

Cse352

Artificial Intelligence

Short Review

for Midterm

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Midterm

- Midterm INCLUDES
- CLASSIFICATION
- CLASSIFICATION by Decision TREES
- and
- PRODUCTION SYSTEMS
- PROPOSITIONAL RESOLUTION
- material you needed to review for Q1

Learning Process

- **Questions:**
- Describe and discuss all stages of the **Data Mining-Learning Process**
- Describe the role of **Preprocessing stage** and its main methods
- Discuss the **Data Mining –Learning Proper** stage
- Describe what is **Descriptive/ non Descriptive Learning**
Which **Models** you would use for the **Descriptive Learning** and which for the **non Descriptive Learning**
- How and what decides **which type** of Learning is the best to use (implement)
- Give examples **of types of applications** and the **best Models** (algorithms) for them

Classification

- Describe what is **CLASSIFICATION**; type of data, goals and applications
- Describe **all stages** of the **classification process**
- Describe and discuss **basic classification Models** and their **differences**
- Discuss the **Decision Tree Induction** and its strengths and weaknesses
- Define a **CLASSIFIER**
- Describe a process of **building a CLASSIFIER**

Classification Data and Rules

Given a **classification** dataset **DB** with a set

A = {*a1, a2, ..., an*} of **attributes** and a **class** attribute **C**
with values

{*c1, c2, ..., ck*} - **k** classes

Definition 1

Any expression ***a1 = v1 & ... & ak = vk*** where ***ai* ∈ A**
and ***vi*** are corresponding values of attributes from **A**

is called a **DESCRIPTION**

Any expression ***C = ci*** is for ***ci* ∈ {*c1, c2, ..., ck*}**

Is called a **CLASS DESCRIPTION**

Classification Data and Rules

Definition 2

A **CHARACTERISTIC FORMULA** is any expression

$$C = ck \Rightarrow a1 = v1 \ \& \ \dots \ \& \ ak = vk$$

We write it as

$$\text{CLASS} \Rightarrow \text{DESCRIPTION}$$

Definition 3

A **DETERMINANT FORMULA** is any expression

$$a1 = v1 \ \wedge \ \dots \ \wedge \ ak = vk \Rightarrow C = ck$$

We write it as

$$\text{DESCRIPTION} \Rightarrow \text{CLASS}$$

Classification Data and Rules

Definition 4

A characteristic formula

$$\mathbf{CLASS} \Rightarrow \mathbf{DESCRIPTION}$$

is called a **CHARACTERISITIC RULE** of the classification dataset **DB**
iff

it is **TRUE** in **DB**, i.e. when the following holds

$$\{\mathbf{o: DESCRIPTION}\} \cap \{\mathbf{o: CLASS}\} \text{ not} = \emptyset$$

Where

$$\{\mathbf{o: DESCRIPTION}\}$$

is the set of all records of DB corresponding to the **DESCRIPTION**

$\{\mathbf{o: CLASS}\}$ is the set of all records of DB corresponding to the **CLASS**

Classification Data and Rules

Definition 5

A discriminant formula

DESCRIPTION \Rightarrow CLASS

is called a **DISCRIMINANT RULE** of **DB**

iff

it is **TRUE in DB**, i.e. the following conditions hold

1. **$\{o: \text{DESCRIPTION}\} \text{ not} = \emptyset$**
2. **$\{o: \text{DESCRIPTION}\} \subseteq \{o: \text{CLASS}\}$**

PROBLEM 1

Prove

that for any **classification** data base **DB**
and any of its **DISCRIMINANT RULES** of the form

DESCRIPTION \Rightarrow CLASS

the formula \subseteq

CLASS \Rightarrow DESCRIPTION

is a **CHARACTERISTIC RULE** of the **DB**

PROBLEM 1 Solution

By **definition 5**, for any database DB :

DESCRIPTION \Rightarrow CLASS

is a **DISCRIMINANT RULE** iff

1. **$\{o: \text{DESCRIPTION}\} \text{ not} = \emptyset$**

2. **$\{o: \text{DESCRIPTION}\} \subseteq \{o: \text{CLASS}\}$**

Therefore,

$\{o: \text{DESCRIPTION}\} \cap \{o: \text{CLASS}\} \text{ not} = \emptyset$

and by **Definition 4**

CLASS \Rightarrow DESCRIPTION

Is the **CHARACTERISITIC RULE**

PROBLEM 2

Given a dataset:

Record	A1	A2	A3	A4	C
O1	1	1	1	0	1
O2	2	1	2	0	2
O3	0	0	0	0	0
O4	0	0	2	1	0
O5	2	1	1	0	1

Find the set **{o :DESCRIPTION}**
for the following descriptions

- 1) $a1 = 2 \ \& \ a2 = 1$
- 2) $a3 = 1 \ \& \ a4 = 0$
- 3) $a2 = 0 \ \& \ a3 = 2$
- 4) $c=1$
- 5) $c=0$

PROBLEM 2 SOLUTION

Find the set **{o :DESCRIPTION}**
for the following descriptions

1) $a_1 = 2$ & $a_2 = 1$

Answer : {o1 }

2) $a_3 = 1$ & $a_4 = 0$

Answer : {o1 , o5}

3) $a_2 = 0$ & $a_3 = 2$

Answer : {o4}

4) $c=1$

Answer : {o1,o5}

5) $c=0$

Answer : {o3 ,o5}

PROBLEM 3

For the following formulae use proper definitions to determine (it means **prove**) whether **they are / are not DISCRIMINANT / CHARACTERISTIC RULES** of our dataset.

$$6) \quad a_1 = 1 \ \& \ a_2 = 1 \Rightarrow C = 1$$

$$7) \quad C = 1 \Rightarrow a_1 = 0 \ \& \ a_2 = 1 \ \& \ a_3 = 1$$

$$8) \quad C = 2 \Rightarrow a_1 = 1$$

$$9) \quad C = 0 \Rightarrow a_1 = 1 \ \& \ a_4 = 0$$

$$10) \quad a_1 = 2 \ \& \ a_2 = 1 \ \& \ a_3 = 1 \Rightarrow C = 0$$

$$11) \quad a_1 = 0 \ \& \ a_3 = 2 \Rightarrow C = 1$$

PROBLEM 3 SOLUTION

For the following formulae use proper definitions to determine (it means prove) whether they are / are not **DISCRIMINANT / CHARACTERISTIC RULES** of our dataset.

6) $a_1 = 1 \ \& \ a_2 = 1 \Rightarrow C = 1$

$\{o_1\}$ is a subset of $\{o_1, o_5\}$ so this is a **DISCRIMINANT** rule

7) $C = 1 \Rightarrow a_1 = 0 \ \& \ a_2 = 1 \ \& \ a_3 = 1$

$\{o: a_1 = 0 \ \& \ a_2 = 1 \ \& \ a_3 = 1\}$ is an empty set so this is **not** a **CHARACTERISTIC** rule

8) $C = 2 \Rightarrow a_1 = 1$

As the intersection is empty so this is **not** a **CHARACTERISTIC** rule

9) $C = 0 \Rightarrow a_1 = 1 \ \& \ a_4 = 0$ ----- $\{o_3, o_4\} \wedge \{o_5\}$ is empty set so this is

not a **CHARACTERISTIC** rule

10) $a_1 = 2 \ \& \ a_2 = 1 \ \& \ a_3 = 1 \Rightarrow C = 0$ ----- $\{o_5\}$ is not a subset of $\{o_3, o_4\}$, so this is

not a **DISCRIMINANT** rule

11) $a_1 = 0 \ \& \ a_3 = 2 \Rightarrow C = 1$ ----- $\{o_4\}$ is not a subset of $\{o_1, o_5\}$, so this is

not a **DISCRIMINANT** rule

Classification

- Describe **what is Classification**; which is the goal, what data one needs etc....
- Describe all **stages** of the **Classification Process**
- Describe **basic methods** of training and testing
- Describe the **process of building a CLASSIFIER**
- What is a **CLASSIFIER**?

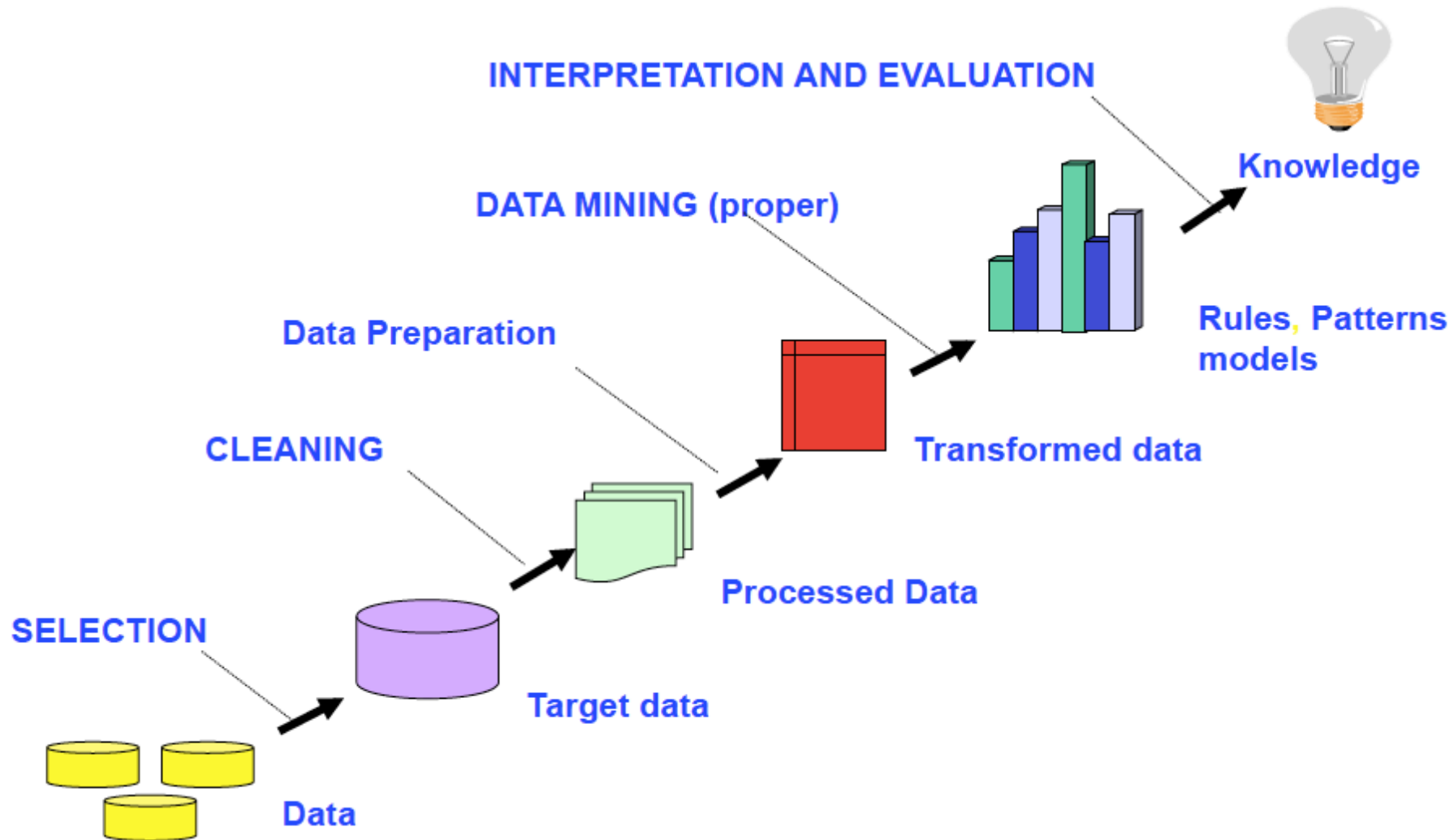
Problem: Classification by DTREE

1. Use the data below build a CLAFSSIFIER by basic DTREE algorithm
2. Use 2 different testing Method of your choice and compare the results

CLASSIFICATION DATA

Record	A1	A2	C
1	1	1	1
2	0	0	0
3	0	1	0
4	0	0	0
5	1	1	1
6	1	1	0
7	0	0	0
8	1	0	1

Data Mining Process



Preprocessing stage

- **Preprocessing:**
- includes all the operations that have to be performed before a data mining algorithm is applied
- **Data in the real world is dirty:** incomplete, noisy and inconsistent.
- **Quality decisions** must be based on quality Data.

Preprocessing stage

- **Data cleaning**
 - – Fill in missing values, smooth noisy data (binning, clustering, regression), identify or remove outliers, and resolve inconsistencies
- **Data integration**
 - – Integration of multiple databases, data cubes, or files

Preprocessing stage

- **Data transformation**
- **Normalization** and aggregation
- **Data reduction** and attribute selection
- Obtains reduced presentation in volume but produces the same or similar analytical results (stratified sampling, PCA, cluster)
- **Data discretization**
- Part of data reduction but **reduces the number of values of the attributes** by dividing the range of attributes into intervals (segmentation by natural partition, hierarchy generation)
-

Learning Proper

- **Learning proper** is a step in the **DM process** in which algorithms are applied to obtain patterns in data.
- It can be re-iterated- and usually is

Descriptive / non descriptive models

- **Statistical - descriptive**
- **Statistical** data mining uses historical data to predict some unknown or missing numerical values
- **Descriptive** data mining aims to find patterns in the data that provide some information about what the data contains
- often presents the knowledge as a set of rules of the form **IF.... THEN...**

Models

- **Discriptive:** Decision Trees, Rough Sets, Classification by Association
- **Statistical:** Neural Networks, Bayesian Networks, Cluster, Outlier analysis, Trend and evolution analysis
- **Optimization method:** Genetic Algorithms – can be descriptive

Classification

- **Classification:**
- Finding models (rules) that describe (characterize) or/ and distinguish (discriminate) classes or concepts for future prediction
- **Classification Data Format:**
- a data table with key attribute removed.
- Special attribute, called a **class attribute** must be distinguished.
- The values: **c1, c2, ...cn** of the class attribute C are called **class labels**
- The class label attributes are discrete valued and unordered.

Classification

- **Goal:**
- **FIND** a minimal set of **characteristic and/or discriminant rules**, or **other descriptions** of the class **C**, or all, or some other classes
- We also want the found rules to involve as few attributes as it is possible

Classification

- Stage 1: build the basic patterns structure- **training**
- Stage 2: optimize parameter settings; can use (N:N) re-substitution- **parameter tuning**
- Re-substitution error rate = training data error rate
- Stage 3: use **test data** to compute- predictive accuracy/error rate - **testing**

Decision Tree

- **DECISION TREE**
- A flow-chart-like tree structure;
- **Internal node** denotes an **attribute**;
- **Branch** represents the **values** of the node attribute;
- **Leaf nodes** represent **class labels**

DT Basic Algorithm

- The **basic DT algorithm** for decision tree construction is a greedy algorithm that constructs decision trees in a top-down recursive divide-and-conquer manner
- **Tree STARTS** as a single node representing all training dataset (data table with records called samples)
- **IF** the samples (records in the data table) are all in the same class, **THEN** the node becomes a leaf and is **labeled with that class**
- The algorithm uses the same **process recursively** to form a **decision tree** at each partition

DT Basic Algorithm

- The recursive partitioning **STOPS** only when any one of the following conditions is TRUE
- **1.** All records (samples) for the given node belong to the same class
- **2.** There are no remaining attributes on which the samples (records in the data table) may be further partitioned – a **LEAF** is created with **majority vote** for training sample
- **3.** There is no records (samples) left – a **LEAF** is created with **majority vote** for training sample
- **Majority voting** involves converting node **N** into a leaf and labeling it with the most common class in **D** which is a set of training tuples and their associated class labels

Attribute Selection Measures

- **Some Heuristics:**
- **Dtree:** some Attribute Selection Measures
- **Information Gain, Gini Index**

- We use them for selecting the **attribute** that **“best” discriminates** the given tuples according to **class**

Rule Based Systems REVIEW

Exercise

- Exercise 1
- Here are three simple **expert rules**
- **R1:** If your savings are small, then don't invest in stocks
- **R2:** If you have no children and large income, then invest in stocks
- **R3:** If you have children and small income, then invest in savings

Exercise 1

- **Conceptualize** rules **R1, R2, R3** in **Predicate Form** using predicates
attribute(x, value of attribute)
attribute(object, value of attribute)

WRITE a format of a **database TABLE** needed for your conceptualization

REMARK: In order to express the rules **Predicate Form**, we must first define appropriate **ATTRIBUTES** and their **values**

Exercise 1

- **We have the following ATTRIBUTES:**

- **Savings**

Values: **small, large**

- **Income**

Values: **small, large**

- **InvestStocks**

Values: **yes, no**

- **InvestSavings**

- Values: **yes, no**

- **Children**

Values: **yes, no**

Exercise 2

- Exercise 2
- The initial database has the following **FACTS**
- **F1:** Savings(John, small)
- **F2:** Children(John, no)
- **F3:** Income(John, large)
- Are these **FACTS** true in **Exercise 1** Data Table for some record $o = \text{John}$?
- Design a **Data Table 2** in which the above **FACTS** are true
- Can you deduce **InvestStocks(John, yes)** on the base of the **Data Table 2**

Exercise 1: Predicate Form Conceptualization

Data Table Example

Records	Savings	Income	InvesrStocks	InvestSavings	Children
O ₁	small	small	yes	yes	yes
O ₂	large	small	no	no	no
O ₃	small	large	yes	yes	no

Rules in Predicate Form

- **RULES:**
- **R1:** $\text{Savings}(x, \text{small}) \rightarrow \text{InvestStock}(x, \text{no})$
- **R2:** $\text{Children}(x, \text{no}) \wedge \text{Income}(x, \text{large}) \rightarrow \text{InvestStocks}(x, \text{yes})$
- **R3:** $\text{Children}(x, \text{yes}) \wedge \text{Income}(x, \text{small}) \rightarrow \text{InvestSavings}(x, \text{yes})$
-

Rules in Predicate Form

- **RULES:**
- **R1:** $\text{Savings}(x, \text{small}) \rightarrow \text{InvestStock}(x, \text{no})$
- **R2:** $\text{Children}(x, \text{no}) \wedge \text{Income}(x, \text{large}) \rightarrow \text{InvestStocks}(x, \text{yes})$
- **R3:** $\text{Children}(x, \text{yes}) \wedge \text{Income}(x, \text{small}) \rightarrow \text{InvestSavings}(x, \text{yes})$
-

Exercise 1: Rules in Predicate Form

- **RULES:**
- **R1:** $\text{Savings}(x, \text{small}) \rightarrow \text{InvestStock}(x, \text{no})$
- **R2:** $\text{Children}(x, \text{no}) \wedge \text{Income}(x, \text{large}) \rightarrow \text{InvestStocks}(x, \text{yes})$
- **R3:** $\text{Children}(x, \text{yes}) \wedge \text{Income}(x, \text{small}) \rightarrow \text{InvestSavings}(x, \text{yes})$
-

PART3: Exercise 2

- Exercise 2
- The initial database has the following **FACTS**
- **F1:** Savings(John, small)
- **F2:** Children(John, no)
- **F3:** Income(John, large)
- **1.** Are these **FACTS true** in **Exercise 1 Data Table** for a record $o = \text{John}$?
- **2.** Design a **Data Table 2** in which the above **FACTS** are true
- **3.** Can you deduce **InvestStocks(John, yes)** on the base of the **Data Table 2**

Part 3: Exercise 3

- Given rules from **Exercise 1**:
- **R1**: If your savings are small, then don't invest in stocks
- **R2**: If you have no children and large income, then invest in stocks
- **R3**: If you have children and small income, then invest in savings

Exercise 3

- **Conceptualize** rules **R1, R2, R3**

In **Propositional Logic** in two ways:

1. Rules admit **only atomic formulas**; i.e. rules are built from propositional variables only – call the set of rules **PR1**
2. Rules admit **atomic formulas** and **negation** of atomic formulas – call obtained set of rules **PR2**

Part 3: Exercise 3

- Write initial databases **B1** and **B2** of facts corresponding to the facts **F1, F2, F3** from **Exercise 2** for
 - (1) propositional conceptualization 1.
 - (2) propositional conceptualization 2.
 - (3) use corresponding rules from sets **PR1, PR2** to deduce all facts from **B1** and **B2**, respectively
- Use **Conflict Resolution** from Busse Handout