Hashing

CSE260, Computer Science B: Honors
Stony Brook University

http://www.cs.stonybrook.edu/~cse260
Objectives

- To understand what hashing is and what hashing is used for
- To obtain the hash code for an object and design the hash function to map a key to an index
- To handle collisions using open addressing
- To know the differences among linear probing, quadratic probing, and double hashing
- To handle collisions using separate chaining
- To understand the load factor and the need for rehashing
- To implement MyHashMap using hashing
- To implement MyHashSet using hashing
Hashing and Maps

• Why hashing?
  • O(1) time to search, insert, and delete an element in a map or a set vs. O(logn) time in a well-balanced search tree

• A map (aka. dictionary, a hash table, or an associative array) is a data structure that stores entries, where each entry contains two parts: key (also called a search key) and value
  • The key is used to search for the corresponding value
  • For example, a dictionary can be stored in a map, where the words are the keys and the definitions of the words are the values
import java.util.HashMap;

public class HashMapDemo {
    public static void main(String[] args) {
        HashMap<String, Integer> map;
        map = new HashMap<>();
        map.put("Smith", 30);
        map.put("Anderson", 31);
        map.put("Lewis", 29);
        map.put("Cook", 29);
        map.put("Smith", 65);
        System.out.println("Entries in map: " + map);
        System.out.println("The age for " + "Lewis is " + map.get("Lewis"));
        System.out.println("Is Smith in the map? " + map.containsKey("Smith");
        System.out.println("Is age 33 in the map? " + map.containsValue(33));
        map.remove("Smith");
        System.out.println("Entries in map: " + map);
        map.clear();
        System.out.println("Entries in map: " + map);
    }
}
Hashing

- If you know the index of an element in the array, you can retrieve the element using the index in $O(1)$ time
- So, can we store the values in an array and use the key as the index to find the value?
- The answer is yes if you can map a key to an index
- The array that stores the values is called a hash table
- The function that maps a key to an index in the hash table is called a hash function
- Hashing is a technique that retrieves the value using the index obtained from key without performing a search
Hash Functions and Hash Codes

• A typical *hash function* first converts a search key to an *integer* value called a *hash code*, then compresses the hash code into an index to the hash table.

• Java’s root class *Object* has the *hashCode* method, which returns an integer hash code — by default, the method returns the *memory address* for the object.

• You should override the *hashCode* method whenever the *equals* method is overridden to *ensure that two equal objects return the same hash code*.

• During the execution of a program, invoking the *hashCode* method multiple times on the same object returns the same integer, provided that the object’s data are not changed.

• Two unequal objects may have the same hash code, but you should implement the *hashCode* method to avoid too many such cases.
Hash Codes for Primitive Types

- The types `byte`, `short`, `int`, and `char` are simply casted into `int`
  - two different search keys of any one of these types will have different hash codes
- For a search key of the type `float`, return an `int` value whose bit representation is the same as the bit representation for the floating number
  - use `Float.floatToIntBits(key)` to get the the hash code
- For a search key of the type `long`, simply casting it to `int` would not be a good choice, because all keys that differ in only the first 32 bits will have the same hash code

```java
System.out.println((int)(4294967296L)); // 0
System.out.println((int)(4294967297L)); // 1
System.out.println((int)(4294967298L)); // 2
System.out.println((int)(4294967299L)); // 3
```
- Divide the 64 bits into two halves and perform the exclusive or operation to combine the two halves (this process is called `folding`)

```java
hashCode = (int)(key ^ (key >> 32));
```

1010110 ^ 0110111 yields 1100001
Hash Codes for Primitive Types

- For a search key of the type `double`, first convert it to a `long` value using the `Double.doubleToLongBits` method, and then perform a folding as follows:

```java
long bits = Double.doubleToLongBits(key);
int hashCode = (int)(bits ^ (bits >> 32));
```
An intuitive approach is to sum the Unicode of all characters as the hash code for the string.

This approach may work if two search keys in an application don’t contain the same letters, but it fails otherwise, e.g., `tod` and `dot`.

A better approach is to generate a hash code that takes the position of characters into consideration:

\[ s_0 \cdot b^{(n-1)} + s_1 \cdot b^{(n-2)} + \ldots + s_{n-1} \]

where \( s_i \) is `s.charAt(i)`.

Using Horner’s rule for polynomial evaluation, the hash code can be calculated efficiently as follows:

\[ \ldots (((s_0 \cdot b + s_1) b + s_2) b + \ldots + s_{n-2}) b + s_{n-1} \]

This expression is a polynomial for some positive \( b \), so this is called a polynomial hash code.
Hash Codes for Strings

- The hash computation can cause an overflow for long strings, but arithmetic overflow is ignored in Java.
- You should choose an appropriate value \( b \) to minimize collisions.
- Experiments show that good choices for \( b \) are 31, 33, 37, 39, and 41.
- In the String class, the `hashCode` is overridden using the polynomial hash code with \( b \) being 31.
Compressing Hash Codes

• The hash code for a key can be a large integer that is out of the range for the hash-table index
  • you need to scale it down to fit in the index’s range
• Assume the index for a hash table is between 0 and $N-1$
  -- the most common way to scale an integer is
  $$h(\text{hashCode}) = \text{hashCode} \mod N$$
• To ensure that the indices are spread evenly, choose $N$ to be a prime number greater than 2
  • However, it is time consuming to find a large prime number
Compressing Hash Codes

- In the Java API implementation for `java.util.HashMap`, `N` is set to a value of the power of 2 because then

  \[ h(\text{hashCode}) = \text{hashCode} \mod N \]

  is the same as

  \[ h(\text{hashCode}) = \text{hashCode} \& (N - 1) \]

  Bitwise conjunction

  \& can be performed much faster than the \mod operator

- The bitwise operations are much faster than the multiplication, division, and remainder operations -- you should replace these operations with the bitwise operations whenever possible

- For example, assume `N = 4` and `hashCode = 11`

  \[ h(\text{hashCode}) = \text{hashCode} \mod N \]

  \[ 11 \mod 4 = 3 \]

  \[ h(\text{hashCode}) = \text{hashCode} \& (N - 1) \]

  \[ (01011)_2 \& (00011)_2 = (11)_2 = 3 \]
Compressing Hash Codes

- To ensure that the hashing is evenly distributed, a supplemental hash function is also used along with the primary hash function in the implementation of `java.util.HashMap`

  ```java
  private static int supplementalHash(int h) {
    h ^= (h >>> 20) ^ (h >>> 12);
    return h ^ (h >>> 7) ^ (h >>> 4);
  }
  ```

- The complete hash function is defined as:

  \[
  h(\text{hashCode}) = \text{supplementalHash}(\text{hashCode}) \mod N
  \]

  which is the same as

  \[
  h(\text{hashCode}) = \text{supplementalHash}(\text{hashCode}) \& (N - 1)
  \]

  since \( N \) is a power of 2
A typical hash function first converts a search key to an integer value called a **hash code**, and then compresses the hash code into an index to the hash table:

\[
i = \text{hash(key)}
\]

**Hash function**

An entry
Handling Collisions

- A hashing collision occurs when two keys are mapped to the same index in a hash table.
- There are two ways for handling collisions: open addressing and separate chaining.
  - **Open addressing** is the process of finding an open location in the hash table in the event of a collision.
  - Open addressing has several variations: linear probing, quadratic probing and double hashing.
Linear Probing

- When a collision occurs during the **insertion** of an entry to a hash table, linear probing finds the next available location sequentially.
- If a collision occurs at $\text{hashTable}[k \ % \ N]$, check whether $\text{hashTable}[(k+1) \ % \ N]$ is available.
- If not, check $\text{hashTable}[(k+2) \ % \ N]$ and so on, until an available cell is found.

![Diagram showing linear probing](image)

For simplicity, only the keys are shown and the values are not shown. Here $N$ is 11 and index = key % N.
Linear Probing

- To **remove** an entry from the hash table, search the entry that matches the key
- If the entry is found, place a special marker to denote that the entry is available
- Each cell in the hash table has three possible states: *occupied*, *marked*, or *empty*
  - A marked cell is also available for insertion
- Linear probing tends to cause groups of consecutive cells in the hash table to be occupied -- each group is called a **cluster**
  - Each cluster is actually a probe sequence that you must search when retrieving, adding, or removing an entry
  - As clusters grow in size, they may merge into even larger clusters, further slowing down the search time
- This is a big disadvantage of linear probing
Quadratic Probing

- Quadratic probing looks at the cells at indices $(k+j^2) \mod N$, for $j \geq 0$, that is, $k \mod N$, $(k+1) \mod N$, $(k+4) \mod N$, $(k+9) \mod N$, and so on.

```
<table>
<thead>
<tr>
<th>Index</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>44</td>
</tr>
<tr>
<td>1</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>5</td>
<td>16</td>
</tr>
<tr>
<td>6</td>
<td>28</td>
</tr>
<tr>
<td>7</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>21</td>
</tr>
</tbody>
</table>
```

For simplicity, only the keys are shown and not the values. Here $N$ is 11 and index = key $\mod N$. New element with key 26 to be inserted. Quadratic probe 2 times before finding an empty cell.
Quadratic Probing

- Quadratic probing works in the same way as linear probing except for the change in the search sequence
- **Quadratic probing** can avoid the clustering problem in linear probing
  - It has its own clustering problem, called *secondary clustering*; that is, the entries that collide with an occupied entry use the same probe sequence
- Linear probing guarantees that an available cell can be found for insertion as long as the table is not full
  - there is no such guarantee for quadratic probing
Both linear probing and quadratic probing add an increment to the index $k$: 1 for linear probing and $j^2$ for quadratic probing

- These increments are independent of the keys
- **Double hashing** uses a secondary hash function $h'(key)$ on the keys to **determine the increments to avoid the clustering** problem
- Double hashing looks at the cells at indices ($k+j*h'(key)) \% N$, for $j>=0$, that is, $k \% N$, $(k+h'(key)) \% N$, $(k+2*h'(key)) \% N$, $(k+3*h'(key)) \% N$, and so on
Double Hashing

- For example, let the primary hash function $h$ and secondary hash function $h'$ on a hash table of size 11 be defined as follows:
  
  $h(key) = key \mod 11$;
  
  $h'(key) = 7 - key \mod 7$;

- For a search key of 12, we have
  
  $h(12) = 12 \mod 11 = 1$;
  
  $h'(12) = 7 - 12 \mod 7 = 2$;

The indices of the probe sequence are as follows: 1, 3, 5, 7, 9, 0, 2, 4, 6, 8, 10
The *separate chaining scheme* places all entries with the same hash index into the same location, rather than finding new locations.

- Each location in the separate chaining scheme is called a *bucket*.
- A *bucket* is a container that holds multiple entries:

![Diagram showing separate chaining with buckets](image-url)
Load Factor and Rehashing

- Load factor $\lambda$ (lambda) is the ratio of the number of elements to the size of the hash table

$$\lambda = \frac{n}{N}$$

where $n$ denotes the number of elements and $N$ the number of locations in the hash table

- For the open addressing scheme, $\lambda$ is between 0 and 1
  - If the hash table is empty, then $\lambda = 0$
  - If the hash table is full, then $\lambda = 1$

- For the separate chaining scheme, $\lambda$ can be any value
Load Factor and Rehashing

• As $\lambda$ increases, the probability of a collision increases
  • The load factor measures how full a hash table is
  • You should maintain the load factor under 0.5 for the open addressing scheme and under 0.9 for the separate chaining scheme
    • In the implementation of the `java.util.HashMap` class in the Java API, the threshold 0.75 is used
  • If the load factor is exceeded, increase the hash-table size and reload the entries into a new larger hash table - this is called rehashing
    • We need to change the hash functions, since the hash-table size has been changed
    • To reduce the likelihood of rehashing, since it is costly, you should at least double the hash-table size
MyHashMap<K, V>

+MyHashMap()
+MyHashMap(capacity: int)
+MyHashMap(capacity: int, loadFactorThreshold: float)

MyMap.Entry<K, V>

-key: K
-value: V

+Entry(key: K, value: V)
+getKey(): K
+getValue(): V

(c) Paul Fodor & Pearson Education
public interface MyMap<K, V> {
    /** Remove all of the entries from this map */
    public void clear();

    /** Return true if the specified key is in the map */
    public boolean containsKey(K key);

    /** Return true if this map contains the specified value */
    public boolean containsValue(V value);

    /** Return a set of entries in the map */
    public java.util.Set<Entry<K, V>> entrySet();

    /** Return the first value that matches the specified key */
    public V get(K key);

    /** Return true if this map contains no entries */
    public boolean isEmpty();

    /** Return a set consisting of the keys in this map */
    public java.util.Set<K> keySet();

    /** Add an entry (key, value) into the map */
    public V put(K key, V value);

    /** Remove the entries for the specified key */
    public void remove(K key);
/** Return the number of mappings in this map */
public int size();

/** Return a set consisting of the values in this map */
public java.util.Set<V> values();

/** Define inner class for Entry */
public static class Entry<K, V> {
    K key;
    V value;

    public Entry(K key, V value) {
        this.key = key;
        this.value = value;
    }

    public K getKey() {
        return key;
    }

    public V getValue() {
        return value;
    }

    @Override
    public String toString() {
        return "[" + key + ", " + value + "]";
    }
}
import java.util.LinkedList;

public class MyHashMap<K, V> implements MyMap<K, V> {
    // Define the default hash table size. Must be a power of 2
    private static int DEFAULT_INITIAL_CAPACITY = 4;

    // Define the maximum hash table size. 1 << 30 is same as 2^30
    private static int MAXIMUM_CAPACITY = 1 << 30;

    // Current hash table capacity. Capacity is a power of 2
    private int capacity;

    // Define default load factor
    private static float DEFAULT_MAX_LOAD_FACTOR = 0.75f;

    // Specify a load factor used in the hash table
    private float loadFactorThreshold;

    // The number of entries in the map
    private int size = 0;

    // Hash table is an array with each cell that is a linked list
    LinkedList<MyMap.Entry<K,V>>[] table;

    /** Construct a map with the default capacity and load factor */
    public MyHashMap() {
        this(DEFAULT_INITIAL_CAPACITY, DEFAULT_MAX_LOAD_FACTOR);
    }
}
/** Construct a map with the specified initial capacity and *
 * default load factor */
public MyHashMap(int initialCapacity) {
    this(initialCapacity, DEFAULT_MAX_LOAD_FACTOR);
}

/** Construct a map with the specified initial capacity *
 * and load factor */
public MyHashMap(int initialCapacity, float loadFactorThreshold) {
    if (initialCapacity > MAXIMUM_CAPACITY)
        this.capacity = MAXIMUM_CAPACITY;
    else
        this.capacity = trimToPowerOf2(initialCapacity);

    this.loadFactorThreshold = loadFactorThreshold;
    table = new LinkedList[capacity];
}

@Override /** Remove all of the entries from this map */
public void clear() {
    size = 0;
    removeEntries();
}

@Override /** Return true if the specified key is in the map */
public boolean containsKey(K key) {
    return get(key) != null;
}
@Override /** Return the value that matches the specified key */
public V get(K key) {
    int bucketIndex = hash(key.hashCode());
    if (table[bucketIndex] != null) {
        LinkedList<Entry<K, V>> bucket = table[bucketIndex];
        for (Entry<K, V> entry: bucket)
            if (entry.getKey().equals(key))
                return entry.getValue();
    }
    return null;
}

@Override /** Return true if this map contains no entries */
public boolean isEmpty() {
    return size == 0;
}

@Override /** Return a set consisting of the keys in this map */
public java.util.Set<K> keySet() {
    java.util.Set<K> set = new java.util.HashSet<K>();
    for (int i = 0; i < capacity; i++)
        if (table[i] != null) {
            LinkedList<Entry<K, V>> bucket = table[i];
            for (Entry<K, V> entry: bucket)
                set.add(entry.getKey());
        }
    return set;
}
@Override /** Return true if this map contains the value */
public boolean containsValue(V value) {
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            LinkedList<Entry<K, V>> bucket = table[i];
            for (Entry<K, V> entry: bucket)
                if (entry.getValue().equals(value))
                    return true;
        }
    }
    return false;
}

@Override /** Return a set of entries in the map */
public java.util.Set<MyMap.Entry<K,V>> entrySet() {
    java.util.Set<MyMap.Entry<K, V>> set =
        new java.util.HashSet<MyMap.Entry<K, V>>();
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            LinkedList<Entry<K, V>> bucket = table[i];
            for (Entry<K, V> entry: bucket)
                set.add(entry);
        }
    }
    return set;
}

@Override /** Return the number of entries in this map */
public int size() {
    return size;
}
@Override /** Add an entry (key, value) into the map */
public V put(K key, V value) {
    if (get(key) != null) { // The key is already in the map
        int bucketIndex = hash(key.hashCode());
        LinkedList<Entry<K, V>> bucket = table[bucketIndex];
        for (Entry<K, V> entry: bucket)
            if (entry.getKey().equals(key)) {
                V oldValue = entry.getValue();
                // Replace old value with new value
                entry.value = value;
                // Return the old value for the key
                return oldValue;
            }
    }
    // Check load factor
    if (size >= capacity * loadFactorThreshold) {
        if (capacity == MAXIMUM_CAPACITY)
            throw new RuntimeException("Exceeding maximum capacity");
        rehash();
    }
    int bucketIndex = hash(key.hashCode());
    // Create a linked list for the bucket if it is not created
    if (table[bucketIndex] == null) {
        table[bucketIndex] = new LinkedList<Entry<K, V>>();
    }
    // Add a new entry (key, value) to hashTable[index]
table[bucketIndex].add(new MyMap.Entry<K, V>(key, value));
size++; // Increase size
return value;
@Override /** Remove the entries for the specified key */
public void remove(K key) {
    int bucketIndex = hash(key.hashCode());
    // Remove the first entry that matches the key from a bucket
    if (table[bucketIndex] != null) {
        LinkedList<Entry<K, V>> bucket = table[bucketIndex];
        for (Entry<K, V> entry: bucket)
            if (entry.getKey().equals(key)) {
                bucket.remove(entry);
                size--; // Decrease size
                break; // Remove just one entry that matches the key
            }
    }
}

@Override /** Return a set consisting of the values in this map */
public java.util.Set<V> values() {
    java.util.Set<V> set = new java.util.HashSet<V>();
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            LinkedList<Entry<K, V>> bucket = table[i];
            for (Entry<K, V> entry: bucket)
                set.add(entry.getValue());
        }
    }
    return set;
}
/** Hash function */
private int hash(int hashCode) {
    return supplementalHash(hashCode) & (capacity - 1);
}

/** Ensure the hashing is evenly distributed */
private static int supplementalHash(int h) {
    h ^= (h >>> 20) ^ (h >>> 12);
    return h ^ (h >>> 7) ^ (h >>> 4);
}

/** Return a power of 2 for initialCapacity */
private int trimToPowerOf2(int initialCapacity) {
    int capacity = 1;
    while (capacity < initialCapacity) {
        capacity <<= 1;
    }
    return capacity;
}

/** Remove all entries from each bucket */
private void removeEntries() {
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            table[i].clear();
        }
    }
}
/** Rehash the map */
private void rehash() {
    java.util.Set<Entry<K, V>> set = entrySet(); // Get entries
    capacity <<= 1; // Double capacity
    table = new LinkedList[capacity]; // Create a new hash table
    size = 0; // Reset size to 0
    for (Entry<K, V> entry: set) {
        put(entry.getKey(), entry.getValue()); // Store to new table
    }
}

@Override
public String toString() {
    StringBuilder builder = new StringBuilder("[");

    for (int i = 0; i < capacity; i++) {
        if (table[i] != null && table[i].size() > 0)
            for (Entry<K, V> entry: table[i])
                builder.append(entry);
    }
    builder.append("]");
    return builder.toString();
}
public class TestMyHashMap {
    public static void main(String[] args) {
        // Create a map
        MyMap<String, Integer> map = new MyHashMap<String, Integer>();
        map.put("Smith", 30);
        map.put("Anderson", 31);
        map.put("Lewis", 29);
        map.put("Cook", 29);
        map.put("Smith", 65);
        System.out.println("Entries in map: " + map);
        System.out.println("The age for " + "Lewis is " +
            map.get("Lewis");
        System.out.println("Is Smith in the map? " +
            map.containsKey("Smith");
        System.out.println("Is age 33 in the map? " +
            map.containsValue(33));
        map.remove("Smith");
        System.out.println("Entries in map: " + map);
        map.clear();
        System.out.println("Entries in map: " + map);
    }
}

Output:
Entries in map: [[Anderson, 31][Smith, 65][Lewis, 29][Cook, 29]]
The age for Lewis is 29
Is Smith in the map? true
Is age 33 in the map? false
Entries in map: [[Anderson, 31][Lewis, 29][Cook, 29]]
Entries in map: []
### Implementing Set Using Hashing

#### Interface

```
interface MySet<E>
```

- `+iterator()`: java.util.Iterator<E>
- `+clear()`: void
- `+contains(e: E)`: boolean
- `+add(e: E)`: boolean
- `+remove(e: E)`: boolean
- `+isEmpty()`: boolean
- `+size()`: int

- MyHashSet<E>
  - `+MyHashSet()`
  - `+MyHashMap(capacity: int)`
  - `+MyHashMap(capacity: int, loadFactorThreshold: float)`

### Method Descriptions

- **clear()**: void
  - Removes all elements from this set.
  - Returns true if the element is in the set.
- **add(e: E)**: boolean
  - Adds the element to the set and returns true if the element is added successfully.
- **remove(e: E)**: boolean
  - Removes the element from the set and returns true if the set contained the element.
- **isEmpty()**: boolean
  - Returns true if this set does not contain any elements.
- **size()**: int
  - Returns the number of elements in this set.

- **MyHashSet<E>**
  - Creates an empty set with default capacity 4 and default load factor threshold 0.75f.
  - Creates a set with a specified capacity and default load factor threshold 0.75f.
  - Creates a set with a specified capacity and load factor threshold.
public interface MySet<E> extends java.lang.Iterable<E>{
    /** Remove all elements from this set */
    public void void clear();

    /** Return true if the element is in the set */
    public boolean contains(E e);

    /** Add an element to the set */
    public boolean add(E e);

    /** Remove the element from the set */
    public boolean remove(E e);

    /** Return true if the set contains no elements */
    public boolean isEmpty();

    /** Return the number of elements in the set */
    public int size();
}
import java.util.LinkedList;
public class MyHashSet<E> implements MySet<E> {
    // Define the default hash table size. Must be a power of 2
    private static int DEFAULT_INITIAL_CAPACITY = 4;

    // Define the maximum hash table size. 1 << 30 is same as 2^30
    private static int MAXIMUM_CAPACITY = 1 << 30;

    // Current hash table capacity. Capacity is a power of 2
    private int capacity;

    // Define default load factor
    private static float DEFAULT_MAX_LOAD_FACTOR = 0.75f;

    // Specify a load factor threshold used in the hash table
    private float loadFactorThreshold;

    // The number of elements in the set
    private int size = 0;

    // Hash table is an array with each cell that is a linked list
    private LinkedList<E>[] table;

    /** Construct a set with the default capacity and load factor */
    public MyHashSet() {
        this(DEFAULT_INITIAL_CAPACITY, DEFAULT_MAX_LOAD_FACTOR);
    }
}
/** Construct a set with the specified initial capacity and*
 * default load factor */
public MyHashSet(int initialCapacity) {
    this(initialCapacity, DEFAULT_MAX_LOAD_FACTOR);
}

/** Construct a set with the specified initial capacity
 * and load factor */
public MyHashSet(int initialCapacity, float loadFactorThreshold) {
    if (initialCapacity > MAXIMUM_CAPACITY)
        this.capacity = MAXIMUM_CAPACITY;
    else
        this.capacity = trimToPowerOf2(initialCapacity);

    this.loadFactorThreshold = loadFactorThreshold;
    table = new LinkedList[capacity];
}

@Override /** Remove all elements from this set */
public void clear() {
    size = 0;
    removeElements();
}
@Override /** Return true if the element is in the set */
public boolean contains(E e) {
    int bucketIndex = hash(e.hashCode());
    if (table[bucketIndex] != null) {
        LinkedList<E> bucket = table[bucketIndex];
        for (E element: bucket)
            if (element.equals(e))
                return true;
    }
    return false;
}

@Override /** Return true if the set contains no elements */
public boolean isEmpty() {
    return size == 0;
}

@Override /** Return the number of elements in the set */
public int size() {
    return size;
}

@Override /** Return an iterator for the elements in this set */
public java.util.Iterator<E> iterator() {
    return new MyHashSetIterator(this);
@Override /** Add an element to the set */
public boolean add(E e) {
    if (contains(e)) // Duplicate element not stored
        return false;
    if (size + 1 > capacity * loadFactorThreshold) {
        if (capacity == MAXIMUM_CAPACITY)
            throw new RuntimeException("Exceeding maximum capacity");
        rehash();
    }
    int bucketIndex = hash(e.hashCode());
    // Create a linked list for the bucket if it is not created
    if (table[bucketIndex] == null) {
        table[bucketIndex] = new LinkedList<E>();
    }
    // Add e to hashTable[index]
    table[bucketIndex].add(e);
    size++; // Increase size
    return true;
}
@Override /** Remove the element from the set */
public boolean remove(E e) {
    if (!contains(e))
        return false;
    int bucketIndex = hash(e.hashCode());
    // Create a linked list for the bucket if it is not created
    if (table[bucketIndex] != null) {
        LinkedList<E> bucket = table[bucketIndex];
        for (E element: bucket)
            if (e.equals(element)) {
                bucket.remove(element);
                break;
            }
    }
    size--; // Decrease size
    return true;
}
/** Inner class for iterator */
private class MyHashSetIterator implements java.util.Iterator<E> {
    // Store the elements in a list
    private java.util.ArrayList<E> list;
    private int current = 0; // Point to the current element in list
    private MyHashSet<E> set;

    /** Create a list from the set */
    public MyHashSetIterator(MyHashSet<E> set) {
        this.set = set;
        list = setToList();
    }

    @Override /** Next element for traversing? */
    public boolean hasNext() {
        if (current < list.size())
            return true;
        return false;
    }

    @Override /** Get current element and move cursor to the next */
    public E next() {
        return list.get(current++);
    }
}
@Override /** Remove the current element and refresh the list */
public void remove() {
    // Delete the current element from the hash set
    set.remove(list.get(current));
    list.remove(current); // Remove current element from the list
}

/** Hash function */
private int hash(int hashCode) {
    return supplementalHash(hashCode) & (capacity - 1);
}

/** Ensure the hashing is evenly distributed */
private static int supplementalHash(int h) {
    h ^= (h >>> 20) ^ (h >>> 12);
    return h ^ (h >>> 7) ^ (h >>> 4);
}

/** Return a power of 2 for initialCapacity */
private int trimToPowerOf2(int initialCapacity) {
    int capacity = 1;
    while (capacity < initialCapacity)
        capacity <<= 1;
    return capacity;
}
/** Remove all e from each bucket */
private void removeElements() {
    for (int i = 0; i < capacity; i++)
        if (table[i] != null)
            table[i].clear();
}

/** Rehash the set */
private void rehash() {
    java.util.ArrayList<E> list = setToList(); // Copy to a list
    capacity <<= 1; // Double capacity
    table = new LinkedList[capacity]; // Create a new hash table
    size = 0; // Reset size
    for (E element: list)
        add(element); // Add from the old table to the new table
}

/** Copy elements in the hash set to an array list */
private java.util.ArrayList<E> setToList() {
    java.util.ArrayList<E> list = new java.util.ArrayList<E>();
    for (int i = 0; i < capacity; i++)
        if (table[i] != null)
            for (E e: table[i])
                list.add(e);
    return list;
@Override
public String toString() {
    java.util.ArrayList<E> list = setToList();
    StringBuilder builder = new StringBuilder("[");
    // Add the elements except the last one to the string builder
    for (int i = 0; i < list.size() - 1; i++)
        builder.append(list.get(i) + ", ");
    // Add the last element in the list to the string builder
    if (list.size() == 0)
        builder.append("]");
    else
        builder.append(list.get(list.size() - 1) + "]");
    return builder.toString();
}
public class TestMyHashSet {
    public static void main(String[] args) {
        // Create a MyHashSet
        MySet<String> set = new MyHashSet<String>();
        set.add("Smith");
        set.add("Anderson");
        set.add("Lewis");
        set.add("Anderson");
        set.add("Cook");
        set.add("Smith");
        set.add("Cook");
        set.add("Smith");
        System.out.println("Elements in set: " + set);
        System.out.println("Number of elements in set: " + set.size());
        System.out.println("Is Smith in set? " + set.contains("Smith"));

        set.remove("Smith");
        System.out.print("Names in set in uppercase are ");
        for (String s: set)
            System.out.print(s.toUpperCase() + " ");

        set.clear();
        System.out.println("\nElements in set: " + set);
    }
}

Output:
Elements in set: [Anderson, Smith, Lewis, Cook]
Number of elements in set: 4
Is Smith in set? true
Names in set in uppercase are ANDERSON LEWIS COOK
Elements in set: []