Sets and Maps

CSE260, Computer Science B: Honors
Stony Brook University

http://www.cs.stonybrook.edu/~cse260
Objectives

• To store unordered, nonduplicate elements using a set
• To explore how and when to use `HashSet`, `LinkedHashSet` or `TreeSet` to store elements
• To compare performance of sets and lists
• To use sets to develop a program that counts the keywords in a Java source file
• To tell the differences between `Collection` and `Map` and describe when and how to use `HashMap`, `LinkedHashMap`, and `TreeMap` to store values associated with keys
• To use maps to develop a program that counts the occurrence of the words in a text
• To obtain singleton sets, lists, and maps, and unmodifiable sets, lists, and maps, using the static methods in the `Collections` class
Motivation Problem

• Suppose we need to write a program that checks whether a student is in a class
  • You can use a list to store the names of the students and search for the student with linear search
  • However, a more efficient data structure for this application is a set with efficient methods to search for elements

• Suppose your program also needs to store detailed information about the students in the class (e.g., grades for labs, homework submissions, submission times, GPA) and all can be retrieved using the name of the student as the key
  • A map is an efficient data structure for such a task
Review of Java Collection Framework hierarchy

- **Set** is a sub-interface of **Collection**
- You can create a set using one of its three concrete classes: **HashSet**, **LinkedHashSet**, or **TreeSet**
The Collection interface is the root interface for manipulating a collection of objects.

Reminder:

- Returns an iterator for the elements in this collection.

- Adds a new element o to this collection.
- Adds all the elements in the collection c to this collection.
- Removes all the elements from this collection.
- Returns true if this collection contains the element o.
- Returns true if this collection contains all the elements in c.
- Returns true if this collection is equal to another collection o.
- Returns the hash code for this collection.
- Returns true if this collection contains no elements.
- Removes the element o from this collection.
- Removes all the elements in c from this collection.
- Retains the elements that are both in c and in this collection.
- Returns the number of elements in this collection.
- Returns an array of Object for the elements in this collection.

Returns true if this iterator has more elements to traverse.
Returns the next element from this iterator.
Removes the last element obtained using the next method.
The **Set** Interface

- The **Set** interface extends the **Collection** interface, but it does not introduce new methods or constants, but it **stipulates** that an instance of **Set** contains no duplicate elements
  - That is, **no two elements** \( e_1 \) and \( e_2 \) can be in the set such that \( e_1.equals(e_2) \) is true
  - The **concrete classes** that implement **Set** must ensure that **no duplicate elements can be added** to the set
AbstractSet

- The **AbstractSet** class extends **AbstractCollection** and partially implements **Set**
AbstractSet

• The AbstractSet class provides concrete implementations for the equals method and the hashCode method
• The hash code of a set is the sum of the hash codes of all the elements in the set
• Since the size method and iterator method are not implemented in the AbstractSet class, AbstractSet is an abstract class
The Set Interface Hierarchy
The HashSet Class

• The **HashSet** class is a concrete class that implements **Set**
  • It can be used to store duplicate-free elements
  • You can create an empty hash set using its no-arg constructor or create a hash set from an existing collection
The HashSet Class

- By default, the initial capacity is 16 and the load factor is 0.75
- The load factor is a value between 0.0 and 1.0.
- The load factor measures how full the set is allowed to be before its capacity is increased.
  - When the number of elements exceeds the product of the capacity and load factor, the capacity is automatically doubled.
  - For example, if the capacity is 16 and load factor is 0.75, the capacity will be doubled to 32 when the size reaches 12 \((16 \times 0.75 = 12)\).
- A higher load factor decreases the space costs but increases the search time.
- The default load factor 0.75 is a good tradeoff between time and space costs.
The HashSet Class

- Hash codes:
  - `hashCode` method is defined in the `Object` class
  - The hash codes of two objects must be the same if the two objects are equal
  - Two unequal objects may have the same hash code, but you should implement the `hashCode` method to avoid too many such cases
  - API Java hashcodes:
    - `hashCode` in the `Integer` class returns its `int` value
    - `hashCode` in the `Character` class returns the Unicode of the character
    - `hashCode` in the `String` class returns
      \[s_0 \times 31^{(n-1)} + s_1 \times 31^{(n-2)} + \ldots + s_{n-1}\]
      where \(s_i\) is `s.charAt(i)`.
  - 31 is an odd prime with a nice property that the multiplication can be replaced by a shift and a subtraction for better performance: \(31 \times i == (i<<5) - i\). Modern VMs do this sort of optimization automatically.
Example: Using HashSet and Iterator

- This example creates a hash set filled with strings, and uses an iterator to traverse the elements in the list.

```java
import java.util.*;
public class TestHashSet {
    public static void main(String[] args) {
        // Create a hash set
        Set<String> set = new HashSet<>();
        // Add strings to the set
        set.add("London");
        set.add("Paris");
        set.add("New York");
        set.add("San Francisco");
        set.add("Beijing");
        set.add("New York");
        System.out.println(set);
        // Display the elements in the hash set
        for (String s: set) {
            System.out.print(s.toUpperCase() + " ");
        }
        System.out.println();
        // Process the elements using the forEach method
        set.forEach(e -> System.out.print(e.toLowerCase() + " "));
    }
}
```
The **HashSet** Class

- The strings are not stored in the order in which they are inserted into the set
  - There is no particular order for the elements in a hash set
- To impose an order on them, you need to use the **LinkedHashSet** class
- **Collection** interface extends the **Iterable** interface, so the elements in a set are iterable
- Also, since a set is an instance of **Collection**, all methods defined in **Collection** can be used for sets
  - Including **for**-each loops can be used to traverse all the elements in the set
public class TestMethodsInCollection {
    public static void main(String[] args) {
        // Create set1
        java.util.Set<String> set1 = new java.util.HashSet<>();

        // Add strings to set1
        set1.add("London");
        set1.add("Paris");
        set1.add("New York");
        set1.add("San Francisco");
        set1.add("Beijing");

        System.out.println("set1 is " + set1);
        System.out.println(set1.size() + " elements in set1");

        // Delete a string from set1
        set1.remove("London");
        System.out.println("\nset1 is " + set1);
        System.out.println(set1.size() + " elements in set1");

        // Create set2
        java.util.Set<String> set2 = new java.util.HashSet<>();
    }
}
Output:

set1 is [San Francisco, New York, Paris, Beijing, London]
5 elements in set1

set1 is [San Francisco, New York, Paris, Beijing]
4 elements in set1
// Add strings to set2
set2.add("London");
set2.add("Shanghai");
set2.add("Paris");
System.out.println("set2 is " + set2);
System.out.println(set2.size() + " elements in set2");

System.out.println("Is Taipei in set2? "
    + set2.contains("Taipei")));

set1.addAll(set2);
System.out.println("After adding set2 to set1, set1 is "
    + set1);

set1.removeAll(set2);
System.out.println("After removing set2 from set1, set1 is "
    + set1);

set1.retainAll(set2);
System.out.println("After removing common elements in set2 "
    + "from set1, set1 is " + set1);
}
Output (cont.):

set2 is [Shanghai, Paris, London]
3 elements in set2

Is Taipei in set2? false

After adding set2 to set1, set1 is
[San Francisco, New York, Shanghai, Paris, Beijing, London]

After removing set2 from set1, set1 is
[San Francisco, New York, Beijing]

After removing common elements in set2 from set1, set1 is []
The LinkedHashSet Class

• **LinkedHashSet** extends **HashSet** with a linked-list implementation that supports an ordering of the elements in the set.

• The elements in a **HashSet** are not ordered, but the elements in a **LinkedHashSet** can be retrieved in the order in which they were inserted into the set.

• To impose a different order (e.g., increasing or decreasing order), you can use the **TreeSet** class.
Example: Using `LinkedHashSet`

- This example creates a hash set filled with strings, and uses an iterator to traverse the elements in the list.

```java
import java.util.*;
public class TestLinkedHashSet {
    public static void main(String[] args) {
        // Create a hash set
        Set<String> set = new LinkedHashSet<>();

        // Add strings to the set
        set.add("London");
        set.add("Paris");
        set.add("New York");
        set.add("San Francisco");
        set.add("Beijing");
        set.add("New York");

        System.out.println(set);

        // Display the elements in the hash set
        for (String element : set) 
            System.out.print(element.toLowerCase() + " ");
    }
}
```
The `SortedSet` Interface and the `TreeSet` Class
The `SortedSet` Interface and the `TreeSet` Class

- **SortedSet** is a sub-interface of **Set**, which guarantees that the elements in the set are sorted.
- **TreeSet** is a concrete class that implements the **SortedSet** interface:
  - It provides the methods `first()` and `last()` for returning the first and last elements in the set.
  - You can add objects into a tree set as long as they can be compared with each other.
The SortedSet Interface and the TreeSet Class

- NavigableSet extends SortedSet to provide navigation methods lower(e), floor(e), ceiling(e), and higher(e) that return elements respectively less than, less than or equal, greater than or equal, and greater than a given element and return null if there is no such element.
- The pollFirst() and pollLast() methods remove and return the first and last element in the tree set, respectively.
- headSet(toElement) and tailSet(fromElement) return a portion of the set whose elements are less than toElement and greater than or equal to fromElement, respectively.
The SortedSet Interface and the TreeSet Class

- You can use an iterator to traverse the elements in the sorted order
- The elements can be sorted in two ways
  - One way is to use the Comparable interface
  - The other way (order by comparator) is to specify a comparator for the elements in the set if the class for the elements does not implement the Comparable interface, or you don’t want to use the compareTo method in the class that implements the Comparable interface
Example: Using TreeSet to Sort Elements in a Set

- This example creates a hash set filled with strings, and then creates a tree set for the same strings
- The strings are sorted in the tree set using the compareTo method in the Comparable interface
import java.util.*;

public class TestTreeSet {
    public static void main(String[] args) {
        // Create a hash set
        Set<String> set = new HashSet<>();

        // Add strings to the set
        set.add("London");
        set.add("Paris");
        set.add("New York");
        set.add("San Francisco");
        set.add("Beijing");
        set.add("New York");

        TreeSet<String> treeSet = new TreeSet<>(set);
        System.out.println("Sorted tree set: " + treeSet);

        // Use the methods in SortedSet interface
        System.out.println("first(): " + treeSet.first());
        System.out.println("last(): " + treeSet.last());
        System.out.println("headSet("New York"): " +
                           treeSet.headSet("New York");
        System.out.println("tailSet("New York"): " +
                           treeSet.tailSet("New York");
    }
}
Output:


first(): Beijing

last(): San Francisco

headSet("New York"): [Beijing, London]

// Use the methods in NavigableSet interface
System.out.println("lower(""P")": " + treeSet.lower("P");
System.out.println("higher(""P")": " + treeSet.higher("P");
System.out.println("floor(""P")": " + treeSet.floor("P");
System.out.println("ceiling(""P")": " + treeSet.ceiling("P");
System.out.println("pollFirst(): " + treeSet.pollFirst();
System.out.println("pollLast(): " + treeSet.pollLast();
System.out.println("New tree set: " + treeSet);
}
[


This outputs:
lower("P"): New York
higher("P"): Paris
floor("P"): New York
ceiling("P"): Paris

pollFirst(): Beijing
pollLast(): San Francisco
New tree set: [London, New York, Paris]
Example: Using Comparator to Sort Elements in a Set

- The example creates a tree set of geometric objects
- The geometric objects are sorted using the \texttt{compare} method in the \texttt{Comparator} interface
import java.util.*;

public class TestTreeSetWithComparator {
    public static void main(String[] args) {
        // Create a tree set for geometric objects using a comparator
        Set<GeometricObject> set =
            new TreeSet<>(new GeometricObjectComparator());
        set.add(new Rectangle(4, 5));
        set.add(new Circle(40));
        set.add(new Circle(40));
        set.add(new Rectangle(4, 1));

        // Display geometric objects in the tree set
        System.out.println("A sorted set of geometric objects");

        for (GeometricObject element: set)
            System.out.println("area = " + element.getArea());
    }
}

A sorted set of geometric objects
area = 4.0
area = 20.0
area = 5021.548245743669
area = 5021.548245743669
Performance of Sets and Lists

- **Sets are more efficient than lists for storing nonduplicate elements**
- **Lists are useful for accessing elements through the index**
- **Sets do not support indexing** because the elements in a set are unordered
  - To traverse all elements in a set, use a for-each loop or iterator
import java.util.*;

public class SetListPerformanceTest {
    static final int N = 50000;

    public static void main(String[] args) {
        // Add numbers 0, 1, 2, ..., N - 1 to the array list
        List<Integer> list = new ArrayList<>();
        for (int i = 0; i < N; i++)
            list.add(i);
        Collections.shuffle(list); // Shuffle the array list

        // Create a hash set, and test its performance
        Collection<Integer> set1 = new HashSet<>(list);
        System.out.println("Member test time for hash set is " +
                           getTestTime(set1) + " milliseconds");
        System.out.println("Remove element time for hash set is " +
                           getRemoveTime(set1) + " milliseconds");

        // Create a linked hash set, and test its performance
        Collection<Integer> set2 = new LinkedHashSet<>(list);
        System.out.println("Member test time for linked hash set is " +
                           getTestTime(set2) + " milliseconds");
        System.out.println("Remove element time for linked hash set is " +
                           getRemoveTime(set2) + " milliseconds");
    }
}

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Member test time for hash set is 20 milliseconds
Remove element time for hash set is 27 milliseconds

Member test time for linked hash set is 27 milliseconds
Remove element time for linked hash set is 26 milliseconds
/ Create a tree set, and test its performance
Collection<Integer> set3 = new TreeSet<>((list);
System.out.println("Member test time for tree set is " +
    getTestTime(set3) + " milliseconds");
System.out.println("Remove element time for tree set is " +
    getRemoveTime(set3) + " milliseconds");

// Create an array list, and test its performance
Collection<Integer> list1 = new ArrayList<>((list);
System.out.println("Member test time for array list is " +
    getTestTime(list1) + " milliseconds");
System.out.println("Remove element time for array list is " +
    getRemoveTime(list1) + " milliseconds");

// Create a linked list, and test its performance
Collection<Integer> list2 = new LinkedList<>((list);
System.out.println("Member test time for linked list is " +
    getTestTime(list2) + " milliseconds");
System.out.println("Remove element time for linked list is " +
    getRemoveTime(list2) + " milliseconds");
}
public static long getTestTime(Collection<Integer> c) {
    long startTime = System.currentTimeMillis();

    // Test if a number is in the collection
    for (int i = 0; i < N; i++)
        c.contains((int)(Math.random() * 2 * N));

    return System.currentTimeMillis() - startTime;
}

public static long getRemoveTime(Collection<Integer> c) {
    long startTime = System.currentTimeMillis();

    for (int i = 0; i < N; i++)
        c.remove(i);

    return System.currentTimeMillis() - startTime;
}
Member test time for hash set is 20 milliseconds
Remove element time for hash set is 27 milliseconds

Member test time for linked hash set is 27 milliseconds
Remove element time for linked hash set is 26 milliseconds

Member test time for tree set is 47 milliseconds
Remove element time for tree set is 34 milliseconds

Member test time for array list is 39802 milliseconds
Remove element time for array list is 16196 milliseconds

Member test time for linked list is 52197 milliseconds
Remove element time for linked list is 14870 milliseconds
Case Study: Counting Keywords

- An application that counts the number of the keywords in a Java source file
- For each word in a Java source file, we need to determine whether the word is a keyword
- To handle this efficiently, store all the keywords in a `HashSet` and use the `contains` method to test if a word is in the keyword set
import java.util.*;
import java.io.*;

public class CountKeywords {
    public static void main(String[] args) throws Exception {
        Scanner input = new Scanner(System.in);
        System.out.print("Enter a Java source file: ");
        String filename = input.nextLine();

        File file = new File(filename);
        if (file.exists()) {
            System.out.println("The number of keywords in " + filename + " is " + countKeywords(file));
        }
        else {
            System.out.println("File " + filename + " does not exist");
        }
    }

    public static int countKeywords(File file) throws Exception {
        // Array of all Java keywords + true, false and null
        int count = 0;
        try (BufferedReader br = new BufferedReader(new FileReader(file))) {
            String line;
            while ((line = br.readLine()) != null) {
                String[] words = line.split(" ");
                for (String word : words) {
                    if (Arrays.asList(keywordString).contains(word.toLowerCase())) {
                        count++;
                    }
                }
            }
        }
        return count;
    }
}
Set<String> keywordSet =
    new HashSet<>(Arrays.asList(keywordString));
int count = 0;

Scanner input = new Scanner(file);

while (input.hasNext()) {
    // read the file word by word
    String word = input.next();
    String[] a = word.split("\\W");
    for(String s:a) // to handle cases like "while(..."
        if (keywordSet.contains(s))
            count++;
}

return count;
}
The **Map** Interface

- The **Map** interface maps keys to the elements
  - The keys are like indexes
- In **List**, the indexes are integer
- In **Map**, the keys can be any objects
There are three types of maps: **HashMap**, **LinkedHashMap**, and **TreeMap**.

The common features of these maps are defined in the **Map** interface.
The **Map** interface provides the methods for querying, updating, and obtaining a collection of values and a set of keys.

```java
public interface Map<K, V> {
    void clear();
    boolean containsKey(Object key);
    boolean containsValue(Object value);
    Set<Map.Entry<K, V>> entrySet();
    V get(Object key);
    boolean isEmpty();
    Set<K> keySet();
    V put(K key, V value);
    V putAll(Map<? extends K, ? extends V> m);
    V remove(Object key);
    int size();
    Collection<V> values();
}
```

- `clear()`: Removes all entries from this map.
- `containsKey(key)`: Returns true if this map contains an entry for the specified key.
- `containsValue(value)`: Returns true if this map maps one or more keys to the specified value.
- `entrySet()`: Returns a set consisting of the entries in this map.
- `get(key)`: Returns the value for the specified key in this map.
- `isEmpty()`: Returns true if this map contains no entries.
- `keySet()`: Returns a set consisting of the keys in this map.
- `put(key, value)`: Puts an entry into this map.
- `remove(key)`: Adds all the entries from `m` to this map.
- `size()`: Removes the entries for the specified key.
- `values()`: Returns the number of entries in this map.
- `Collection(values)`: Returns a collection consisting of the values in this map.
Concrete **Map** Classes

- **java.util.Map<K, V>**
  - **java.util.AbstractMap<K, V>**
    - **java.util.HashMap<K, V>**
      - `HashMap()`
      - `HashMap(initialCapacity: int, loadFactor: float)`
      - `HashMap(m: Map<? extends K, ? extends V>)`
    - **java.util.LinkedHashMap<K, V>**
      - `LinkedHashMap()`
      - `LinkedHashMap(m: Map<? extends K, ? extends V>)`
      - `LinkedHashMap(initialCapacity: int, loadFactor: float, accessOrder: boolean)`
  - **java.util.SortedMap<K, V>**
    - **java.util.NavigableMap<K, V>**
      - `floorKey(key: K): K`
      - `ceilingKey(key: K): K`
      - `lowerKey(key: K): K`
      - `higherKey(key: K): K`
      - `pollFirstEntry(): Map.EntrySet<K, V>`
      - `pollLastEntry(): Map.EntrySet<K, V>`
    - **java.util.TreeMap<K, V>**
      - `TreeMap()`
      - `TreeMap(m: Map<? extends K, ? extends V>)`
      - `TreeMap(c: Comparator<? super K>)`
The **Map** Interface UML Diagram

- You can obtain a set of the keys in the map using the `keySet()` method.
- The `entrySet()` method returns a set of entries.
- The entries are instances of the `Map.Entry` interface, where `Entry` is an inner interface for the `Map` interface.

```
interface java.util.Map.Entry<K, V>

+getKey(): K
+getValue(): V
+setValue(value: V): void
```

- Returns the key from this entry.
- Returns the value from this entry.
- Replaces the value in this entry with a new value.
HashMap and TreeMap

- The **HashMap**, **LinkedHashMap** and **TreeMap** classes are two concrete implementations of the **Map** interface.
- The **HashMap** class is efficient for locating a value, inserting a mapping, and deleting a mapping.
- **LinkedHashMap** extends **HashMap** with a linked-list implementation that supports an ordering of the entries in the map.
  - the entries in a **LinkedHashMap** can be retrieved either in the order in which they were inserted into the map (known as the insertion order) or in the order in which they were last accessed, from least recently to most recently accessed (access order).
- The **TreeMap** class, implementing **SortedMap**, is efficient for traversing the keys in a sorted order using the **Comparable** interface or the **Comparator** interface.
Example: Using **HashMap** and **TreeMap**

- A hash map with the student’s name as its key and the grade as its value
- The program then creates a tree map from the hash map and displays the entries in ascending order of the keys
- Finally, the program creates a linked hash map with access order, adds the same entries to the map, and displays the entries
  - The entry with the key Lewis is last accessed, so it is displayed last
import java.util.*;

class TestMap {
    public static void main(String[] args) {
        // Create a HashMap
        Map<String, Integer> hashMap = new HashMap<>();
        hashMap.put("Smith", 100);
        hashMap.put("Anderson", 91);
        hashMap.put("Lewis", 99);
        hashMap.put("Cook", 89);

        System.out.println("Display entries in HashMap");
        System.out.println(hashMap + 
        "\n");

        // Create a TreeMap from the preceding HashMap
        Map<String, Integer> treeMap = new TreeMap<>(hashMap);
        System.out.println("Display entries in ascending order of key");
        System.out.println(treeMap);

        // Create a LinkedHashMap
        Map<String, Integer> linkedHashMap =
                new LinkedHashMap<>((16, 0.75f, true);
        linkedHashMap.put("Smith", 100);
        linkedHashMap.put("Anderson", 91);
        linkedHashMap.put("Lewis", 99);
        linkedHashMap.put("Cook", 89);
    }
}
// Display the grade for Lewis
System.out.println("The grade for " + "Lewis is " +
    linkedHashMap.get("Lewis");

System.out.println("Display entries in LinkedHashMap");
System.out.println(linkedHashMap);

// Display each entry with name and grade
System.out.print("Names and grades are ");
treeMap.forEach(
    (name, grade) -> System.out.print(name + ": "+ grade + " "));
}

Output:
Display entries in HashMap
{Cook=89, Smith=100, Lewis=99, Anderson=91}

Display entries in ascending order of key
{Anderson=91, Cook=89, Lewis=99, Smith=100}

The grade for Lewis is 99

Display entries in LinkedHashMap
{Smith=100, Anderson=91, Cook=89, Lewis=99}
Case Study: Counting the Occurrences of Words in a Text

- This program counts the occurrences of words in a text and displays the words and their occurrences in ascending order of the words.
- The program uses a hash map to store a pair consisting of a word and its count.
- For each word, check whether it is already a key in the map.
  - If not, add the key and value 1 to the map.
  - Otherwise, increase the value for the word (key) by 1 in the map.
- To sort the map, we use a tree map.
import java.util.*;

public class CountOccurrenceOfWords {
    public static void main(String[] args) {
        // Set text in a string
        String text = "Good morning. Have a good class. " +
                        "Have a good visit. Have fun!";

        // Create a TreeMap to hold words as key and count as value
        Map<String, Integer> map = new TreeMap<>();

        String[] words = text.split("[\s\p+]");
        for (int i = 0; i < words.length; i++) {
            String key = words[i].toLowerCase();
            if (key.length() > 0) {
                if (!map.containsKey(key)) {
                    map.put(key, 1);
                } else {
                    int value = map.get(key);
                    value++;
                    map.put(key, value);
                }
            }
        }
    }
}
// Display key and value for each entry
map.forEach((k, v) -> System.out.println(k + "\t" + v));
The Singleton and Unmodifiable Collections

- You can create singleton sets, lists, and maps and unmodifiable sets, lists, and maps using the static methods in the `Collections` class.

<table>
<thead>
<tr>
<th>java.util.Collections</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>+singleton(o: Object): Set</code></td>
</tr>
<tr>
<td><code>+singletonList(o: Object): List</code></td>
</tr>
<tr>
<td><code>+singletonMap(key: Object, value: Object): Map</code></td>
</tr>
<tr>
<td><code>+unmodifiableCollection(c: Collection): Collection</code></td>
</tr>
<tr>
<td><code>+unmodifiableList(list: List): List</code></td>
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<td><code>+unmodifiableMap(m: Map): Map</code></td>
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<tr>
<td><code>+unmodifiableSet(s: Set): Set</code></td>
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<tr>
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<td><code>+unmodifiableSortedSet(s: SortedSet): SortedSet</code></td>
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</tbody>
</table>

- The `Collections` class defines three constants—`EMPTY_SET`, `EMPTY_LIST`, and `EMPTY_MAP`—for an empty set, an empty list, and an empty map (these are returned by singleton…).