Reasoning about the Behavior of Semantic Web Services with Concurrent Transaction Logic

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ABSTRACT
The recent upsurge in the interest in Semantic Web services and the efforts such as the WSMO, OWL-S, and SWSL projects have drawn attention to the importance of logic-based modeling of the behavior of Web services. In the context of Semantic Web services, the logic-based approach has many applications, including service discovery, service choreography and enactment, and contracting for services. In this paper, we extend our earlier work on workflow modeling towards reasoning about service behavior, including the aforementioned choreography, contracting, and enactment. The formalism underlying our framework is Concurrent Transaction Logic—a logic for declarative specification, analysis, and execution of database transactions. The new results include reasoning about service behavior under more general sets of constraints and extension of the framework towards data flow—a crucial aspect that was completely missing from previous logical formalizations.

1. INTRODUCTION
The idea and the promise of combining the Semantic Web with Web services has attracted intense interest in the research community and industry. The early projects like OWL-S1 and SWSL2 were followed by bigger and more sustained efforts like WSMO,3 which is at the center of a series of large European integrated projects, such as DIP4 and SUPER5 The research problems in this area are many and varied in nature: ontology specification languages that must go well beyond OWL, service discovery, service choreography (i.e., specification of how autonomous client agents interact with services), automated contracting for services, service enactment, and execution monitoring, and others. In this paper, we address some of the aforesaid problems: modeling, contracting, and enactment.

The techniques we are using here are based on Concurrent Transaction Logic (CTR) [6] and continue our earlier line of research [7, 16, 8]. The use of CTR for process modeling in workflows was first advocated in [7], where a scheduling algorithm for executing workflows under temporal and causality constraints was introduced. The present work extends those results fourfold. First, we allow a significantly more complex set of constraints, which encompasses all the constraints available in the recently proposed language DecSerFlow [19]. Second, data flow, without which any description of a service of workflow is unrealistic, is now part of the framework. Third, the algorithms are greatly improved by expanding the proof theory of CTR, which allowed us to replace various ad hoc parts of the earlier approaches (such as so-called knot elimination in [7, 8]). Finally, we show how our framework applies to the areas of service choreography and contracting—areas whose logical foundations have not seen much research. In [8] we extended CTR to a logic, called CTR-S, which was designed for modeling service choreography and contracting. However, CTR-S turned out to be a very complex formalism and the results were limited to rather simple forms of contracting. The present paper uses a much simpler logic, CTR, but complex patterns of choreography and contracting can be modelled nonetheless.

Our new techniques significantly extend the kinds of service contracts that can be handled, but it is not known whether and how much is given up in terms of choreography. Finally, [16] introduced techniques from constraint logic programming to the problem of service enactment under aggregate constraints (such as aggregate cost of service execution). We incorporate some of those techniques to model the data flow that arises in service choreography and contracting. Discussion of additional related work appears in Section 6.

The remainder of this paper is organized as follows. Section 2 describes the basic techniques from process modeling, which includes control flow graphs and constraints. It then outlines our framework in which service choreography and the process of contracting for services can be handled using these techniques.

To make the paper self-contained, Section 3 gives a short introduction to CTR. Section 4 shows how the framework outlined in Section 2 is formalized in CTR. Section 5 describes the verification procedure, which is the key component of service contracting in our framework. Section 6 presents related work, and Section 7 concludes this paper.

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1 http://www.daml.org/services/owl-s/
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5 http://ip-super.org/
2. SERVICE BEHAVIOR: MODELING, REASONING, AND ENACTMENT

Figure 1 depicts the main aspects of service behavior addressed in our work. The behavior of the service is described through its choreography—a specification of how to invoke and interact with the service in order to get results. This is known as the WSMO model of choreography. The W3 Choreography group’s model includes both the service interactions and the client interactions. This model is symmetric and can be represented in our framework by including the choreography, policy, and contract components on both the client and the service side in the figure. This can be further extended to multiagent interactions. However, these issues are beyond the scope of this paper and they are orthogonal to the reasoning problems, which we consider here. One way to describe the choreography interface of the service is through the control and data flow graphs.

![Figure 1: Elements of the reasoning architecture for semantic Web services.](image)

The service policy component shown in Figure 1 is typically a set of additional constraints imposed on the choreography and on the input. The contract requirements, included on the client side of the figure, represent the contractual requirements of the user, which go beyond the basic functions (such as selling books or helping with travel arrangements) of the service. Thus, in our framework, the choreography, policy, and contract components on both the client and the service side in the figure. This can be further extended to multiagent interactions. However, these issues are beyond the scope of this paper and they are orthogonal to the reasoning problems, which we consider here. One way to describe the choreography interface of the service is through the control and data flow graphs.

![Figure 2: A control-flow graph.](image)

A control flow graph is typically used to specify local execution dependencies among the interactions with the service; it is a good way to visualize the overall flow of control. Such a graph has an initial and the final interaction in the process, the successor-interaction for each interaction in the graph, and whether these successors must all be executed concurrently or in some unspecified order (represented using AND-nodes), or whether only one of the alternative branches needs to be executed non-deterministically (represented using OR-nodes). In Figure 2, all successors of the initial interaction place_order must be executed, but all these successors are OR-nodes. For example, the lowermost successor node of place_order is an OR-node and only one of its successors, pay_by_cheque or pay_by_CC, is supposed to be executed. The node accept_delivery is also an OR-node, but with a twist. The upper branch going out of this node represent a situation where a customer returns the purchased item. The lower branch, however, has no interactions, and it meets the upper branch. This means that the upper branch is optional: the customer may or may not return the item. Similarly, the rightmost segment of the graph indicates that rebate is an optional interaction.

Two more things about the control flow graph in Figure 2 are worth noting: the shaded boxes labeled with give_security and pay are, and the condition credit_limit > price attached to the arc leaving the node give_CC. The shaded boxes delineate control flow subgraphs corresponding to complex interactions that are composed of several sub-interactions. If a control graph represents a workflow then these complex interactions would be would called complex tasks and would correspond subworkflows. The condition credit_limit > price attached to the aforesaid arc is called a transition condition. It says that in order for the next interaction with the service to take place the condition must be satisfied. The parameters credit_limit and price may be obtained by querying the current state of the service or they may be passed as parameters from one interaction to another—the actual method depends on a concrete representation. In general, transition conditions are Boolean expressions attached to the arcs in control flow graphs. Only the arcs whose conditions evaluate to true can be followed at run time.

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6http://www.wsmo.org/TR/d14/
7http://www.w3.org/TR/2006/WD-ws-cdl-10-primer-20060619/
**Constraints.** In more complex cases, a control flow graph may contain additional elements, such as loops. However, such graphs are typically used to represent local dependencies among interactions in a choreography interface. Global dependencies often arise as part of specification of policies; they take the form of global temporal and causality constraints. Yet another situation when global constraints arise is when a client has specific requirements to interact with the service. These requirements have little to do with what the functionality of the service (e.g., selling books), but rather with the particular guarantees that the client wants to have in order to enter into a contract with the service and strike a deal. We call such sets of client-side constrains client contract requirements. Figure 3 gives an example of global constraints that represent service policy and client contract requirements for our running example.

**Service policy**

1. If pay\_by\_CC takes place after accept\_delivery then give\_security must precede accept\_delivery
2. If pay\_by\_cheque takes place after accept\_delivery then pay\_by\_cheque immediately follows accept\_delivery
3. If rebate is given then pay must precede accept\_delivery

**Client contract requirements**

4. The interaction accept\_delivery must precede pay\_by\_check

Figure 3: Global behavioral constraints.

**Data flow graphs.** Any series of interactions with a service typically involves passing data, and the flow of data among these interactions are normally modeled using graphs. A data flow graph is like a control flow graph except that the arcs represent the routes along which data is passed from one interaction to the other. These arcs are labeled with data items that are being passed around. Since, in many cases, control flow is accompanied by passing data, a data flow graph often has many of the arcs present in the control flow graph. A data flow graph corresponding to our running example is depicted in Figure 4.

The parts “inherited” from the control flow graph are shaded to help focus attention on the new elements. The data flow graph has two new arcs, which represent non-local passing of the credit card information. Also, the arcs going out of the initial interaction place\_order are labeled with the Order\# item to indicate that this item is being passed along those arcs. In fact, this item (and some others) are passed along almost all arcs in the graph and to avoid cluttering the picture we did not include them.

One important observation is that the interactions at the ends of an arc in the data flow graph must be ordered in time, since generally the interaction that receives an item must wait for the interaction that produces the item. However, this interaction is not only temporal but also conditional. For instance, the interaction partial\_refund receives the credit card number from pay\_by\_CC only if the client pays by a credit card. Such features must be representable in the underlying formalism.

**Service enactment.** Service enactment deals with the execution of the process underlying the service. Interactions in the choreography interface must be first scheduled (i.e. ordered) according to the model specified by the control and data flow graphs, the service policy, etc., and then executed. Process scheduling is a non-trivial problem and solutions have typically high computational complexity [13]. Existing approaches to process scheduling can be classified as passive and proactive.

Passive schedulers receive sequences of events from an external source, such as a process or a transaction manager, and verify that these sequences satisfy all global constraints (possibly after reordering some events in the incoming sequences). Several such schedulers are described in [17, 2, 12]. In passive scheduling, an unspecified external system is supposed to ensure that scheduling complies with all the constraints, that liveness of the scheduling strategy is observed. The known algorithms for these tasks are worst-case exponential because verification of constraints happens at run time.

Proactive scheduling does not rely on external systems. Instead, it constructs a concise (as much as possible) explicit representation of all allowed executions (i.e., executions that are known to satisfy all constraints)—either in advance or dynamically. The representation of all valid schedules is then used by the scheduler. Depending on the expressive-ness of the framework, such scheduling can be linear at run time, since there is no need to verify constraints after the construction stage. In a sense, all constraints get compiled into the aforesaid concise representation. One such proactive approach is described in [7]. Although [7] proposes a linear run-time scheduler this is achieved by placing limits on process modelling, which does not permit transition conditions in control flow graphs and does not consider data flow.

3. THE BASICS OF CTR

The formalism used in this paper to model, reason, and enact service choreographies is Concurrent Transaction Logic or CTR [6]. This section provides a short summary of the relevant parts of CTR syntax and informally explains the semantics. Due to space limitation, we cannot discuss the model theory of the logic or its proof theory, but they can be found in [6].

CTR is a conservative extension of the classical predicate logic in the sense that both its proof theory and the model theory reduce to classical logic for formulas that do not cause state transitions (but only query the current state).
Basic syntax. The atomic formulas of CTR are identical to those of the classical logic, i.e., they are expressions of the form \( p(t_1, \ldots, t_n) \), where \( p \) is a predicate symbol and the \( t_i \)'s are function terms. More complex formulas are built with the help of connectives and quantifiers.

Apart from the classical \( \lor, \land, \neg, \forall \) and \( \exists \), CTR has two additional connectives, \( \otimes \) (serial conjunction) and \( \circ \) (concurrent conjunction), and two modal operators, \( \diamond \) (execu-
tional possibility) and \( \odot \) (isolated execution). For instance, \( \circ(p(X) \otimes q(X)) \) \( \circ(q(Y) \lor s(X, Y)) \) is a well-formed formula.

Informal semantics. Underlying the logic and its semantics is a set of database states and a collection of paths. For the purpose of this paper, the reader can think of the states as a set of relational databases, but the logic does not rely on the exact nature of the states—it can deal with a wide variety of them.

A path is a finite sequence of states. For instance, if \( s_1, s_2, \ldots, s_n \) are database states, then \( \langle s_1 \rangle, \langle s_1, s_2 \rangle, \ldots, \langle s_1, s_2, \ldots, s_n \rangle \) are paths of length 1, 2, and \( n \), respectively.

Just as in classical logic, CTR formulas assume truth values. However, unlike classical logic, the truth of CTR formulas is determined over paths, not at states. If a formula, \( \phi \), is true over a path \( \langle s_1, \ldots, s_n \rangle \), it means that \( \phi \) can execute starting at state \( s_1 \). During the execution, the current state will change to \( s_2, s_3, \ldots \), etc., and the execution terminates at state \( s_n \).

With this in mind, the intended meaning of the CTR connectives can be summarized as follows:

- \( \phi \otimes \psi \) means: execute \( \phi \) then execute \( \psi \). Or, model-theoretically, \( \phi \otimes \psi \) is true over a path \( \langle s_1, \ldots, s_n \rangle \) if \( \phi \) is true over a prefix of that path, say \( \langle s_1, \ldots, s_i \rangle \), and \( \psi \) is true over the suffix \( \langle s_i, \ldots, s_n \rangle \).
- \( \phi \mid \psi \) means: \( \phi \) and \( \psi \) must both execute concurrently, in an interleaved fashion.
- \( \phi \land \psi \) means: \( \phi \) and \( \psi \) must both execute along the same path. In practical terms, this is best understood in terms of constraints on the execution. For instance, \( \phi \) can be thought of as a transaction and \( \psi \) as a constraint on the execution of \( \phi \). It is this feature of the logic that lets us specify temporal constraints as part of process specifications.
- \( \phi \lor \psi \) means: execute \( \phi \) or execute \( \psi \) non-deterministically.
- \( \neg \phi \) means: execute in any way, provided that this will not be a valid execution of \( \phi \). Negation is an important ingredient in temporal constraint specifications.
- \( \circ \phi \) means: execute \( \phi \) in isolation, i.e., without interleaving with other concurrently running activities. This operator enables us to specify the transactional parts of process specifications.

Concurrent-Horn subset of CTR. Implication \( p \leftarrow q \) is defined as \( p \lor \neg q \). The form and the purpose of the implication in CTR is similar to that of Datalog: \( p \) can be thought of as the name of a procedure and \( q \) as the definition of that procedure. However, unlike Datalog, both \( p \) and \( q \) assume truth values on execution paths, not at states.

More precisely, \( p \leftarrow q \) means: if \( q \) can execute along a path \( \langle s_1, \ldots, s_n \rangle \), then so can \( p \). If \( p \) is viewed as a subroutine name, then the meaning can be re-phrased as: one way to execute \( p \) is to execute its definition, \( q \).

The control flow parts of service choreographies are formally represented using concurrent-Horn goals and concurrent Horn rules. A concurrent Horn goal is defined as follows:

- any atomic formula is a concurrent-Horn goal;
- \( \phi \otimes \psi, \phi \mid \psi, \phi \land \psi \) and \( \phi \lor \psi \) are concurrent-Horn goals, if so are \( \phi \) and \( \psi \);
- \( \circ \phi \) and \( \circ \phi \) are concurrent-Horn goals, if so is \( \phi \).

A concurrent-Horn rule is a CTR formula of the form \( head \leftarrow body \), where \( head \) is an atomic formula and \( body \) is a concurrent-Horn goal.

Observe that the definition of concurrent-Horn rules and goals does not include the connective \( \land \). In general, \( \land \) represents constrained execution, which is usually hard to implement, since constraints must be checked at every step of the execution. If a constraint violation is detected, a new execution path must be tried out. In contrast, the concurrent-Horn fragment of CTR is efficiently implementable, and there is an SLD-style proof procedure that proves concurrent-Horn formulas and executes them at the same time.

The efficiency gap between concurrent-Horn execution and constrained execution is the main motivation for our results. In a previous work by one of the authors [7], it was shown that for a certain class of constraints, formulas of the form \( ConcurrentHornGoal \land Constraints \) have an equivalent concurrent-Horn representation (which, therefore, does not use the connective \( \land \)). This enabled the use of the proof theory for Horn CTR as a means of obtaining a linear run-time scheduling algorithm (as opposed to, for example, exponential run-time scheduling in [18]).

In the present work, we consider a larger class of constraints than in [7], and this precludes the strategy used in [7]. We can still borrow some of the ideas from that early work and transform \( ConcurrentHornGoal \land Constraints \) into a conjunction that uses a smaller set of special kind of constraints. Although this conjunction cannot be further reduced to a concurrent Horn goal, we extend the proof theory of CTR to obtain a gain similar to [7]. Furthermore, we eliminate the need for having to compile away certain precedence constraints, which in [7] were handled in an expensive way. Instead, these constraints are now handled by the extended proof theory.

Elementary updates. We complete our informal introduction to CTR by explaining how execution of (some) formulas may actually change the underlying database state. Most of the machinery has already been introduced (albeit very informally). What is missing is the notion of elementary updates.

In CTR, elementary updates are represented by ordinary atomic, variable-free formulas. Syntactically, CTR does not distinguish elementary updates in any way, but the user may want to do so by adopting a syntactic convention (e.g., a convention could be that insert.p(t) represents the act of insertion of tuple \( t \) into the relation \( p \)).

What distinguishes elementary updates is their semantics. Through some black magic, called transition oracle,
CTR arranges that each elementary updates is always true along certain arcs, i.e., paths of the form \((s_1, s_2)\). Informally, one can think of an elementary update as a binary relation over states. For instance, if \((s_1, s_2)\) belongs to the relation corresponding to an elementary update \(u\), it means that \(u\) can cause a transition from state \(s_1\) to state \(s_2\). Note that an update can be non-deterministic (any one of a number of alternative state transitions might be possible) and it is possible for an update to be inapplicable in certain states (for instance, \text{delete.p}(t)\) may be applicable only if \(p(t)\) is true in the current state).

This mechanism is very general. It accounts for a wide variety of elementary state changes: from simple tuple insertions and deletions, to relational assignments, to updates performed by legacy programs, to whatever workflow activities might do. The connectives of CTR are then used to build more complex updates from the elementary ones and then to combine these complex updates into even more complex update programs. This process of building CTR programs from the ground up is very natural and powerful. The reader is referred to [3, 5, 6] for concrete examples.

4. MODELLING SERVICES WITH CTR

We now show how to use CTR to represent the control flow, constraints, and the data flow aspects of service choreographies.

4.1 Control Flow

In [7], it was shown that concurrent Horn goals are natural formalizations of so-called structured control flow graphs. Nodes in such graphs can be represented by propositions that act as elementary state transitions of CTR (see the end of the previous section). The connective \(\otimes\) represents sequential composition of interactions and is reflected by the arcs connecting adjacent nodes. The connective \(|\) is used to specify interactions that can be done in parallel; it is represented by the "AND"-nodes in the graph. Classical disjunction \(\lor\) represents non-deterministic choice and corresponds to the "OR"-nodes in the graphs. Transition conditions between adjacent nodes are modeled as queries that are sequentially composed with the formulas that label the nodes in question. Subworkflows (or complex interactions in service choreography—see Section 2) are modeled with rules. The head of such a rule represents the subworkflow's name (the name of a shaded box in Figure 2) and the body represents the subgraph corresponding to the subworkflow.

In this paper we model not only control flow but also data flow, so the nodes in the control graph are no longer propositions, but predicates with variables. These variables is one mechanism for specifying the data flow. Other data exchanges may happen through the database state. In this case, the producer inserts a data item into the shared database state, and the consuming interaction retrieves it. To illustrate, we use CTR to represent the flow of control and data for our running example (cf. Figures 2 and 4).

The CTR representation uses a special proposition, \(\text{path}\), to specify optional actions. It is defined as \(\phi \lor \neg \phi\), for some (does not matter which) formula \(\phi\). This means that \(\text{path}\) is true on all possible execution paths. It is a counterpart of the proposition “true” in classical logic. The proposition \(\text{path}\) will also be used to represent temporal constraints in our framework.

\[
\text{place}\_\text{order}(\text{Order}\#, \text{Price}) \leftarrow \\
\left( \left( \text{accept}\_\text{delivery}(\text{Order}\#) \otimes (\text{refund}(\text{Order}\#) \lor \text{path}) \right) \lor \left( \text{give}\_\text{security}(\text{Order}\#, \text{Price}) \lor \text{path} \right) \right) \lor \text{pay}(\text{Order}\#, \text{Price}) \\
\otimes (\text{pay}\_\text{cheque}(\text{Order}\#, \text{Price}) \lor \text{pay}\_\text{cc}(\text{Order}\#, \text{Price}) \lor \text{refund}(\text{Order}\#)) \rightarrow \text{return}(\text{Order}\#) \lor \text{partial}\_\text{refund}(\text{Order}\#) \\
\text{partial}\_\text{refund}(\text{Order}\#) \rightarrow \text{refund}(\text{Order}\#, \text{cc, CC}) \otimes \text{refund}(\text{Order}\#, \text{Amount}) \otimes \text{issue}\_\text{credit}(\text{CC}, \text{Amount}) \otimes \text{pay}\_\text{cheque}(\text{Order}\#, \text{Price}) \rightarrow \text{get}\_\text{cheque}(\text{Price, Cheque}) \otimes \text{insert}\_\text{payment}(\text{Order}\#, \text{cc, CC}) \otimes \text{charge}(\text{CC}, \text{Price}) \\
\text{give}\_\text{CC}(\text{Order}\#, \text{CC}) \rightarrow \text{payment}(\text{Order}\#, \text{cheque, Cheque}) \otimes \text{send}\_\text{check}(\text{Order}, \text{Amount}) \otimes \text{pay}\_\text{by}\_\text{cheque}(\text{Order}\#, \text{Price}) \rightarrow \text{get}\_\text{cheque}(\text{Price, Cheque}) \otimes \text{insert}\_\text{payment}(\text{Order}\#, \text{cheque, Cheque}) \\
\text{pay}\_\text{by}\_\text{CC}(\text{Order}\#, \text{Price}) \rightarrow \text{payment}(\text{Order}\#, \text{cc, CC}) \otimes \text{charge}(\text{CC}, \text{Price})
\]

(1)

One can see that, in this representation, rules are used to represent subworkflows and variables (such as \text{Order}\#) to pass data among choreography interactions. Other instances of data flow, such as passing the credit card number from \text{give}\_\text{CC} to \text{partial}\_\text{refund} is done through the underlying state: the credit card number is inserted into the state by \text{give}\_\text{CC} and queried by \text{partial}\_\text{refund}.

4.2 Events and Constraints

In process-oriented information systems, tasks are typically modeled in terms of their externally observable events, such as \text{start}, \text{commit}, \text{precommit}, \text{abort}, \text{terminated}, etc. Such events can be directly incorporated as nodes in a control flow graph. (For brevity, our running example collapses different occurrences of the same type of event. To illustrate, our running example collapses all significant events for the same task into one event.) Temporal and causality constraints among nodes of the graph are then expressed in terms of these events. In this work, we restrict choreographies to be non-iterative, which means that we do not use recursive CTR rules.

Definition 4.1 (Assumptions). We make the following assumptions, which simplify the discussion, but do not limit the generality of the approach.

- No significant event occurs twice during the execution.
- Each significant event is represented as an elementary update that applies in every state.

The first assumption does not limit generality, since we are dealing with non-iterative processes and can always rename different occurrences of the same type of event. The second assumption means that we require each significant event to leave a footprint in the underlying database state. This is commonly done by maintaining a system log where footprints are recorded.

The first assumption above translates into the following \textit{unique event property}.

Definition 4.2 (Unique Event Property). A concurrent-Horn goal \(G\) has the unique event property if and only if every significant event occurs at most once in every execution of \(G\). In such cases, we shall also say that \(G\) is a unique-event goal.
Unique-event goals can be recognized in linear time in the size of the goal. It is easy to see that the unique event property implies the following:

- If \( G = E_1 \otimes E_2 \) is a unique-event goal and \( \alpha \) occurs in \( E_1 \) then it cannot occur in \( E_2 \).
- If \( G = E_1 \mid E_2 \) is a unique-event goal and \( \alpha \) occurs in \( E_1 \) then it cannot occur in \( E_2 \).
- If \( G = E_1 \lor E_2 \) then \( G \) is a unique-event goal if and only if so are both \( E_1 \) and \( E_2 \).

In the rest of this paper, all concurrent-Horn goals are assumed to have the unique event property.

Transaction Logic can express a wide variety of temporal constraints [4], but in this paper we are looking for sets of constraints that are general enough to be used for service policies and client contracts and such that the computational complexity of reasoning about such constraints is better than what follows from known results. Earlier [7] studied reasoning about set of constraints, which subsume Singh's Event Algebra [18]. In this paper, we extend this set to cover all constraints of the DecSerFlow language [19].

Using these constraints we can specify that one task must start before some other task, that one task must start before some other task, that one task must start immediately after another one finished executing, that the execution of one task causes some other task to be executed or not executed, etc. The DecSerFlow constraints [19] are believed to be sufficient for the needs of process-aware information systems.

We specify all significant events in the system as formulas drawn from a set denoted by \( \mathcal{VENT} \). Note that, unlike [7], we use predicates with variables— not just propositions—to represent control and data flow. In [7], the events could be simple propositions, but in our case they are existentially quantified atomic formulas of the form

\[ 3DDataFlowVars eventName(DataFlowVars) \]

Here \( eventName \) is the event (or interaction) that is supposed to happen (or not happen), and \( DataFlowVars \) are the data flow parameters used in modeling this event (see (3), for example).

**Definition 4.3**: Constraints. The basic building blocks of \( \mathcal{CONST} \) are formulas of the form \( \text{path} \otimes e \otimes \text{path} \otimes e \), and \( e \otimes \text{path} \), where \( e \in \mathcal{VENT} \). Then the following constraints form the constraint algebra \( \mathcal{CONST} \):

1. **Primitive constraints**: If \( e \in \mathcal{VENT} \) then \( \text{path} \otimes e \otimes \text{path} \) (event \( e \) must happen) and \( \neg (\text{path} \otimes e \otimes \text{path}) \) (event \( e \) must not happen) are primitive constraints in \( \mathcal{CONST} \). For convenience we introduce a shorthand notation \( \forall e \) for \( \text{path} \otimes e \otimes \text{path} \). Then we say that \( \forall e \) is a positive primitive constraint and \( \neg \forall e \) is a negative primitive constraint.

2. **Immediate serial constraints**: If \( e_1, \ldots, e_n \in \mathcal{VENT}, \) then \( \text{path} \otimes (e_1 \otimes \cdots \otimes e_n) \otimes \text{path} \) (events \( e_1, \ldots, e_n \) must happen next to each other with no other events in-between) is a (positive) immediate serial constraint in \( \mathcal{CONST} \). We use \( v \otimes (e_1 \otimes \cdots \otimes e_n) \otimes \text{path} \) to represent \( \text{path} \otimes e_1 \otimes \cdots \otimes e_n \otimes \text{path} \).

This type of constraints is quite hard to enforce, and it was not allowed in [7]. We will see a use of such a constraint in our running example.

3. **Serial constraints**: If \( s_1, \ldots, s_n \in \mathcal{CONST} \) are positive primitive constraints or positive immediate serial constraints, then \( s_1 \otimes \cdots \otimes s_n \in \mathcal{CONST} \) is a serial constraint. We will also sometimes call constraints of the form \( \forall a \otimes \forall b \) plain serial constraints (as opposed to the immediate ones).

4. **Complex constraints**: If \( C_1, C_2 \in \mathcal{CONST} \) then \( C_1 \land C_2 \), and \( C_1 \lor C_2 \).

*Nothing else is in \( \mathcal{CONST} \). □*

To get a better picture of what can be expressed using \( \mathcal{CONST} \), we show some examples.

- \( \forall e \land \forall f \) — events \( e \) and \( f \) must both occur (in any order).
- \( \neg \forall e \land \neg \forall f \) — it is not possible for \( e \) and \( f \) to happen together.
- \( \forall e \lor \forall f \) — if event \( e \) occurs, then \( f \) must also occur (before or after \( e \)). This can be more naturally represented using implication: \( \forall e \rightarrow \forall f \).
- \( \forall e \land \forall f \) — if event \( f \) has occurred, then event \( e \) must have occurred some time prior to that.
- \( \forall e \lor \forall f \lor (\forall e \otimes \forall f) \) — if both \( e \) and \( f \) occur, then \( e \) must come before \( f \). Equivalently: \( \forall e \land \forall f \rightarrow (\forall e \otimes \forall f) \).
- \( \forall e \land \forall f \lor (\forall e \otimes f) \) — if event \( e \) occurs, then \( f \) must occur right after \( e \) with no event in-between.
- \( \forall v \lor \neg (\forall v \otimes (k \otimes d)) \) — if both \( k \) and \( d \) occur then \( d \) must happen right after \( k \) with no other event in-between. Equivalently: \( \forall v \land \neg (\forall v \otimes (k \otimes d)) \).

It was also shown in [7] that the constraints in \( \mathcal{CONST} \) (without the immediate serial constraints) can be converted to the following normal form:

\[ \forall_i (\lambda_{i}, \text{serialConstr}_{i,j}) \]  

(2)

where each \( \text{serialConstr}_{i,j} \) is either a primitive constraint, an immediate serial constraint, or a serial constraint composed of two positive primitive constraints. This rule generalizes to the constraints of the form \( \forall \land (\ldots) \) quite easily, because any immediate serial constraint of the form \( \forall \land (a \otimes b \otimes c) \) is equivalent to \( \forall \land (a \otimes b) \land \forall \land (b \otimes c) \). Therefore, any immediate serial constraint can be replaced with a conjunction of binary such constraints.

Although Definition 4.3 does not explicitly state that \( \mathcal{CONST} \) is closed under negation, it was shown in [7] that (without the immediate serial constraints) it is. This makes it possible to express some constraints easier than otherwise. For instance:

- \( \neg (\forall e \otimes \forall f) \) — it is not possible for \( f \) to occur after \( e \) (and for \( e \) before \( f \)). Without direct negation of a serial constraint, this would be much more complex: \( \neg (\forall e \land (\forall e \otimes \forall f)) \).
- \( \neg (\forall e \otimes \forall f \otimes \forall g) \) — if \( e \) happens and then \( f \), then \( g \) cannot come later.

The result of [7] that \( \mathcal{CONST} \) is closed under negation can be extended to include constraints of the form \( \forall \land (\ldots) \), but this requires a new construct: existential events, denoted \( \forall_i \), for \( i = 1, \ldots, n \). A constraint of the form \( \forall_i \land (\forall a \otimes \forall b) \) means that some event from \( \mathcal{VENT} \) must occur before \( b \). A constraint \( (\forall_i \otimes \forall b) \land (\forall a \otimes \forall b') \) means that some event must occur before \( b \) and the same event must occur after \( a \). That is, it must occur in-between \( a \) and \( b \). By the unique
event property, this event must be different from both a and b and, therefore, a cannot be immediately followed by b.

We will now extend $\mathcal{E}_{\text{VENT}}$ with symbols $?_1, ?_2, \ldots$, where each $?_i$ represents some concrete, but unknown event from $\mathcal{E}_{\text{VENT}}$. With this in mind, we can see that negation of any binary immediate serial constraint $\neg \diamond (a \otimes b)$ is equivalent to a constraint where negation is applied only to primitive events: $\neg a \lor \neg b \lor (a \otimes ?_i) \lor (\neg ?_i \otimes b)$, for some $?_i$, that does not occur elsewhere in $\mathcal{C}_{\text{CONST}}$. Since general immediate serial constraints can be split into binary ones, it shows that $\mathcal{C}_{\text{CONST}}$ is closed under application of negation to immediate constraints.

We can now show that $\mathcal{C}_{\text{CONST}}$ is sufficiently expressive to formalize the policy and contract constraints for our running example (see Figure 3). For readability, we use implication instead of the disjunctive form (2):

1. $\exists \text{Order}\# \exists \text{Price}$ \((\langle \text{accept\_delivery} (\text{Order}\#) \otimes \neg \text{pay\_by\_CC} (\text{Order}\#, \text{Price}) \rangle \rightarrow \langle \neg \text{accept\_security} (\text{Order}\#, \text{Price}) \otimes \text{accept\_delivery} (\text{Order}\#) \rangle)\)
2. $\exists \text{Order}\# \exists \text{Price}$ \((\langle \text{accept\_delivery} (\text{Order}\#) \otimes \text{pay\_by\_heque} (\text{Order}\#, \text{Price}) \rangle \rightarrow \langle \text{pay\_by\_heque} (\text{Order}\#, \text{Price}) \otimes \text{accept\_delivery} (\text{Order}\#) \rangle)\)
3. $\exists \text{Order}\# \exists \text{Price}$ \((\langle \neg \text{trebate} (\text{Order}\#) \rightarrow \text{pay\_by\_heque} (\text{Order}\#, \text{Price}) \otimes \text{accept\_delivery} (\text{Order}\#) \rangle)\)
4. $\exists \text{Order}\# \exists \text{Price}$ \((\langle \text{accept\_delivery} (\text{Order}\#) \otimes \text{pay\_by\_heque} (\text{Order}\#, \text{Price}) \rangle)\)

(3)

4.3 Data Flow and Conditional Control Flow

As explained in Section 4.1 and illustrated using the running example (see the representation (3)), data flow in CTR can be represented through shared variables or through the underlying database state. This captures all the usual forms of data flow in real systems, which occur through passing of parameters, messages, and through a shared persistent state.

From the service enactment point of view, data flow induces certain order constraints on the interactions specified in the choreography interface. These constraints can be culled directly from the data flow graph, and added to the set of constraints that constitute the policy of the service and the contract requirements of the user.

These constraints are constructed as follows. Consider an arc in the data flow graph that leads from node f to node g and suppose $f(U)$ and $g(V)$ are the predicates (with the associated variables) that represent these nodes in CTR (see the representation (3) for a concrete example). The constraint that is induced by that arc has to state that if both events $U = f(U)$ and $V = g(V)$ occur then the first must precede the second. Denoting the above events with $f$ and $g$ respectively, we can write the above as $\forall f \lor \forall g \lor (\forall f \otimes \forall g)$. Note that this is a conditional constraint. For instance, in our example the client may never provide a credit card number and, in this case, the interaction $\text{partial\_refund}$ does not need to wait for the interaction $\text{pay\_by\_CC}$.

In practice, we only need to add the constraints that correspond to the new arcs in the data flow graph. In Figure 4, these are the depicted as non-shaded arcs. This is because the constraints that correspond to the arcs that were inherited from the control flow graph (the shaded arcs on Figure 4) are already accounted for implicitly by the control flow graph itself.

This, the data flow constraints that for our running example are as follows:

1. $\exists \text{Order}\# \exists \text{CC}\# \exists \text{Price}$ \((\langle \text{give\_CC} (\text{Order}\#, \text{CC}\#) \otimes \neg \text{pay\_by\_CC} (\text{Order}\#, \text{Price}) \rangle \rightarrow \langle \neg \text{give\_CC} (\text{Order}\#, \text{CC}\#) \otimes \text{pay\_by\_CC} (\text{Order}\#, \text{Price}) \rangle)\)
2. $\exists \text{Order}\# \exists \text{Price}$ \((\langle \text{pay\_by\_CC} (\text{Order}\#, \text{Price}) \otimes \text{partial\_refund}\_\text{Order}\# \rangle \rightarrow \langle \text{pay\_by\_CC} (\text{Order}\#, \text{Price}) \otimes \text{partial\_refund}\_\text{Order}\# \rangle)\)

Conditions in the control graph can take many forms (e.g., linear, equality, and which are typically over some specific domains (e.g., integer, real, finite). In control flow graphs, the conditions attached to arcs are usually tests performed on the values of the variables that are passed between the nodes. In general, these conditions can be checked only at run time, during enactment, but in some cases certain inferences can be made statically. For instance, if the conditions are constraints for which solvers are available (e.g., linear constraints over the domain of reals) then certain parts of the control graph can be eliminated if we can show that the set of conditions attached to the arcs of some branch is unsatisfiable.

We now describe an algorithm, which traverses the control flow graph and cuts off the parts that cannot be enacted because their associated constraints are cumulatively unsatisfiable. The algorithm is based on a subroutine called CHECK\_NODE, which operates directly on the underlying control flow graph; this graph is not passed as a parameter. The input parameters are a node, $N$, in the graph and a constraint, which represents the cumulative constraint on the arcs that lead from the starting node in the graph to $N$. The algorithm starts simply by calling CHECK\_NODE\_\text{startNode}, true) and when it ends the control flow graph is reduced by cutting off dead branches.

The algorithm assumes that there is a constraint solver for the conditions attached to the arcs; it is invoked by calling a subroutine $\text{simplify}$, which takes a constraint and returns an equivalent constraint in a simplified form. If it detects that the input constraint is unsatisfiable, it returns $\text{false}$. Note that each node in the control graph is visited at most as many times as there are incoming edges. So, the algorithm is linear in the size of the graph. The real work is performed by the constraint solver when simplify is called. The complexity of this operation depends on the complexity of the constraints.

The other two operations in the algorithm delete parts of the underlying graph. The operation $\text{delete\_Subgraph\_At}$ removes the part of the graph that starts at node $N$. This is done by first deleting the edges of that subgraph and then deleting the isolated nodes (i.e., nodes that have no adjacent edges). The operation $\text{delete\_Branch\_At}$ takes an OR-split node $N$ and a successor node $S$. The successor node determines the OR-branch at node $N$ to be deleted. The branch is deleted from node $N$ to the corresponding OR-join node. The deletion is done similarly to deletion of a subgraph: first the edges of the branch are removed and then the isolated nodes are eliminated.

Algorithm CHECK\_NODE\_\text{N, Constr})

1. if $\text{successors}(N) == \emptyset$ then return Constr endif
2. foreach successor $S$ of $N$ do
3. if $c$ is the condition on the arc $\langle S, N \rangle$ do
4. $\text{cond}[S] = \text{CHECK\_NODE}(S, Constr + c)$
5. endfor
7. if N is not an OR-split node then
8. \[ c = \text{simplify}(\land_S \text{cond}[S]) \]
9. if \( c \equiv \text{false} \) then
10. deleteSubgraphAt(N)
11. return false
12. else return c
13. endif
14. else if N is an OR-node
15. foreach successor S of N do
16. \[ c[S] = \text{simplify}(\text{cond}[S]) \]
17. if \( c[S] \equiv \text{false} \) then
18. deleteBranchAt(N,S)
19. endif
20. endforeach
21. return \( \lor_S c[S] \)
22. endif

Figure 5 shows the result of applying \text{CHECKNODE} to the control flow graph 5(a). Although the conditions on the branch \( b \rightarrow g \rightarrow h \) in the graph are satisfiable, the conditions on \( b \rightarrow c \rightarrow e \rightarrow f \rightarrow h \) and \( b \rightarrow c \rightarrow d \rightarrow f \rightarrow h \) are (separately) unsatisfiable. Thus, the \( b \)-branch of node a is deleted. The same happens to the \( i \)-branch of a. On the other hand, the \( m \)-branch of node a is satisfiable, so it is left alone. The resulting graph with the dead parts cut off is shown in Figure 5(b).

Figure 5: (a) A control-flow graph with conditions attached to arcs. (b) Reduced graph with dead branches eliminated.

5. REASONING ABOUT CHOREOGRAPHY AND CONTRACTS

The problem we are now considering is whether there exists a way to schedule choreography interactions in a way that satisfies both the service policy and the client contract requirements. Formally, these problems can be formulated as follows.

Let \( C \) be a set of constraints from \( \text{CONSTR} \), which represents the union of the policy, contract, and data flora constraints, as discussed in Section 4. Let \( G \) be a concurrent-Horn goal that represents the control flow graph of the service choreography, and let \( H \) be the set of concurrent-Horn rules that represent the subworkflows of the control flow graph. Then

1. Contracting: The problem of determining if contracting for the service is possible is the problem of finding out if there is an execution of the CTR formula \( G \land C \) given the set of definitions \( R \), i.e., checking that there is a path \( s_1, \ldots, s_k \) such that \( R, s_1, \ldots, s_k \models G \land C \). This means that for any model \( M \) of \( R, G \land C \) is true in \( M \) on the path \( s_1, \ldots, s_k \).

2. Enactment: The problem of enactment is formally defined as finding a constructive proof that \( R, s_1, \ldots, s_k \models G \land C \) for some path \( s_1, \ldots, s_k \). A constructive proof is a sequence of inference rules of CTR that starts with an axiom and end with the formula \( G \land C \).

In this paper, we solve the above problems as follows. In the first phase, we translate the formula \( G \land C \) into an equivalent formula \( \lor_i (G_i \land \text{serialConstr}_{i,j}) \), where each \( \text{serialConstr}_{i,j} \) is either an immediate serial constraint or a (plain) serial constraint, and \( G_i \) is a concurrent-Horn goal. In this step we get rid of complex and primitive constraints. This transformation is a simplified version of the Apply transformation from [7], and each step in this transformation can be viewed as an inference rule in a proof theory. We present these transformation steps in Section 5.1. In the second phase, we extend the proof theory of Horn CTR to formulas of the form \( G \land \text{serialConstr}_{i,j} \), where result from the Phase 1 transformation, and then use that theory on these formulas. If we find a proof, it means that enactment of the service is possible. This extended proof system of Phase 2 is presented in Section 5.2.

In Phase 2, finding a proof and thus a possible enactment takes time linear in the size of the execution path. Unfortunately, as shown in [7], the very problems of contracting and enactment are NP-complete, and this issue arises in Phase 1: the Apply transformation is worst-time exponential in the size of the largest number of disjuncts in a constraint in \( C \). However, this is still better than the standard verification techniques, which are exponential in the size of \( G \lor C \) [14].

5.1 Phase 1: Transformation

The series of equivalence transformations, below, eliminates complex and primitive constraints by “compiling” them into the concurrent-Horn goal. More precisely, we take formulas of the form \( G \land C \), where \( C = \lor_i (\land_j \text{serialConstr}_{i,j}) \) and the \( \text{serialConstr}_{i,j} \) are either a primitive constraint, an immediate serial constraint, or a plain serial constraint and transform them into equivalent formulas of the form \( \lor_i (G_i \land \text{serialConstr}_{i,j}) \), where each \( \text{serialConstr}_{i,j} \) is an immediate serial constraint or a plain serial constraint. Although

\[ \text{Due to space limitation, we define this only informally. The reader is referred to [6] for the details.} \]
each transformation is an equivalence, we will use the symbol \(\vdash\) to indicate the direction of the transformation and the fact that we treat these transformations as inference rules.

**Definition 5.1 (Applying Complex Constraints).** Let \(T\) be a formula of the form \(G \land C\) where \(G\) is concurrent-Horn goal, and \(C\) is in the normal form. Then:

\[
T \land (C_1 \lor C_2) \vdash (T \land C_1) \lor (T \land C_2)
\]

**Definition 5.2 (Applying Primitive Constraints).** Let \(\alpha, \beta \in \mathcal{EvNet}\). Then:

\[
\begin{align*}
(\alpha \land \neg \alpha) & \vdash \alpha \\
(\beta \land \neg \alpha) & \vdash \neg \text{path} \quad \text{if } \alpha \neq \beta \\
(\alpha \land \neg \beta) & \vdash \neg \text{path} \\
(\beta \land \neg \alpha) & \vdash \beta \quad \text{if } \alpha \neq \beta
\end{align*}
\]

We remind that \(\neg \text{path}\) means inconsistency so if a conjunct reduces to \(\neg \text{path}\) then the whole conjunction is inconsistent and if a disjunct is found to be inconsistent then it can be eliminated.

Let \(T\) and \(K\) be concurrent-Horn goals and let \(\sigma\) stand for \(\forall \alpha \lor \neg \alpha\). Then we have the following transformations:

\[
\begin{align*}
(T \land K) \land \forall \alpha & \vdash (T \land \alpha) \land K \quad \text{if } \alpha \text{ occurs in } T \\
T \land (K \land \alpha) & \vdash (T \land \neg \alpha) \land (K \land \neg \alpha) \\
(T \mid K) \land \alpha & \vdash (T \mid \alpha) \mid K \quad \text{if } \alpha \text{ occurs in } T \\
T \mid (K \land \alpha) & \vdash (T \mid \neg \alpha) \mid (K \land \neg \alpha)
\end{align*}
\]

\[
\begin{align*}
\forall T & \vdash \forall (T \mid \sigma, T) \\
(T \lor K) \land \sigma & \vdash (T \lor \sigma) \lor (K \land \sigma)
\end{align*}
\]

The above series of transformations either lead to \(\neg \text{path}\) (i.e., inconsistency) or to a formula of the form \(\forall \_ (G_i \land \text{serialConstr}_{i,j})\), where each \(\text{serialConstr}_{i,j}\) is either an immediate serial constraint or a (plain) serial constraint. If the result is \(\neg \text{path}\), then enactment is not possible. If the result is a formula of the form \(\forall \_ (G_i \land \text{serialConstr}_{i,j})\), then scheduling might be possible. To check this, we need to use the inference rules introduced in the next section. These inference rules extend the proof theory for Horn CTR to formulas of the form \(G \land \_ \text{serialConstr}_{i,j}\).

### 5.2 Phase 2: Extended Proof Theory

This section develops a proof theory for formulas of the form \(G \land \_ \text{serialConstr}_{i,j}\). This is done in two steps. First, we check constraints for internal consistency and also eliminate some redundancy. If the constraints are consistent, then we go to step 2, which is based on inference rules. The first step is described in Section 5.2.1 and the second in Section 5.2.2.

#### 5.2.1 Constraint Graphs

Let \(C\) be the set of constraints of the form \(\forall x_1 \land \ldots \land \forall x_n\) or \(\forall \_ (x \land x_2 \land \ldots \land x_n)\), where \(x_i\) represents a task.

**Definition 5.3 (Consistency of Constraints).** The set of constraints \(C\) is said to be consistent if there is a path \(s_1, \ldots, s_n\) that satisfies all the constraints. \(\square\)

To help us harness the complexity of the interaction among the different types of serial constraints, we introduce the notion of a constraint graph.

**Definition 5.4 (Constraint Graph).** Constraint graph for a set of serial (immediate and plain) constraints \(C\) is a directed graph where the nodes represent the interactions appearing in the constraints. The graph has two kinds of edges: dashed and solid; they are defined as follows:

\[
\begin{align*}
\text{Edges}_{\text{solid}} & = \{ (x_i, x_j) \mid i \neq j, \lor (x_i \land x_j) \text{ is in } C \} \\
\text{Edges}_{\text{dashed}} & = \{ (x_i, x_j) \mid i \neq j, \lor x_i \land \lor x_j \text{ is in } C \}
\end{align*}
\]

Graphically, the arc from \(x_i\) to \(x_j\) is solid if \((x_i, x_j) \in \text{Edges}_{\text{solid}}\), and dashed if \((x_i, x_j) \in \text{Edges}_{\text{dashed}}\). \(\square\)

Figure 6 gives an example of a constraint graph for the constraints set \(\{ \lor c \land d \land e, \lor f \land g, \lor a \land \lor b \land \lor d, \lor h \land \lor i \land \lor k, \lor e \land \lor f \land \lor k \}\). Note that the last constraint here involves an existential event \(\_i\). These events were introduced in Section 4.2 to express constraints where some events are precluded from immediately following others.

**Figure 6:** A constraint graph.

**Definition 5.5 (Consistency of Constraint Graphs).** A constraint graph is consistent if and only if it was generated from a consistent set of constraints. \(\square\)

We identify several inconsistency patterns below. It turns out that a constraint graph is consistent if and only if it has no inconsistency patterns.

**Inconsistency pattern 1.** Constraint graph has a cycle.

Figure 7 shows a set of constraints \(\{ \lor (a \land b), \lor (c \land e), \lor (f \land \lor a) \}\), whose graph has a cycle. A cycle in a constraint graph implies that every execution that satisfies the constraints must have multiple occurrences of the same event, which violates the unique event property.

**Figure 7:** An example of pattern 1.

**Inconsistency pattern 2.** More than one solid arc goes into or out of a node.

Figure 8 illustrates this pattern for the constraints set \(\{ \lor (a \land b), \lor (c \land e), \lor (d \land \lor a) \}\).

Constraints whose graphs have such a pattern cannot be satisfied. For instance, in Figure 8 both \(b\) and \(c\) must occur right after \(a\). Since \(b\) and \(c\) are distinct tasks, this cannot happen because of the unique event property.

**Inconsistency pattern 3.** Any pair of nodes connected by
a solid path (i.e., a path that consists solid arcs only) and also by another path (solid or not) of length two or more.

Figure 9 illustrates this pattern for the constraints set \( \{ \nabla \odot (c \otimes d \otimes b), \nabla \odot (a \otimes e), \nabla c \otimes \nabla a, \nabla e \otimes \nabla b \} \).

Figure 9: An example of pattern 3.

An existence of pattern 3 means that the tasks on the solid path cannot be executed without being interrupted by the tasks on the second path. This violates the meaning of solid constraint.

**Lemma 5.6.** The constraint graph has no inconsistency patterns if and only if the corresponding set of constraints is consistent.

**Proof (Sketch):** Take a topological sort of the constraint graph. It exists, since the graph is acyclic (by the absence of inconsistency pattern 1 above). This topological sort may not be a valid execution of the events because the constraints of the form \( \nabla \odot (a \otimes b) \) are not necessary satisfied—there is no guarantee that \( b \) occurs right next to \( a \). However, taking advantage of the fact that patterns 2 and 3 do not occur, we can transform the topological sort into another topological sort by moving \( b \) backwards until it is right next to \( a \). Doing so for every violated immediate serial constraint eventually creates a topological sort that satisfies all constraints. □

**Definition 5.7 (Reduced Consistent Constraint Graph).** A consistent constraint graph is reduced if it does not have a pair of nodes that are connected by a dashed arc and some other path.

**Lemma 5.8.** Any consistent constraint graph has an equivalent reduced graph.

Figure 10 shows how a consistent graph can be reduced by deleting dashed arcs.

**Definition 5.9 (Exclusive Nodes).** An exclusive node is any node that occurs on a solid path in a consistent constraint graph, except the node which is at the beginning of that path.

**Definition 5.10 (Well-formed Constraint Graph).** A constraint graph is well-formed if it is consistent, reduced, and has no dashed arcs pointing to an exclusive node.

**Definition 5.11 (Well-formed Set of Constraints).** A well-formed set of constraints is a set of constraints whose constraint graph is well formed.

**Lemma 5.12.** Any consistent set of constraints has an equivalent, effectively constructible set of well-formed constraints.

**Proof (Sketch):** A reduced consistent constraint graph can be transformed into a well-formed constraint graph as follows. Any dashed arc that points to an exclusive node in such a graph can be redirected to point to the head of the solid path of that exclusive node. Repeating this for every dashed arc that violates well-formedness eliminates these violations. This is illustrated in Figure 11 for the constraints: \( \nabla \odot (c \otimes d \otimes b), \nabla \odot (a \otimes e), \nabla c \otimes \nabla a, \) and \( \nabla e \otimes \nabla b \).

**Figure 11:** (a) Consistent graph; (b) an equivalent well-formed graph.

### 5.2.2 Extended Inference System

First, we recall the notion of hot components of a formula from [6]: hot(\( \psi \)) is a set of subformulas of \( \psi \) which are “ready to be executes.” This set is defined inductively as follows:

1. hot(\( \psi \)) = \( \psi \), if \( \psi \) is an atomic formula
2. hot(\( \psi \otimes \phi \)) = hot(\( \psi \))
3. hot(\( \psi | \phi \)) = hot(\( \psi \)) | hot(\( \phi \))
4. hot(\( \psi \lor \phi \)) = \( \psi \lor \phi \)

Let \( \psi \) be a concurrent serial goal and \( C \) a set of constraints with a well-formed constraint graph.

**Definition 5.13 (Enabled Components).** The set of enabled components of \( C \) is as follows: enabled(\( C \)) = \{ \( x \) | \( x \) is a root node of \( C \) or \( x \) is not in \( C \) \}.

**Definition 5.14 (Eligible Components).** The set of eligible components of \( \psi \), eligible(\( \psi \)), is defined as follows:

\[
\text{eligible}(\psi) = \begin{cases} 
 x, & \text{if } x \in \text{hot}(\psi) \cap \text{enabled}(C) \\
 \text{hot}(\psi) \cap \text{enabled}(C), & \text{and } x \text{ is an exclusive node in } C 
\end{cases}
\]

It is easy to see that eligible(\( \phi \)) \( \subseteq \) hot(\( \phi \)). □
Let $P$ be a set of concurrent Horn rules. We now define an extended proof theory for constrained CTR goals. This system expresses proof sequents of the form $P, D \vdash \exists \psi$, called sequents, where $P$ is a set of Horn CTR rules and $D$ is the underlying database state. The informal meaning of such a sequent is that the transaction $\exists \psi$, which is defined by the rules in $P$, can succeed from $D$, i.e., it can execute on a path starting at database $D$. Each inference rule consists of two sequents, one above the other, and has the following interpretation: If the upper sequent can be inferred, then the lower sequent can also be inferred. As in classical resolution, any instance of an answer-substitution is a valid answer to a query.

The extended inference system is almost identical to the inference system for Horn CTR in [6] except for two subtle differences:

1. In the extended system, the inference rule 3 operates on eligible occurrences of atomic formulas, while in the inference system of [6] it was operating on a larger set of hot occurrences.

2. Rules 1 and 3 also modify the set of constraints.

Note that the new system reduces to the old one when the set $C$ of constraints is trivial.

**Axioms:** $P, D \vdash \gamma$, for any database state $D$.

**Inference Rules:** In rules 1-4 below, $\sigma$ denotes a substitution, $\psi$ and $\psi'$ are concurrent serial goals, $C$ and $C'$ are constraint sets with well-formed constraint graphs, $D_1, D_2$ denote database states, and $a$ is an atomic formula in $\text{eligible}(\psi)$.

1. **Applying transaction definitions:** Let $b \vdash \beta$ be a rule in $P$, and assume that its variables have been renamed so that none are shared with $\psi$. If $a$ and $b$ unify with the most general unifier $\sigma$ then

   \[
   P, D \vdash \exists \psi (\psi' \land C') \sigma
   \]

   where $\psi'$ is obtained from $\psi$ by replacing a hot occurrence of $a$ by $\beta$, and $C'$ is constructed as follows. Let $Y_1, \ldots, Y_k$ be the events mentioned in $C$, which appear in $\beta$. Then
   - for each arc from a to a node $X$ in the graph of $C$, delete the arc and replace it with the same kind of arc form each $Y_i$ to $X$.
   - for each arc from a node $X$ in $C$ to $a$, delete the arc and replace it with the same kind of arc form $X$ to each $Y_i$.

2. **Querying the database:** If $\mathcal{O}^a(D, D) \vdash \exists \psi \sigma$ and $a \sigma$ and $C' \sigma$ share no variables then

   \[
   P, D \vdash \exists \psi (\psi' \land C) \sigma
   \]

   where $\psi'$ is obtained from $\psi$ by deleting a hot occurrence of $a$.

3. **Executing elementary updates:** If $\mathcal{O}^a(D_1, D_2) \vdash \exists \psi \sigma$ then

   \[
   P, D_2 \vdash \exists \psi (\psi' \land C') \sigma
   \]

   \[
   P, D_1 \vdash \exists \psi \psi' \land C
   \]

   where $\psi'$ is obtained from $\psi$ and $C'$ from $C$ by
   - (a) deleting an eligible (not just hot) occurrence of $a$.
   - (b) deleting all eligible occurrences of the existential events of the form $?i$. (Existential events were defined in Section 4.2.)

4. **Executing atomic transactions:** If $\exists \alpha$ is a hot component in $\psi$ then

   \[
   P, D \vdash \exists \psi (\alpha \oplus \psi') \land C
   \]

   where $\psi'$ is obtained from $\psi$ by deleting an eligible occurrence of $\exists \alpha$.

**Theorem 5.15.** The above inference rules are sound and complete for proving constraint CTR goals from a set of CTR Horn rules.

**Proof (Sketch):** Let $G \land C$ be a constrained goal where $G$ is a concurrent Horn goal and $C$ a set of serial constraints with a well-formed constraint graph. We can transform proofs of $G$ into proofs of $G \land C$ by delaying the inference rules that apply to hot, but ineligible components of $G$.

6. **RELATED WORK**

Relationship to our previous work [7, 8] has already been discussed in the introduction.

Much of the work in the area of service contracting focuses on defining frameworks, models, and architectures (see [15] for a survey) trying to capture different aspects and phases of e-contracting, such as negotiation, contract establishment, enforcement, violation detection, monitoring, legal aspects, etc. In our paper we use a simple yet realistic and useful framework for e-contracting and solve a concrete problem that arises in establishing of contracts and enacting Web services. In this spirit, the work [11] is the closest to our approach. Here the problem of checking the compliance of business processes with business contracts is described and both processes and contracts rules are represented in a formal contract language (FCL) [10]. To compare, our language for constraints is more expressive than FCL. For instance, immediate serial constraints are outside of FCL. Second, [11] essentially gives a semantic definition for compliance, but no practical algorithm. In contrast, our work provides a number of algorithms and optimizations whose complexity is better than the known results.

Workflow/Process modeling has seen growing interest with the emergence of the area of process-aware information systems (PAIS) [9]. In [1] a set of workflow patterns is analyzed and in [20] Aalst proposed a concrete language, YAWL, based on these patterns. Since YAWL was a procedural language, Aalst later proposed a constraint-based, declarative language DecSerFlow [19]. As mentioned, our framework includes all the constraints used in DecSerFlow. It integrates them with conditional control flows, data flows, and provides reasoning mechanisms.

In process modeling, the main tools are Petri nets, process algebras, and temporal logic, and model checking has been often used for process verification. The advantage of CTR over these approaches is that it is a unifying formalism that integrates a number of process modeling paradigms ranging
from conditional control flows to data flows to hierarchical modeling to constraints, and even to game-theoretic aspects of multiagent processes (see, for example, [8]). Moreover, CTR models the various aspects of processes in distinct ways, which enabled us to devise algorithms with better complexity than the previously known general techniques from the model checking area. For instance, the complexity in the decision problems considered in this paper is polynomial in the size of the control flow graph and is exponential in the size of the set of constraints. In contrast, the approaches that are based on Petri nets, process algebras, and temporal logics that are exponential in the size of the control flow graph (which is encoded as part of the set of constraints) [19, 17, 18, 2, 12].

7. CONCLUSIONS

We have formulated the problems of choreography, contracting, and enactment for semantic Web services using the formalism of Concurrent Transaction Logic (CTR). We presented several reasoning techniques, which make it possible to decide if automatic contracting for a service is possible, find a choreography that obeys the policy of the service and the conditions of the contract, and then enact the service. Apart from semantic Web, these results also apply to workflow scheduling. They extend the work of [7] by incorporating data flow, conditional control transitions, and extend the set of allowed constraints. This work also makes contribution to CTR itself by extending its proof theory to handle constrained concurrent Horn goals.

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8. REFERENCES