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Hidden Surface Removal

Diagram showing the process of hidden surface removal with two cubes: an original cube and a modified cube with hidden surfaces removed.
No Lines Removed
Hidden Lines Removed
Hidden Surfaces Removed
Hidden Surface Removal (a.k.a. Visibility)
Motivation

- Suppose that we have the polyhedron which has 3 totally visible surfaces, 4 totally invisible/hidden surfaces, and 1 partially visible/hidden surface.

- Obviously, invisible/hidden surfaces do not contribute to the final image during graphics production.

- The procedure that distinguishes between visible surfaces from invisible/hidden surfaces is called visible-surface determination, which is often called hidden-surface removal.
Motivation

- **Surfaces may be back-facing:**

  - Viewer
  - Back-Facing Polygon

- **Surfaces may be occluding:**

  - Viewer
  - Occluding Polygon
  - Occluded Polygon
Motivation

- **Surfaces may be overlapping:**

- **Surfaces may be intersecting:**
Occlusion: Full, Partial, None

- The rectangle is closer than the triangle
- Should appear in front of the triangle
Hidden Surface Removal

• Motivation

• Algorithms for Hidden Surface Removal
  – Back-face detection
  – Painter’s algorithm
  – Ray casting
  – Scan-line
  – Z-buffer
  – Area subdivision

• Tradeoffs when comparing different techniques
Image or Object Space Algorithms

• Ideally an object space method converts the 3D scene into a list of 2D areas to be painted
• Image space decides for each pixel which surface to paint
Hidden Surface Removal

- In 3D we must be concerned with whether or not objects are obscured by other objects.
- Most objects are opaque so they should obscure/block things behind them.
- Also Known As: visible surface detection methods or hidden surface elimination methods.
Visibility

- Basic assumption: All polygons are **opaque**
- What polygons are visible with respect to your view frustum?
  - **Outside:** View Frustum Clipping
    - Remove polygons outside of the view volume
    - For example, Liang-Barsky 3D Clipping
  - **Inside:** Hidden Surface Removal
    - Backface culling
      - Polygons facing away from the viewer
    - Occlusion
      - Polygons farther away are obscured by closer polygons
      - Full or partially occluded portions
- Why should we remove these polygons?
  - Avoid unnecessary expensive operations on these polygons later
Visibility Culling

- **Culling techniques**
  - *View-frustum culling*
    - Reject geometry outside the viewing volume
  - *Back-face culling*
    - Reject geometry facing away from the observer
  - *Occlusion culling*
    - Reject objects occluded by others
Back Face Culling

- Performance goals in real-time rendering
  - frame rate: 60-72 frames/sec?
  - resolution: 1600x1200?
  - photorealism (if necessary): undistinguishable from real scene!

- Unfortunately, there is no real upper limit on the scene complexity.

- We should *cull* those portions of the scene that are not considered to contribute to the final image as early as possible, and process only the rest of the scene.

- The simplest is *back-face culling*, which distinguishes between front faces (faces towards the viewer) and back faces (faces away from the viewer).
Backface Culling

• Avoid drawing polygons facing away from the viewer
  ➢ Front-facing polygons occlude these polygons in a closed polyhedron

• Test if a polygon is front- or back-facing?

Ideas?
Which Side of a Plane?

\[(p - n).n = 0\]
Detecting Back-face Polygons

- The polygon normal of a ...
  - front-facing polygon points **towards** the viewer
  - back-facing polygon points **away** from the viewer

If \((\mathbf{n} \cdot \mathbf{v}) > 0\) \(\Rightarrow\) “back-face”
If \((\mathbf{n} \cdot \mathbf{v}) \leq 0\) \(\Rightarrow\) “front-face”
\(\mathbf{v} = \) view vector

- **Eye-space test** ... **EASY**!
  - “back-face” if \(n_z < 0\)

- **glCullFace(GL_BACK)**
Polygon Normals

- Let polygon vertices \( v_0, v_1, v_2, \ldots, v_{n-1} \) be in counterclockwise order and co-planar
- Calculate normal with cross product:
  \[
  n = (v_1 - v_0) \times (v_{n-1} - v_0)
  \]
- Normalize to unit vector with \( n/\|n\| \)
Normal Direction

- Vertices counterclockwise ⇒ Front-facing
- Vertices clockwise ⇒ Back-facing
Back Face Culling

- Back-face culling works as a preprocessing step for hidden surface removal, and is very powerful in that almost half of polygons of an object are discarded as back faces.
- Especially, for a single convex polyhedron, the back-face culling does the entire job of hidden-surface removal.
- Hidden-surface removal is applied to only the remaining front faces.

single convex polyhedron  convex, but not a single polyhedron
Face Normal

- The normal of a triangle \(<p_1, p_2, p_3>\) is computed as \(v_1 \times v_2\) where \(v_1\) is the vector connecting \(p_1\) and \(p_2\), and \(v_2\) connects \(p_1\) and \(p_3\).

- If the vertices of every polygon are ordered consistently (CCW or CW), we can make every polygon’s normal point out of the polyhedron. All mesh data used in this class have triangles of CCW vertex ordering.

\[
\begin{align*}
\text{If the vertices of every polygon are ordered consistently:} & \\
\text{\(t_1 = (p, q, r)\)} & \\
\text{\(t_2 = (s, q, p)\)} & \\
\text{\(t_1\)'s normal = \((q-p)\times(r-p)\)} & \\
\text{\(t_2\)'s normal = \((q-s)\times(p-s)\)}
\end{align*}
\]
Dot Product (revisited)

- Recall the dot product of two vectors $v_i$ & $v_j$.
  - If $v_i \cdot v_j = 0$, $v_i$ & $v_j$ are orthogonal/perpendicular.
  - If $v_i \cdot v_j > 0$, $\text{angle} < 90$
  - If $v_i \cdot v_j < 0$, $\text{angle} > 90$
- The same applies to 3D.
Dot Product for Back Face Culling

- Determining if a polygon is a front face or a back face
  - Generate a vector $C$ connecting COP and a vertex of the polygon.
  - Take the dot product $C \cdot N$ of the vector $C$ and the polygon’s normal $N$.
  - If $C \cdot N > 0$, it’s a back face.
  - If $C \cdot N < 0$, it’s a front face.
  - If $C \cdot N = 0$, it’s a face that is projected as an edge/silhouette on the screen.
Back Face Removal (Culling)

- Used to remove unseen polygons from convex, closed polyhedron (Cube, Sphere)
- Does not completely solve hidden surface problem since one polyhedron may obscure another
Backface Culling

• For all polygons $P_i$
  – Find Polygon Normal $n$
  – Find Viewer Direction $v$
  – IF $(n \cdot v \leq 0)$
    • Then CULL $P_i$

• Does not work well for:
  – Overlapping front faces due to
    • Multiple objects
    • Concave objects
  – Non-polygonal models
  – Non-closed Objects
## Painter’s Algorithm

### Basic Idea
- A painter creates a picture by drawing background scene elements before foreground ones.

### Requirements
- **Draw polygons in back-to-front order**
- **Need to sort the polygons by depth order to get a correct image**
Painter’s Algorithm

1. Sort all objects’ $z_{\text{min}}$ and $z_{\text{max}}$
Painter’s Algorithm

1. Sort all objects’ $z_{\text{min}}$ and $z_{\text{max}}$

2. If an object is uninterrupted (its $z_{\text{min}}$ and $z_{\text{max}}$ are adjacent in the sorted list), it is fine
Painter’s Algorithm

1. **Sort all objects’** $z_{\text{min}}$ and $z_{\text{max}}$

2. **If an object is uninterrupted** (its $z_{\text{min}}$ and $z_{\text{max}}$ are adjacent in the sorted list), it is fine

3. **If 2 objects DO overlap**
   
   3.1 **Check if they overlap in** $x$
      
      - If not, they are fine

   3.2 **Check if they overlap in** $y$
      
      - If not, they are fine
      
      - If yes, need to split one
Painter’s Algorithm

• The splitting step is the tough one
  - Need to find a plane to split one polygon so that each new polygon is entirely in front of or entirely behind the other
  - Polygons may actually intersect, so then need to split each polygon by the other
Painter’s Algorithm

• **The splitting step is the tough one**
  - Need to find a plane to split one polygon so that each new polygon is entirely in front of or entirely behind the other.
  - Polygons may actually intersect, so then need to split each polygon by the other.

• **After splitting, you can resort the list and should be fine**
Painter’s Algorithm-Summary

• **Advantages**
  – Simple algorithm for ordering polygons

• **Disadvantages**
  – Sorting criteria difficult to produce
  – Redraws same pixel many times
  – Sorting can also be expensive
Painter’s Algorithm

- Compute $z_{\text{min}}$ ranges for each polygon
- Project polygons with furthest $z_{\text{min}}$ first
Depth Sorting

• The *painter’s algorithm*: draw from back to front

• **Depth-sort hidden surface removal:**
  – sort display list by z-coordinate from back to front
  – render/display

• **Drawbacks**
  – it takes some time (especially with bubble sort!)
  – it doesn’t work
Depth Sorting

- Requires ordering of polygons first
  - $O(n \log n)$ calculation for ordering
  - Not every polygon is either in front or behind all other polygons

- Order polygons and deal with easy cases first, harder later

Polygons sorted by distance from COP
Easy Cases

- **A lies behind all other polygons**
  - Can render

- **Polygons overlap in z but not in either x or y**
  - Can render independently
Depth Sorting Example

- **Painter’s Algorithm:**
  - Sort surfaces in order of decreasing maximum depth
  - Scan convert surfaces in order starting with ones of greatest depth, reordering as necessary based on overlaps

Diagram:
- View Plane
- Viewer
- Depth Sort
- A, B, C, D, E
Painter’s Example

Sort by depth:
- Green rect
- Red circle
- Blue tri
Hard Cases

Overlap in all directions but can one be fully on one side of the other

cyclic overlap

penetration
Painter’s Algorithm

- Problem: Can you get a total sorting?
Depth-sorting Difficulties

- Polygons with overlapping projections
- Cyclic overlap
- Interpenetrating polygons
- What to do?
Painter’s Algorithm

• **Cyclic Overlap**
  - How do we sort these three polygons?

• **Sorting is nontrivial**
  - Split polygons in order to get a total ordering
  - Not easy to do in general
Depth Sorting

- Completely in front – put in front
- Not overlapping in x, y – either
- Intersecting – divide along intersection
- Overlapping – divide along plane of one polygon.
Depth Sorting

- Cyclically overlapping surfaces that alternately obscure one another
- We can divide the surfaces to eliminate the cyclic overlaps
Painter’s Algorithm
The Painters Algorithm

- Sort polygons according to their z values and render from back to front
- Ends up drawing over the polygons in the back (more or less)
- Problems arise when polygons overlap or are allowed to pierce one another
- *Heedless Painter’s Algorithm*: sort by “farthest” point and draw in order
- *Depth sort* improves on this by splitting up overlapping polygons into less ambiguous pieces
Visibility

- How do we ensure that closer polygons overwrite further ones in general?
Image Space Approach

- Look at each projection (nm for an n x m frame buffer) and find closest of k polygons
- Complexity $O(nmk)$
- Ray tracing
- $z$-buffer
Ray Casting

- **Algorithm:**
  - Cast ray from viewpoint through each pixel to find front-most surface
The Z-buffer Algorithm

- The most widely-used hidden surface removal algorithm
- Relatively easy to implement in hardware or software
- An image-space algorithm which traverses scene and operates per polygon rather than per pixels
- We rasterize polygon by polygon and determine which (parts of) polygons get drawn on the screen
- Relies on a Secondary Buffer called the z-buffer or depth buffer
- Depth buffer has same width and height as the frame-buffer
- Each cell contains the z-value (distance from viewer) of the object at that pixel position
Z-Buffer

- Depth buffer (Z-Buffer)
  - A secondary image buffer that holds depth values
  - Same pixel resolution as the color buffer
  - Why is it called a Z-Buffer?
    - After eye space, depth is simply the z-coordinate

- Sorting is done at the pixel level
  - Rule: Only draw a polygon at a pixel if it is closer than a polygon that has already been drawn to this pixel
Z-Buffer Algorithm

- Visibility testing is done during **rasterization**

```java
for (each face F)
    for (each pixel (x, y) covering the face)
    {
        depth = depth of F at (x, y);
        if (depth < d[x][y])  // F is closest so far
            {
                c = color of F at (x, y);
                set the pixel color at (x, y) to c
                d[x][y] = depth;  // update the depth buffer
            }
    }
```
The Z-buffer Algorithm

1. Initialize all $depth(x, y)$ to 0 and $refresh(x, y)$ to background color

2. For each pixel
   1. Get current value $depth(x, y)$
   2. Evaluate depth value $z$
      if $z > depth(x, y)$
      then
      {  
        $depth(x, y) = z$
        $refresh(x, y) = I_s(x, y)$
      }
      Calculate this using shading algorithm/illumination/fill color/textured
Z-buffer: A Secondary Buffer

Color buffer

Depth buffer
Z-Buffer

• How do we calculate the depth values on the polygon interior?

\[ z_a = z_1 + (z_4 - z_1) \frac{(y_1 - y_s)}{(y_1 - y_4)} \]

\[ z_b = z_1 + (z_2 - z_1) \frac{(y_1 - y_s)}{(y_1 - y_2)} \]

\[ z_p = z_a + (z_b - z_a) \frac{(x_a - x_p)}{(x_a - x_b)} \]

Bilinear Interpolation
Example

Z-buffer

Screen
Parallel with the image plane
Not Parallel

[0,6,7]

[0,1,2]  [5,1,7]

\[
\begin{array}{cccccccc}
5 & 5 & 5 & 5 & 5 & 5 & 5 & \infty \\
5 & 5 & 5 & 5 & 5 & 5 & \infty & \infty \\
5 & 5 & 5 & 5 & 5 & \infty & \infty & \infty \\
5 & 5 & 5 & 5 & \infty & \infty & \infty & \infty \\
4 & 5 & 5 & 5 & \infty & \infty & \infty & \infty \\
3 & 4 & 5 & 6 & 7 & \infty & \infty & \infty \\
2 & 3 & 4 & 5 & 6 & 7 & \infty & \infty \\
\infty & \infty & \infty & \infty & \infty & \infty & \infty & \infty \\
\end{array}
\]
Z-Buffer Algorithm

- Algorithm easily handles this case
Z-buffering in OpenGL

- Create depth buffer by setting `GLUT_DEPTH` flag in `glutInitDisplayMode()` or the appropriate flag in the `PIXELFORMATDESCRIPTOR`

- Enable per-pixel depth testing with `glEnable(GL_DEPTH_TEST)`

- Clear depth buffer by setting `GL_DEPTH_BUFFER_BIT` in `glClear()`
Without Hidden surface removal the wrong polygons can be drawn over

With Backface culling

Alternatively we could cull the front faces to see inside the solid
No hidden surface removal

Culling can reduce workload for depth testing but we need to ensure that objects are proper **solids**. This teapot is not quite a proper solid and as a result the image is incorrect. However, combining backface culling with more expensive depth-testing is usually a good practice.
Scan Line Algorithm

• Similar in some respects to the z-buffer method but handles the image scan-line by scan-line
• Due to coherency in data, this can be relatively efficient.

1. Rasterize all polygon boundaries (edges)
2. Scanning across each scan line we determine the color of each pixel
   a. By default color everything as background
   b. If we encounter the edge of one polygon, start evaluating polygon color at each point and shade the scanline it accordingly
   c. For multiple edges do depth evaluation to see which polygon “wins”
Scan Line Algorithm

- Work one scan line at a time
- Compute intersections of faces along scanline
- Keep track of all “open segments” and draw the closest
Scan Line Algorithm

- Can combine shading and hsr through scan line algorithm

Scan line i: no need for depth information, can only be in no or one polygon

Scan line j: need depth information only when in more than one polygon
Scan Conversion

- At this point in the pipeline, we have only polygons and line segments. Render!
- To render, convert to pixels (“fragments”) with integer screen coordinates \((ix, iy)\), depth, and color
- Send fragments into fragment-processing pipeline
Hidden Surface Removal

- **Object-space vs. Image space**
- **The main image-space algorithm: z-buffer**
- **Drawbacks**
  - Aliasing
  - Rendering invisible objects
- **How would object-space hidden surface removal work?**
Visibility Testing

• In many real-time applications, such as games, we want to eliminate as many objects as possible within the application
  – Reduce burden on pipeline
  – Reduce traffic on bus

• Partition space with Binary Spatial Partition (BSP) Tree
Simple Example

consider 6 parallel polygons

The plane of A separates B and C from D, E and F
Painter’s Algorithm with BSP Trees

• **Building the tree**
  – May need to split some polygons
  – Slow, but done only once

• **Traverse back-to-front or front-to-back**
  – Order is viewer-direction dependent
  – However, the tree is viewer-independent
  – What is front and what is back of each line changes
  – Determine order on the fly
Divide Scene with a Plane

• Everything on the same side of that plane as the eye is in front of everything else.
• Divide front and back with more planes.
• If necessary split polygons by planes.
Details of Painter’s Algorithm

- Each face has form $Ax + By + Cz + D = 0$
- Plug in coordinates and determine
  - Positive: front side
  - Zero: on plane
  - Negative: back side
- **Back-to-front**: inorder traversal, farther child first
- **Front-to-back**: inorder traversal, near child first
- Do backface culling with same sign test
- Clip against visible portion of space (portals)
Binary Space Partition Trees (1979)

- **BSP tree**: organize all of space (hence *partition*) into a binary tree
  - *Preprocess*: overlay a binary tree on objects in the scene
  - *Runtime*: correctly traversing this tree enumerates objects from back to front
  - *Idea*: divide space recursively into half-spaces by choosing *splitting planes*
    - Splitting planes can be arbitrarily oriented
BSP Tree

- **Split space with any line (2D) or plane (3D)**
- **Applications**
  - Painters algorithm for hidden surface removal
  - Ray casting
  - Solid modeling
- **Inherent spatial ordering given viewpoint**
  - Left subtree: in front
  - right subtree: behind
- **Problem: finding good space partitions**
  - Proper ordering for the tree
  - Balance tree
BSP Tree

• **Can continue recursively**
  – Plane of C separates B from A
  – Plane of D separates E and F

• **Can put this information in a BSP tree**
  – Use for visibility and occlusion testing
Building BSP Trees

- Use hidden surface removal as intuition
- Using line 1 or line 2 as root is easy

![Diagram showing a BSP tree and line segments]

- A BSP tree using 2 as root
- The subdivision of space it implies
- Viewpoint
Building BSP Trees

- Using line 3 as root requires splitting
Building a Good Tree

• Naive partitioning of n polygons yields $O(n^3)$ polygons (in 3D)

• Algorithms with $O(n^2)$ increase exist
  – Try all, use polygon with fewest splits
  – Do not need to split exactly along polygon planes

• Should balance tree
  – More splits allow easier balancing
  – Rebalancing?
Binary Space Partitioning Trees

- Basic idea: Objects in the half space opposite of the viewpoint do not obscure objects in the half space containing the viewpoint; thus, one can safely render them without covering foreground objects.
Binary Space Partitioning Trees

- Basic Idea: Objects in the half space opposite of the viewpoint do not obscure objects in the half space containing the viewpoint; thus, one can safely render them without covering foreground objects.

If we want to draw 5 correctly:
- we need draw 6 and 7 first,
- then draw 5,
- then draw 1, 2, 3, 4.
Binary Space Partitioning Trees

- **Basic principle**: Objects in the half space opposite of the viewpoint do not obscure objects in the half space containing the viewpoint; thus, one can safely render them without covering foreground objects.

If we want to draw 5 correctly:
- we need draw 6 and 7 first,
- then draw 5,
- then draw 1, 2, 3, 4

We need to do this for every polygon.

Can we do this efficiently?
Binary Space Partition Trees

- **BSP tree**: organize all of space (hence *partition*) into a binary tree
  - **Preprocess**: overlay a binary tree on objects in the scene
  - **Runtime**: correctly traversing this tree enumerates objects from back to front
  - **Idea**: divide space recursively into half-spaces by choosing *splitting planes*
- **Splitting planes can be arbitrarily oriented**
BSP-Trees

- **Binary Space Partition Trees**
  - Split space along planes
  - Allows fast queries of some spatial relations

- **Simple construction algorithm**
  - Select a plane as sub-tree root
  - Everything on one side to one child
  - Everything on the other side to other child
  - Use random polygon for splitting plane
BSP-Trees
BSP-Trees
BSP-Trees
BSP-Trees
BSP-Trees

Diagram showing a BSP tree with nodes labeled as follows:
- Node a
- Node b
- Node c₂
  - Node c₁
  - Node d
  - Node e₁
  - Node e₂, g
  - Node f

Diagram also includes lines labeled as:
- a
- b
- c₁
- e₁
- e₂
- g
- f
- c₂
BSP-Trees

Diagram showing BSP-Trees with nodes and edges labeled with letters.
How Do We Traverse BSP Tree?

- **Visibility traversal based on BSP tree**
  - **Variation of in-order-traversal**
    - Child one
    - Sub-tree root
    - Child two
  - Select “child one” based on location of viewpoint
    - Child one on same side of sub-tree root as viewpoint
BSP-Trees

c_1:b:d:a:f:e_1:c_2:g:e_2
BSP-Trees

g:e_2;c_2:f:e_1:a:c_1:b:d
BSP Trees: Another Example
BSP Trees: Objects
BSP Trees: Objects
BSP Trees: Objects
BSP Trees: Objects
BSP Trees: Objects
BSP Trees: Objects

When to stop the recursion?
Object Splitting

- No bunnies were harmed in my example
- But what if a splitting plane passes through an object?
  - Split the object; give half to each node;
  - Worst case: can create up to $O(n^3)$ objects!

Ouch
Polygons: BSP Tree Construction

• Split along the plane containing any polygon
• Classify all polygons into positive or negative half-space of the plane
  – If a polygon intersects plane, split it into two
• Recursion down the negative half-space
• Recursion down the positive half-space
BSP Trees: Objects

Traversal order?
BSP Trees: Objects

Traversal order:
8 -> 9 -> 7 -> 6 -> 5 -> 3 -> 4 -> 2 -> 1
Building a BSP Tree for Polygons

- Choose a splitting polygon
- Sort all other polygons as
  - Front
  - Behind
  - Crossing
  - On
- Add “front” polygons to front child, “behind” to back child
- Split “crossing” polygons with infinite plane
- Add “on” polygons to root
- Recursion
Building a BSP Tree

1 2

3

4 5

6 7
Building a BSP Tree

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Building a BSP Tree
Building a BSP Tree

How to divide 2,3,4,5,6,7?
Building a BSP Tree
Building a BSP Tree

Diagram showing the construction of a BSP tree with labels 1, 2, 3, 4, 5, 6, and 7, indicating the division of space into regions.
Building a BSP Tree
Building a BSP Tree

Diagram showing the construction of a BSP tree with labeled nodes and planes.
Building a BSP Tree
Building a BSP Tree
Building a BSP Tree
Building a BSP Tree
Building a BSP Tree
Building a BSP Tree
Rendering with a BSP Tree

- If eye is in front of plane
  - Draw “back” polygons
  - Draw “on” polygons
  - Draw “front” polygons

- If eye is behind plane
  - Draw “front” polygons
  - Draw “on” polygons
  - Draw “back” polygons

- Else eye is on plane
  - Draw “front” polygons
  - Draw “back” polygons
Building a BSP Tree

Traversal order:

b b b b f f
Building a BSP Tree

Traversal order:
6 -> (5-2) -> (7-2) -> 3 -> (5-1) -> 4 -> (7-1) -> 2 -> 1
Building a BSP Tree

Traversal order:
1 -> 3
2

1

4

5-1

6

5-2

7-1

7-2
Building a BSP Tree

Traversal order:
1->2->(7-1)->4->(5-1)->3->(7-2)->(5-2)->6
Building a BSP Tree

Traversal order?
Summary: BSP Trees

• Pros:
  – Simple, elegant scheme
  – No depth comparisons needed
  – Polygons split and ordered automatically
  – Only writes to framebuffer (i.e., painters algorithm)
Summary: BSP Trees

- **Cons:**
  - Computationally intense preprocess stage restricts algorithm to static scenes
  - Splitting increases polygon count
  - Redraws the same pixel many times
  - Choosing splitting plane not an exact science
Improved BSP Rendering

- Take advantage of view direction to cull away polygons behind viewer
Improved BSP Rendering

- Take advantage of view direction to cull away polygons behind viewer

View frustum
Efficiency

- BSP trees are order $n \log(n)$ in the number of polygons.
- Good for VR ‘walkthrough’ because you only re-compute when the eye crosses a separating plane.
Z-Buffer

- Record r, g, b and z (depth) for each pixel.
- Process each polygon line by line and if closer replace r, g, b, z in the buffer.
Scan Line in Screen Space
Area Subdivision

• Fill area if:
  • All surfaces are outside
  • Only one surface intersects
  • One surface occludes other surfaces within area.

• Otherwise, subdivide
The Warnock’s Algorithm

- The Warnock algorithm divides the screen into smaller areas and sorts triangles within these. If there is ambiguity (i.e., polygons overlap in depth extent within these areas), then further subdivision occurs. At the limit, subdivision may occur down to the pixel level.
Warnock Algorithm

- Takes advantage of *area coherence*: divide the display area into successively smaller rectangles until the entire rectangle can be filled with a single color.
Finding the Depth

- Plane equation is $Ax + By + Cz + D = 0$
- $z = - \frac{Ax + By + D}{C}$
- replace $x$ by $x+1$
- $z' = - \frac{A(x+1) + By + D}{C}$
- $\Delta z = z' - z = -\frac{A}{C}$
- New $z$ is found by adding a constant.