree?

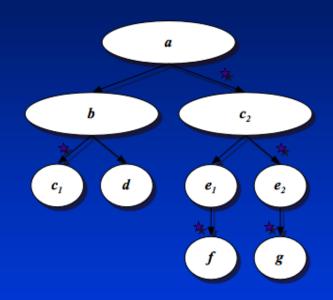
- Visibility traversal based on BSP tree
- -Variation of in-order-traversal
- Child one
- •Sub-tree root
- •Child two
- -Select "child one" based on location of viewpoint
- •Child one on same side of sub-tree root as viewpoint





 $c_1$ :b:d:a:f: $e_1$ : $c_2$ :g: $e_2$ 

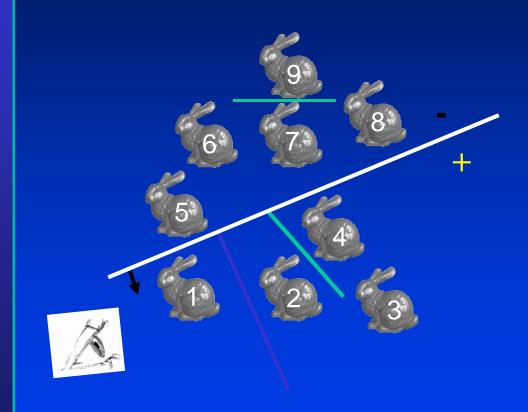


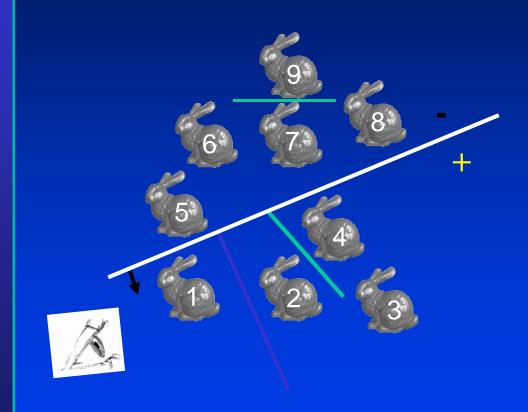


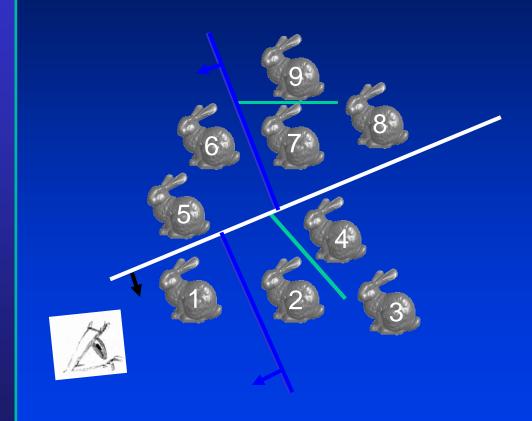
 $g:e_2:c_2:f:e_1:a:c_1:b:d$ 

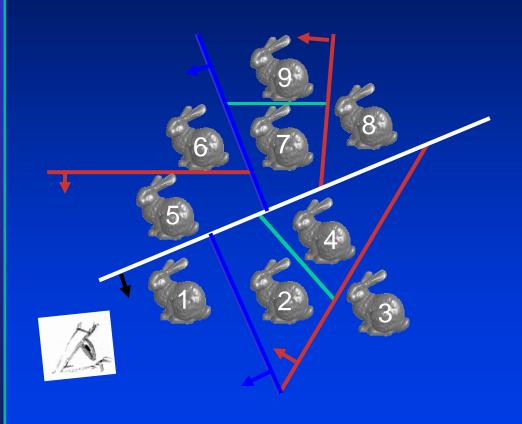
## BSP Trees: Another Example

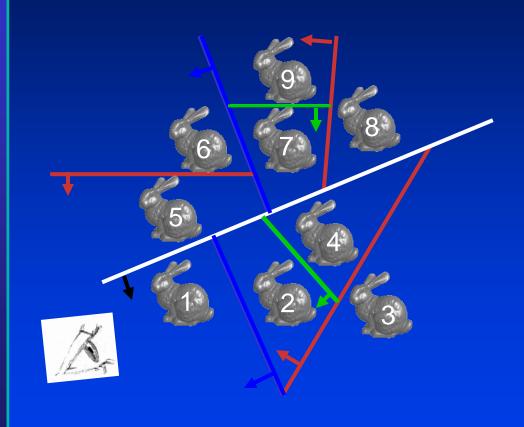


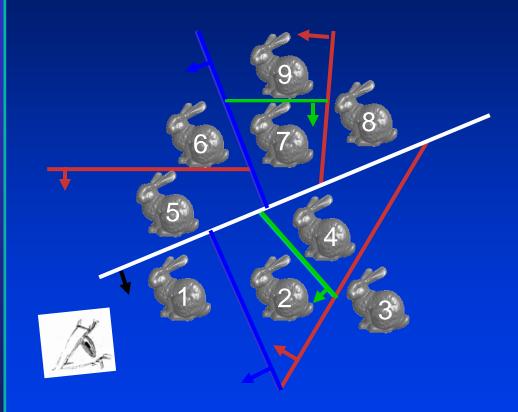








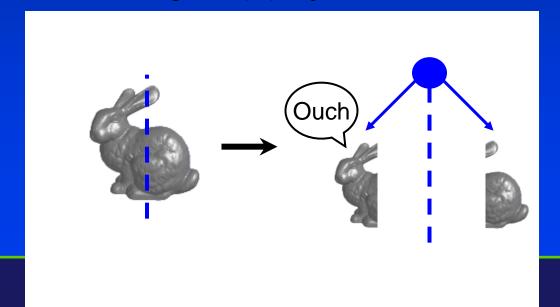




When to stop the recursion?

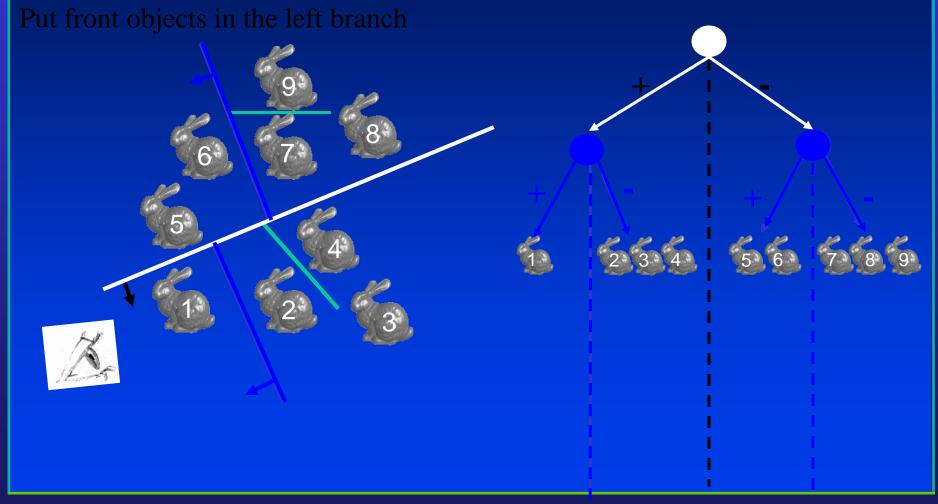
# **Object Splitting**

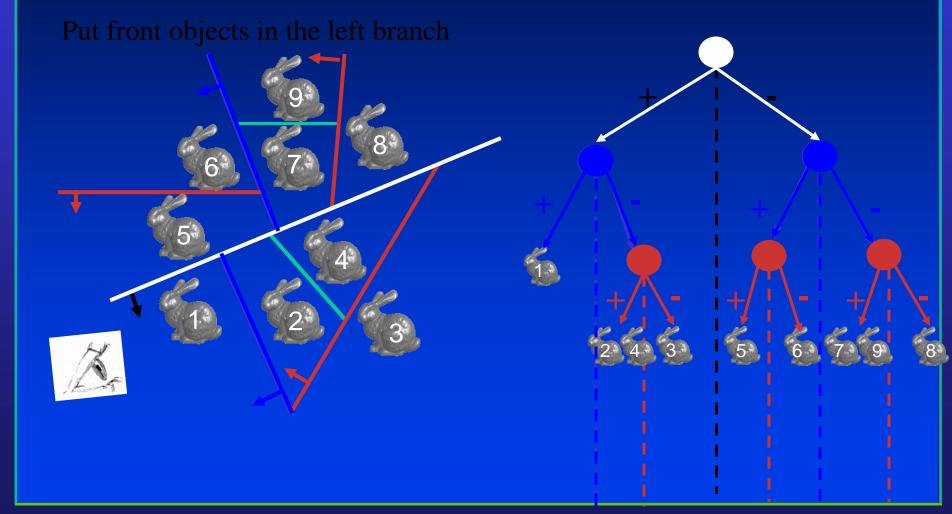
- No bunnies were harmed in my example
- But what if a splitting plane passes through an object?
  - Split the object; give half to each node:
  - Worst case: can create up to O(n<sup>3</sup>) objects!

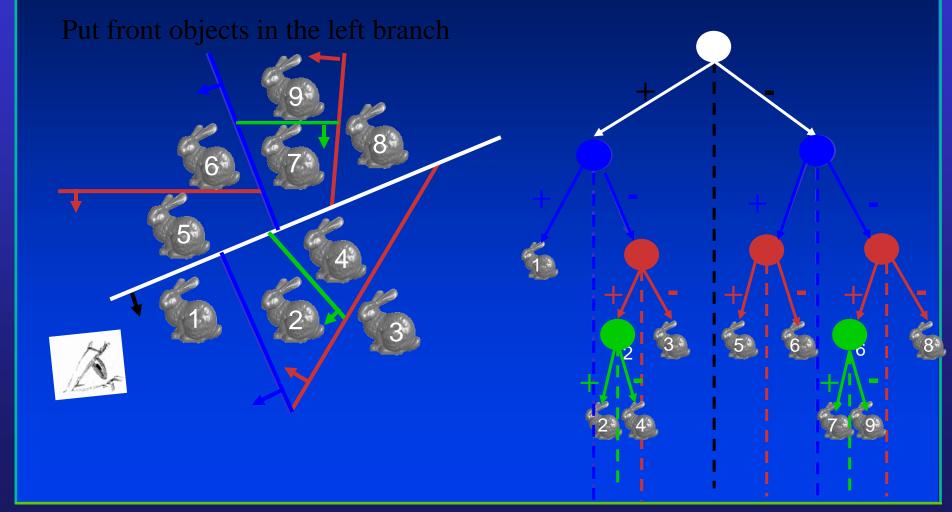


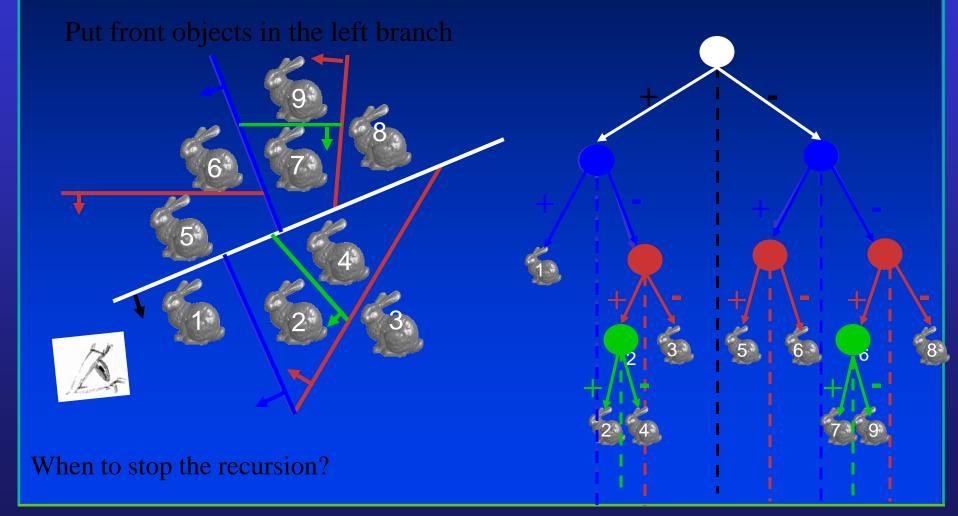
# Polygons: BSP Tree Construction

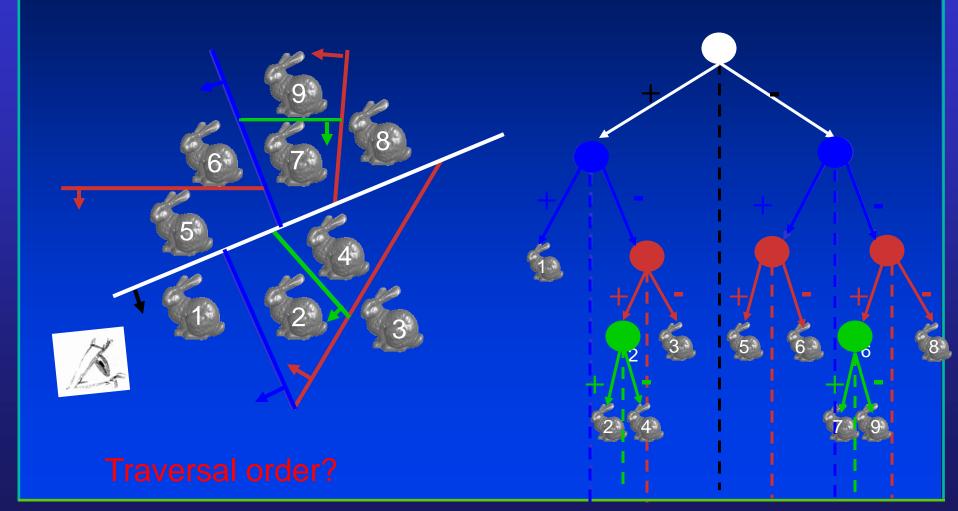
- Split along the plane containing any polygon
- Classify all polygons into positive or negative half-space of the plane
  - If a polygon intersects plane, split it into two
- Recursion down the negative half-space
- Recursion down the positive half-space

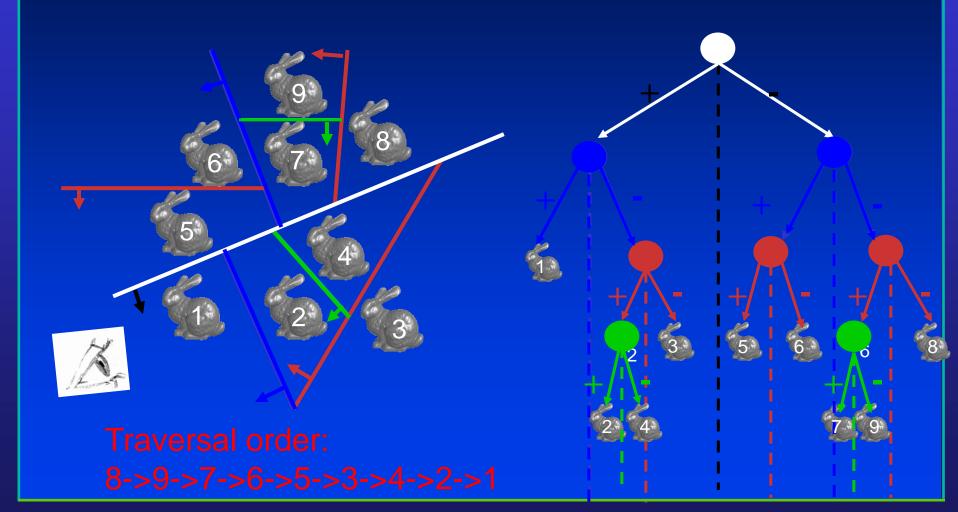








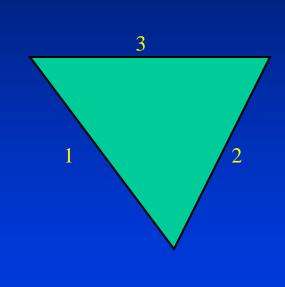


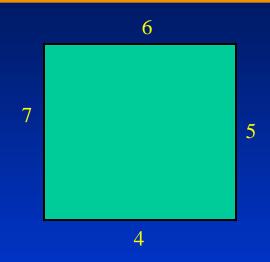


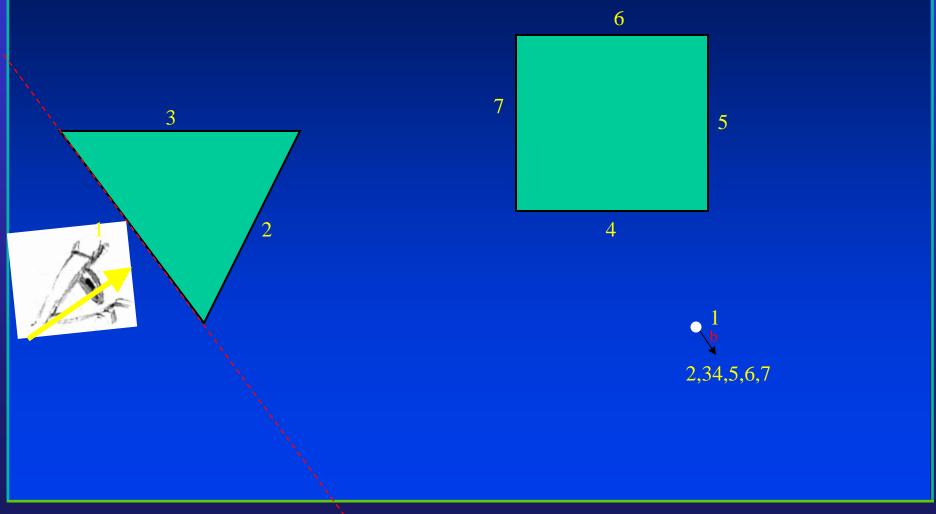
### Building a BSP Tree for Polygons

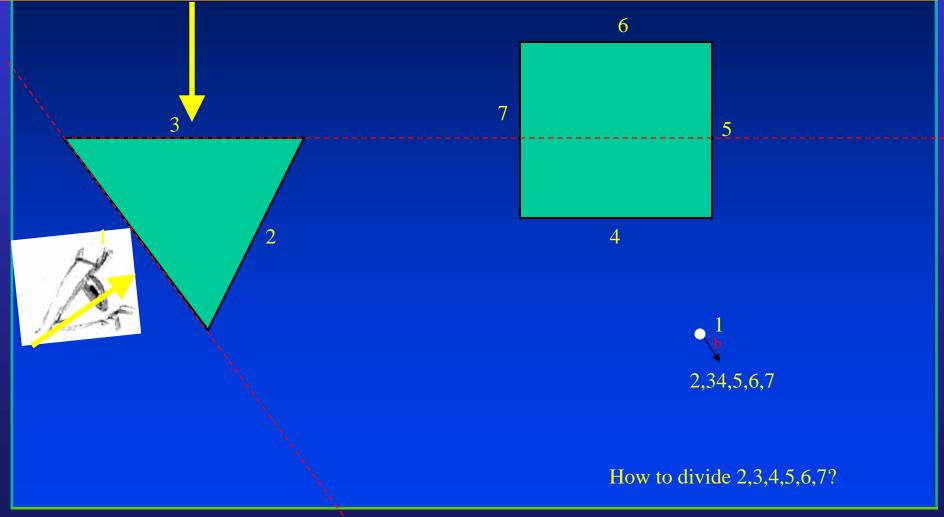
- Choose a splitting polygon
- Sort all other polygons as
  - Front
  - Behind
  - Crossing
  - On
- Add "front" polygons to front child, "behind" to back child
- Split "crossing" polygons with infinite plane
- Add "on" polygons to root
- Recursion until all polygons are processed

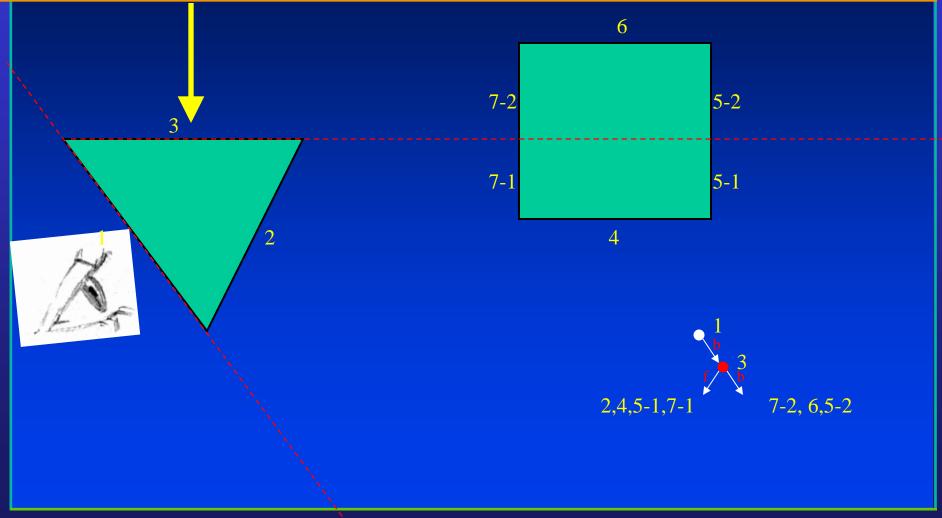
# Building a BSP Tree: Another Example



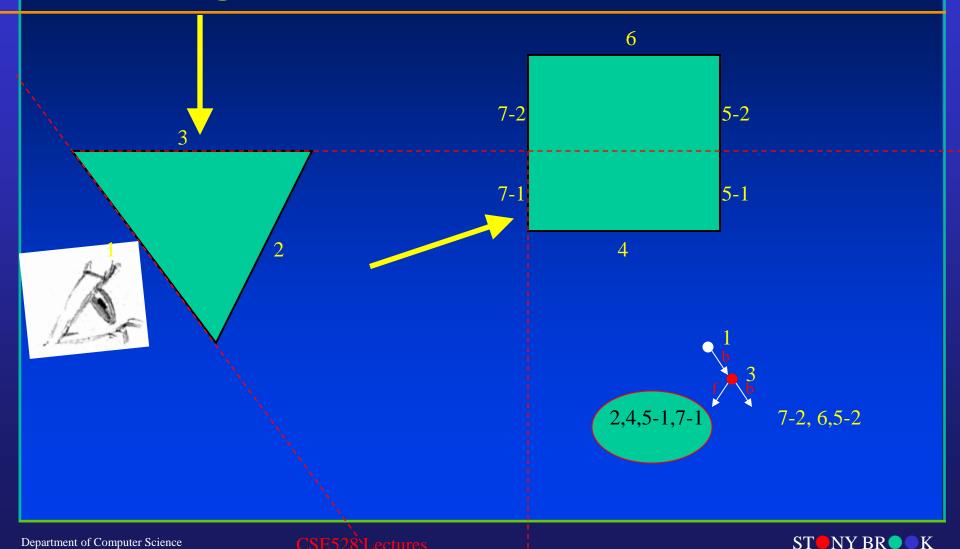




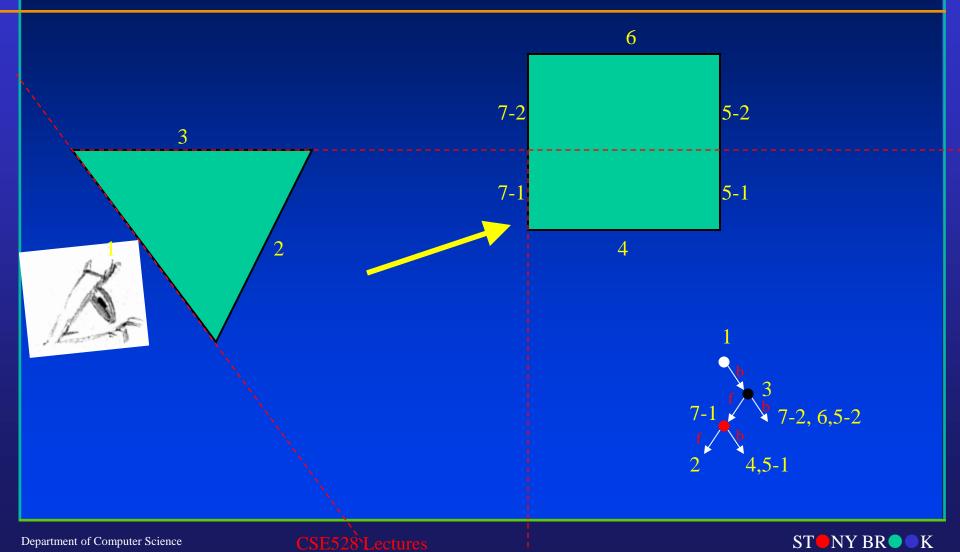




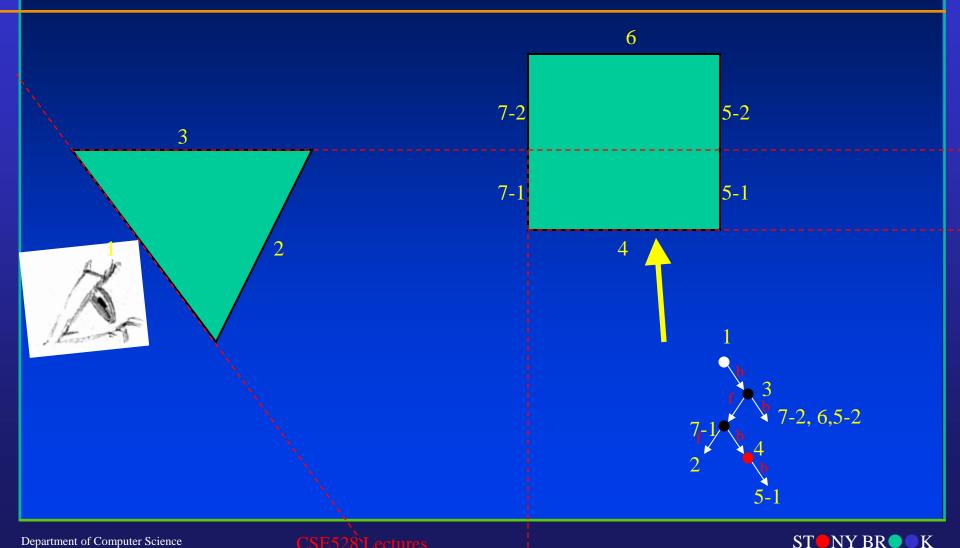
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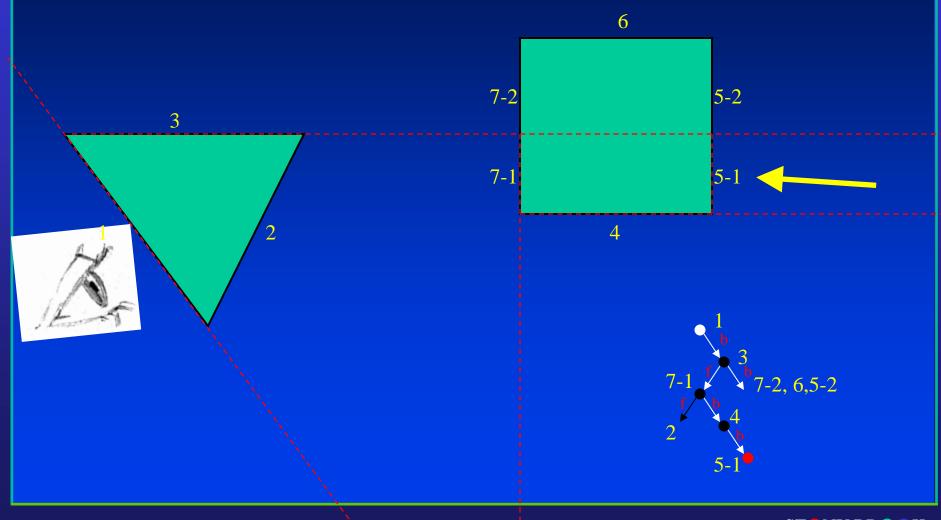


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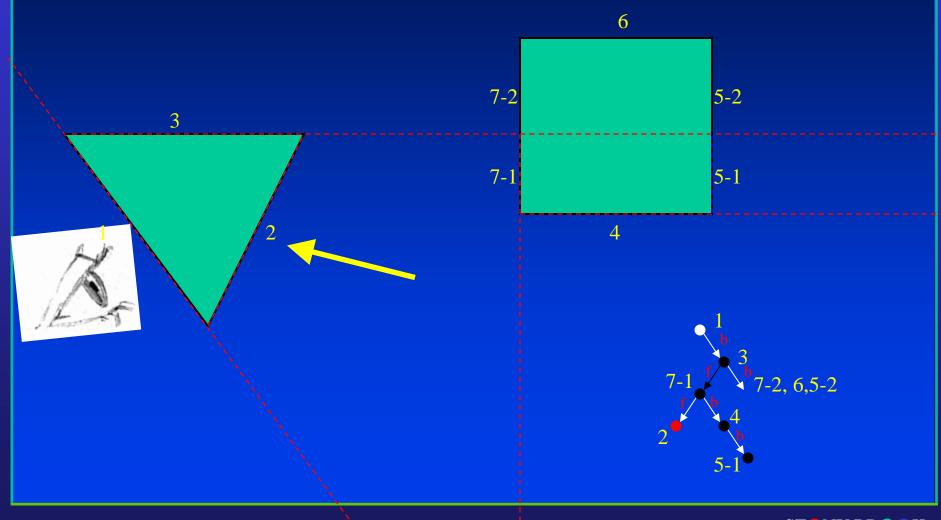
Center for Visual Computing





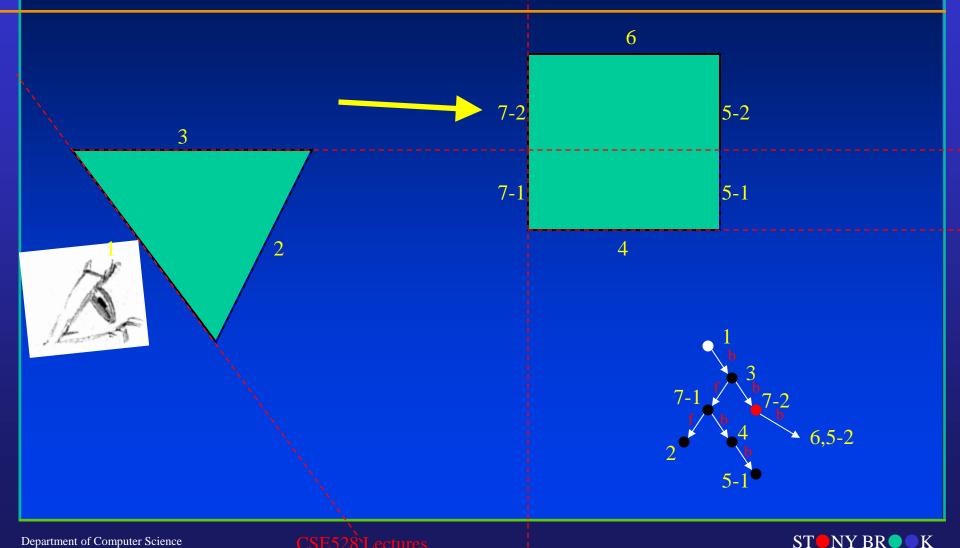
Department of Computer Science Center for Visual Computing CSE528'Lectures



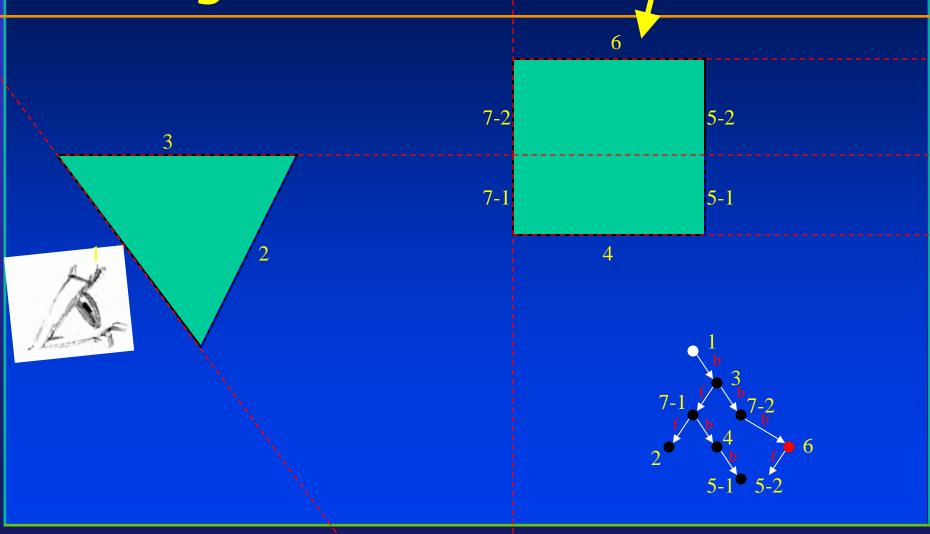


Department of Computer Science Center for Visual Computing CSE528'Lectures

Center for Visual Computing

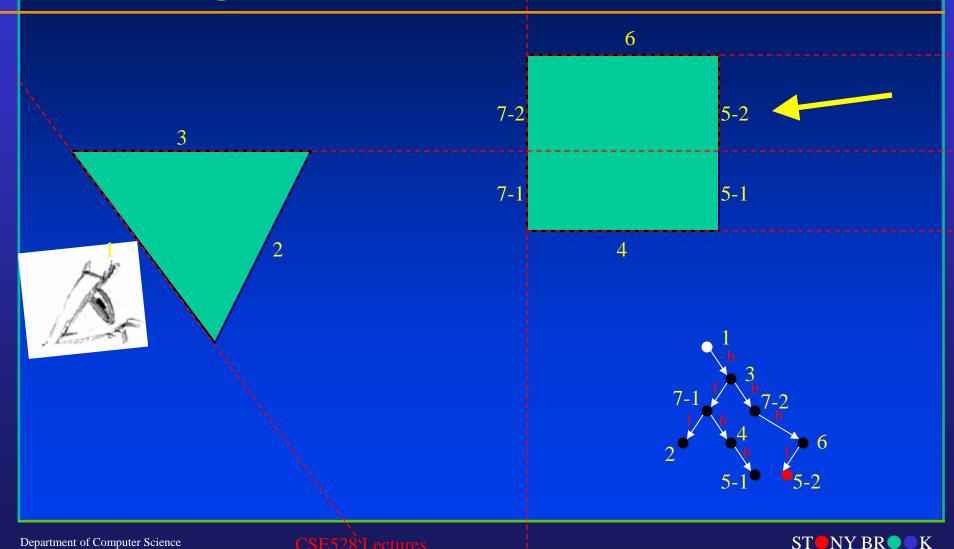


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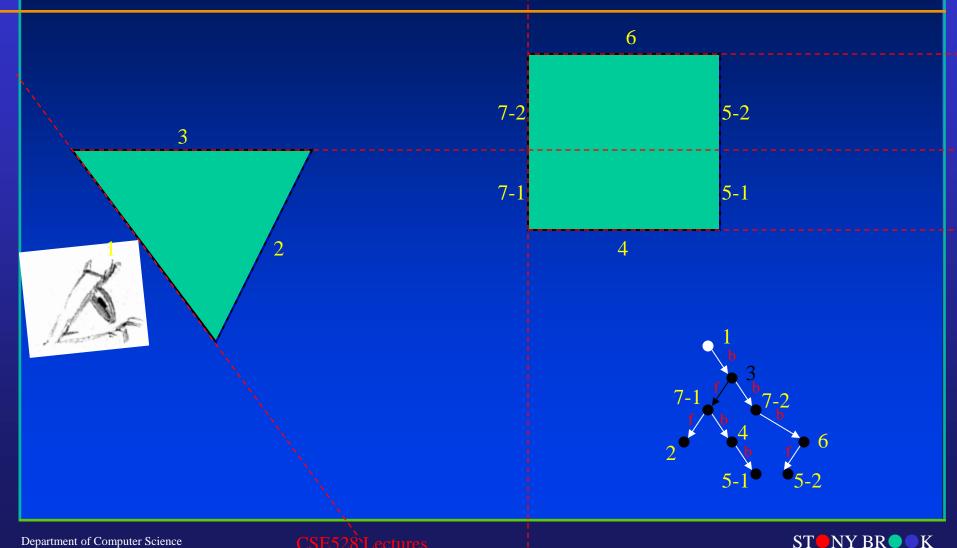


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### Rendering with a BSP Tree

#### • If eye is in front of plane

- Draw "back" polygons
- Draw "on" polygons
- Draw "front" polygons

#### If eye is behind plane

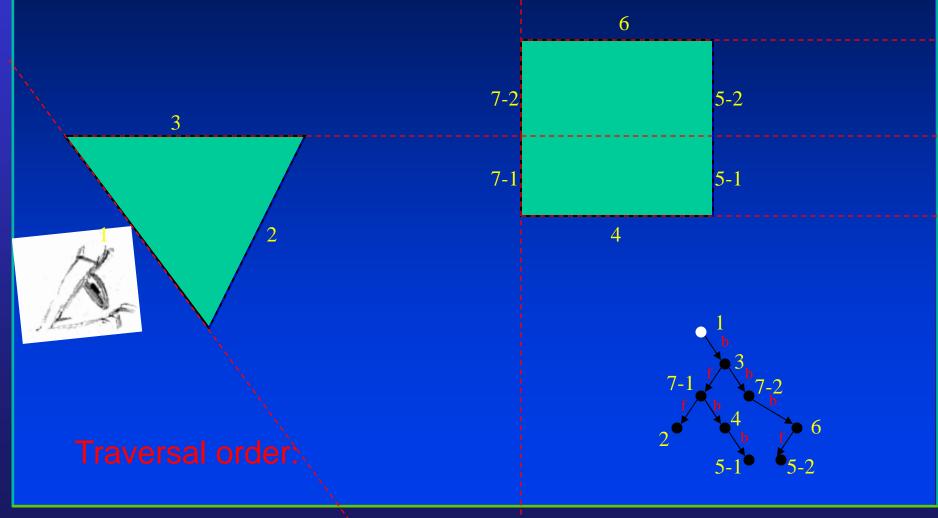
- Draw "front" polygons
- Draw "on" polygons
- Draw "back" polygons

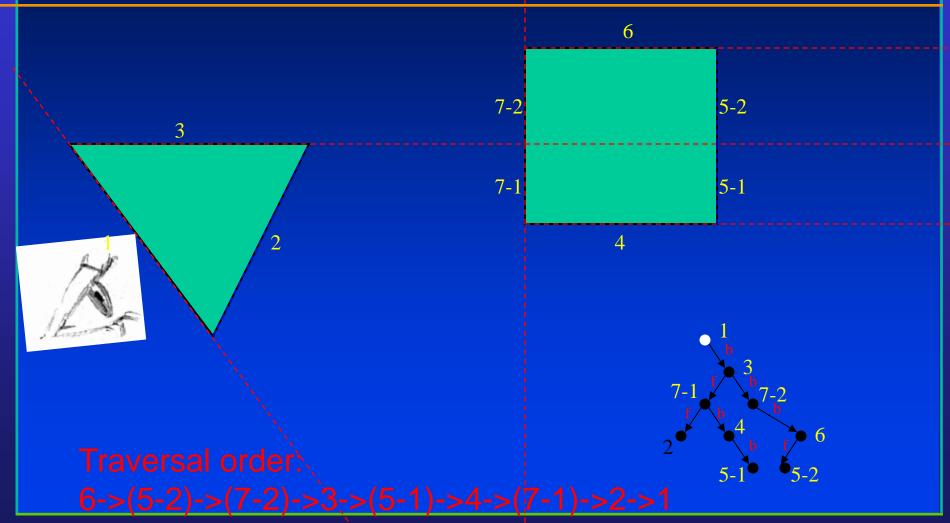
#### Else eye is on plane

- Draw "front" polygons
- Draw "back" polygons



# Building a BSP Tree: Another Example

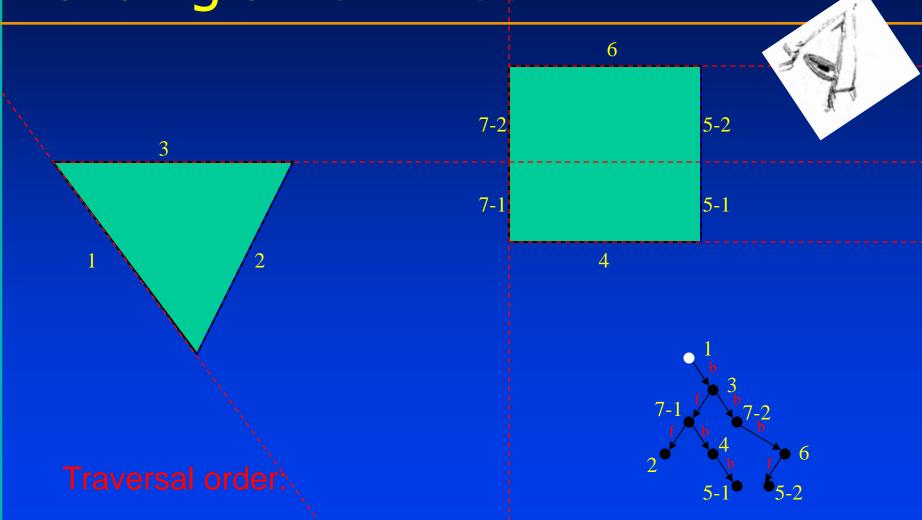


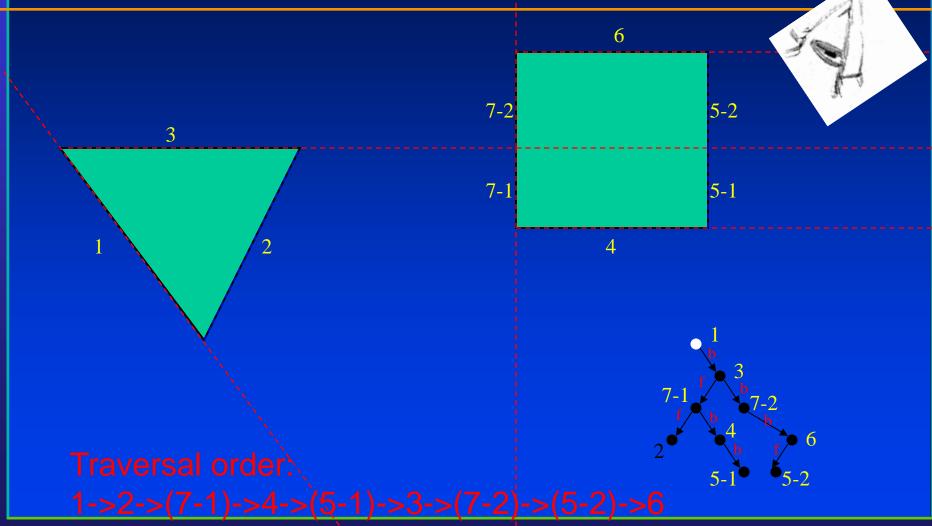


Department of Computer Science Center for Visual Computing

CSE528'Lectures

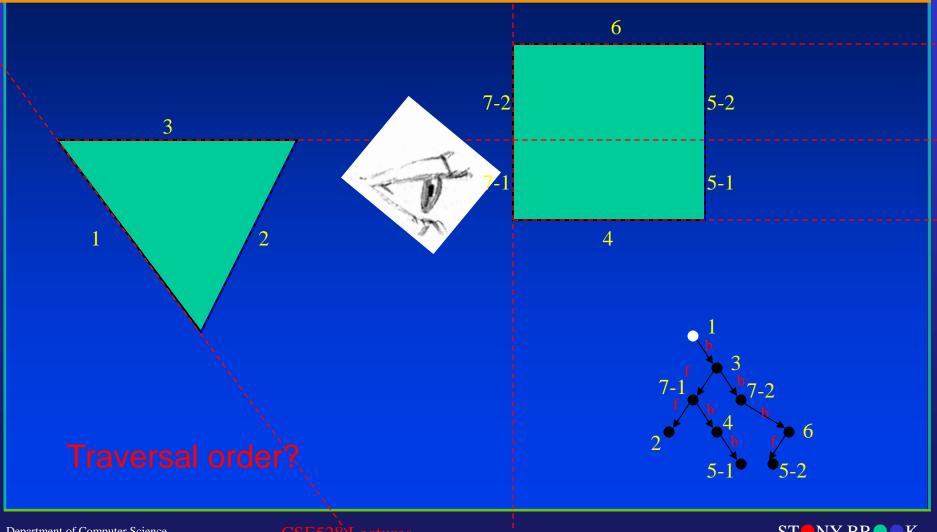






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### Summary: BSP Trees

#### • Pros:

- Simple, elegant scheme
- No depth comparisons needed
- Polygons split and ordered automatically
- Only writes to framebuffer (i.e., painters algorithm)

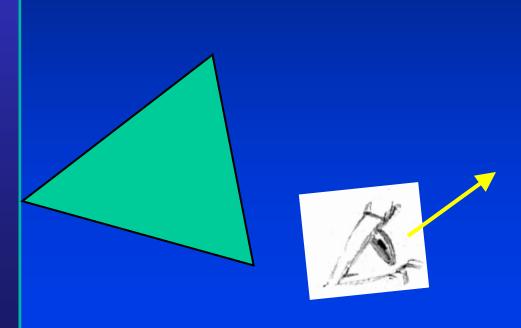
### Summary: BSP Trees

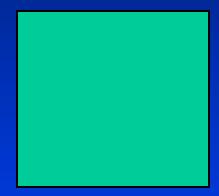
#### • Cons:

- Computationally intense preprocess stage restricts algorithm to static scenes
- Splitting increases polygon count
- Redraws same pixel many times
- Choosing splitting plane not an exact science

### Improved BSP Rendering

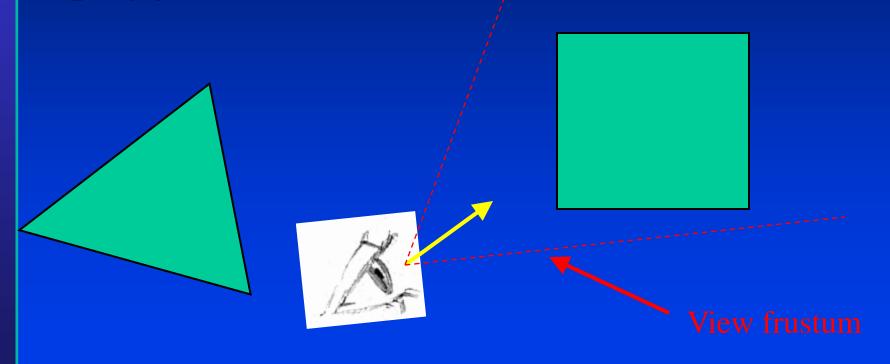
 Take advantage of view direction to cull away polygons behind viewer



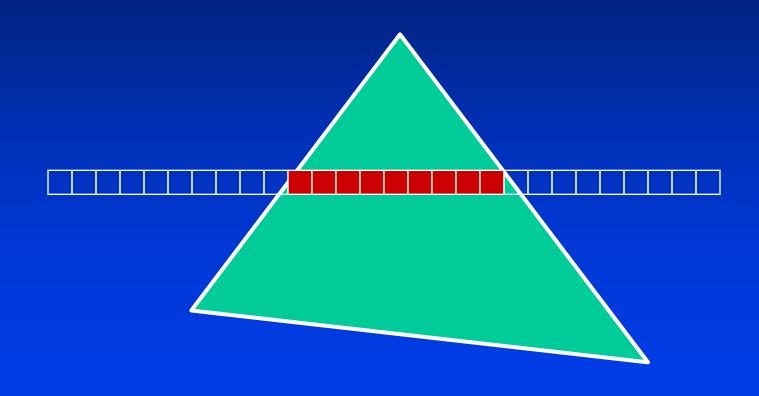


## Improved BSP Rendering

 Take advantage of view direction to cull away polygons behind viewer



# Scan Line in Screen Space

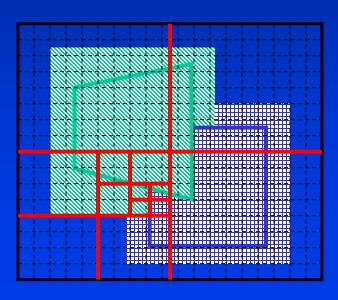


### **Z-Buffer**

- Record r, g, b and z (depth) for each pixel.
- Process each polygon line by line and if closer replace r, g, b, z in the buffer.

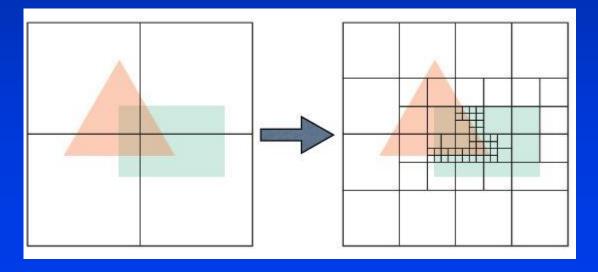
### Area Subdivision

- Fill area if:
  - All surfaces are outside
  - Only one surface intersects
  - One surface occludes other surfaces within area.
- Otherwise, subdivide



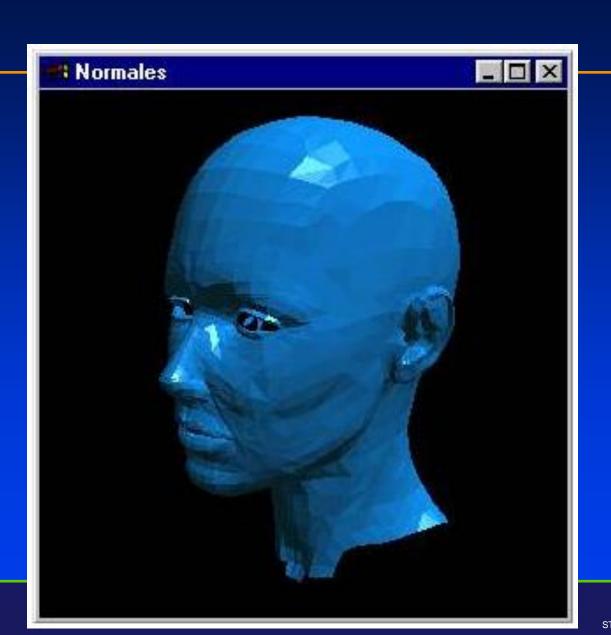
### Warnock Algorithm

• Takes advantage of *area coherence*: divide the display area into successively smaller rectangles until the entire rectangle can be filled with a single color



### The Warnock's Algorithm

• The Warnock algorithm divides the screen into smaller areas and sorts triangles within these areas. If there is ambiguity (i.e., polygons overlap in depth extent within these areas), then further subdivision occurs. At the limit, subdivision may occur down to the pixel level.

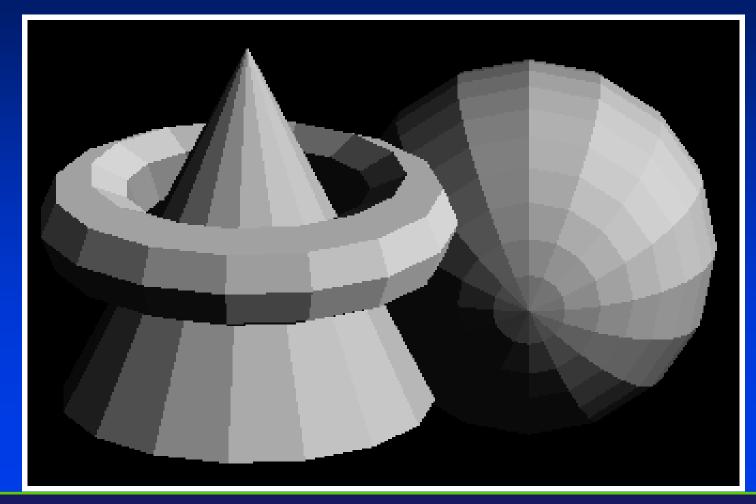


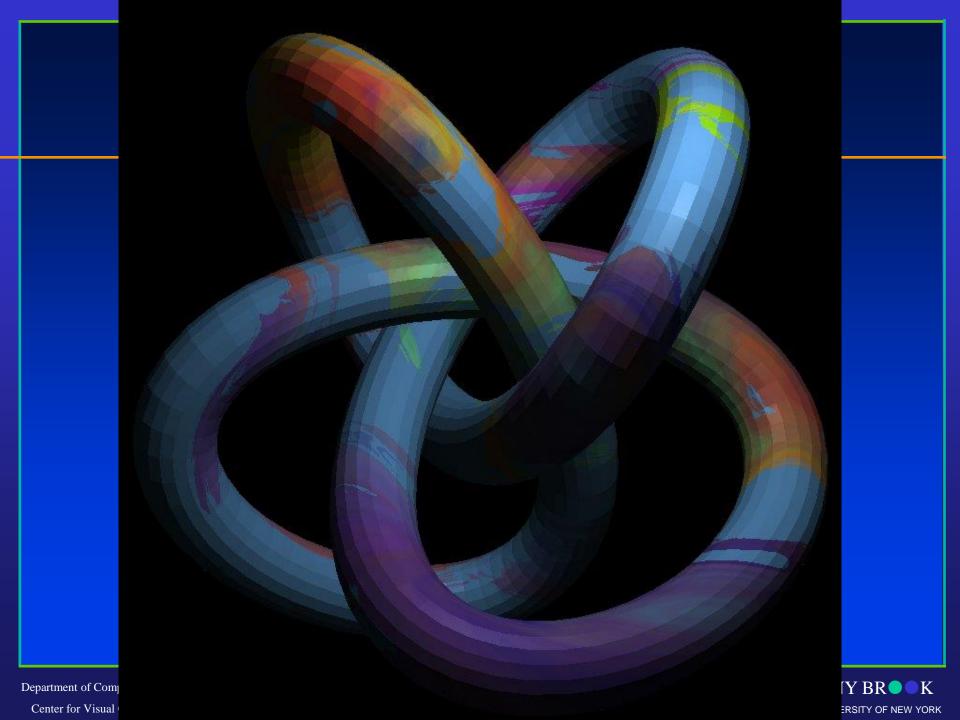
Department of Computer Science Center for Visual Computing STONY BROOK

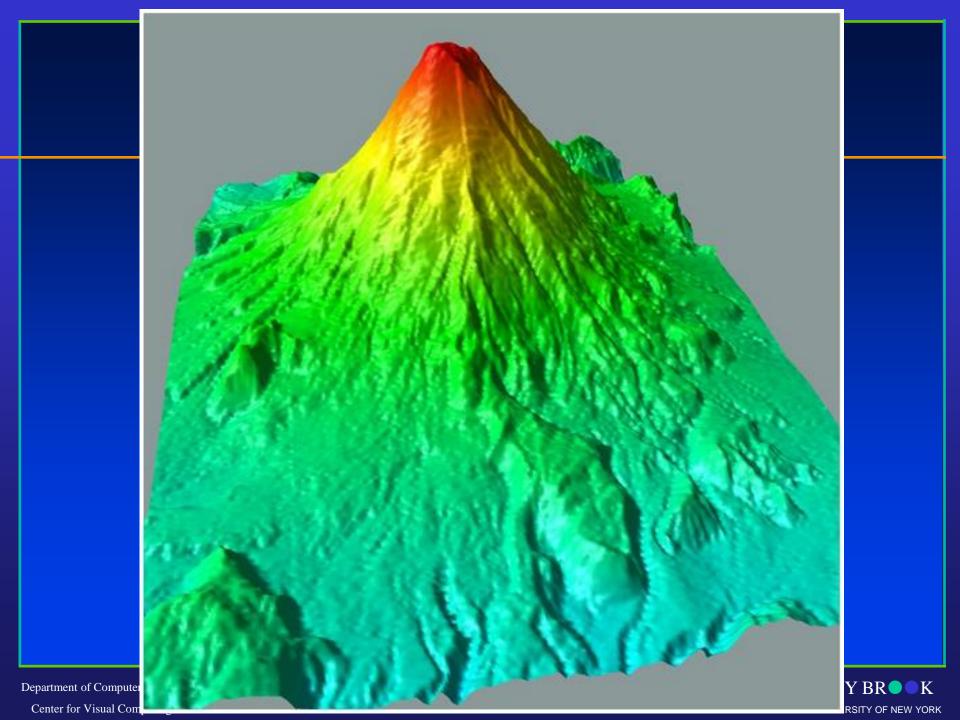


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