HOMEWORK 1

Homework has 3 PARTS and 6 Problems

SOLVE as many problems as possible.
I will post Solutions so you could compare your solutions with mine.
HMKs PROBLEMS will appear on your TEST

SUBMIT **ONLY ONE PROBLEM** from each PART.

You must **TYPE the statement of each problem** you are solving and must **TYPE** your solutions, otherwise problem will not be considered for correction.

Submit HMK as a TEAM by e-mail to TA You must include TEAM Number and Names and IDs of all team members on a FRONT page.

PART ONE

- 1. CONCEPTUALIZATION DEFINITION (NILSON)
- **Conceptualization** step one of formalization of knowledge in declarative form.
- C = (U, F, R)
- U Universe of discourse; it is a FINITE set of objects.
- F Functional Basis Set; Set of functions (defined on U). Functions may be partial.
- **R** Relational Basis Set; Set of relations defined on **U**.
- Remark: sets **R**, **F** are FINITE.

PROBLEM 1

Conceptualize the following situation using the above definition.

In a room there are 3 girls, 4 boys, and 2 cars – one red and one blue. The following properties must be true.

1. Each girl likes exactly one boy.

- 2. Some boys like some girls.
- 3. Everybody (boys and girls) like some car.
- 4. Three boys like a red car.
- **5.** Two girls like a blue car. Use the following notation

U – Universe of discourse is the set

$$U = \{ 01, 02, 03, 04, 05, 06, 07, 08, 09 \}$$

R – Relational Basis Set; Set of relations

R = { GIRL, BOY, CAR, REDCAR, BLUECAR, LIKE}

USE INTENDED Interpretation, i.e.

Relation **GIRL** is defined by a property x is a girl Relation **BOY** is defined by a property x is a boy Relation **CAR** is defined by a property x is a car Relation **CAR** is defined by a property x is a car Relation **REDCAR** is defined by a property x is a red car Relation **BLUECAR** is defined by a property x is a blue car

Relation **LIKE** is defined by a property x likes y

Remark that the relations GIRL, BOY, CAR, REDCAR, BLUECAR are one argument relations and the relation

LIKE is a two argument relation and all of them are defined on the Universe **U**

PART TWO

PREDICATE LOGIC CONCEPTUALIZATION

1. Translations from Natural Language

PROBLEM 2

- **P1. Translate** into plain English predicate logic examples from our MAIN **BOOK**, **page 23 P2. Write a FULL solution** following the Predicate Logic (1) Lecture Notes, with explanation and justification of correctness for the examples on the main **book page 24**, i.e. follow the steps:
- 1. **Identify** the domain: always a set $X \neq \phi$
- 2. **Identify** predicates (simple: atomic)
- 3. **Identify** functions (if needed)
- 4. **Identify** the connectives
- 5. **Identify** the quantifiers $\forall x$, $\exists x$ or Restricted Quantifiers $\forall P(x)$, $\exists Q(x)$
- 6. **Write** a formula using symbols from **2,3,4,5 Use restricted domain quantifier translation rules**, where needed
- 7. **Write LOGIC formula** without Restricted Quantifiers

P3. This Problem is about different Knowledge representations

FOLLOW PROBLEM 2 steps to write detailed solution to part b) of **problems 2, 3** from our MAIN BOOK, **page 39.** Follow the Book or Busse Notes to write solution of part a)

PREDICATE LOGIC CONCEPTUALIZATION

2. Translations from Mathematics Language

PROBLEM 3

Here is a mathematical statement **S**:

For all natural numbers n the following implication holds:

IF n < 0, then there is a natural number m, such that m+n < 0

- 1. Re-write S as a "formula" **MF** that only uses mathematical and logical symbols
- 2. Translate your **MF** to a correct **logic formula LF**
- 3. Argue whether the statement **S** it true of false

PART THREE

RULE BASED SYSTEMS

PROBLEM 4

- **P1.** CONCEPTUALIZE problem 5 from our MAIN BOOK, page 39 in **Propositional Logic** and solve it using Conflict Resolution.
- **P2.** CONCEPTUALIZE problem 5 from our BOOK, page 39 in **Predicate Logic convention** using predicates **attribute(x, value of attribute)**, **attribute(object, value of attribute)**

WRITE a format of a database TABLE needed for solution of **P2**

PROBLEM 5

CONCEPTUALIZE the EXAMPLE (Rules R1- R4) on page 47 of the BOOK in **Propositional Logic.**

EXPLAIN the role of Questions posed to the system (in your conceptualization) and use backward chaining to solve the problem depending on the answers given to the system.

PROBLEM 6

P1. Write detailed solution to problems 2 from BUSSE BOOK

P2. Write detailed solution to problems 4 from BUSSE BOOK